

Lecture note on
Circuit and Network Theory
3rd Sem Electrical Engineering

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* Introduction

- ⇒ Every elements in the surrounding are made up of sub atomic particles known as atoms.
- ⇒ So, every materials are made up of infinite no. of atoms.
- ⇒ In an atom several sub atomic particles are found i.e. electrons and nucleus.
- ⇒ The electrons are revolving around the nucleus as planets are revolving around the sun, in a specific path known as orbit.
- ⇒ So, the electron possess specific energy while revolving around, the nucleus.
- ⇒ Inside the nucleus we also found out sub atomic particles like proton and neutron with some binding energy.
- ⇒ The electrons are made free by applying external energy.
- ⇒ Now the electrons are free from the hold of nucleus and moves to other near by atoms.
- ⇒ According to the scientist, Rutherford, the electrons are $-ve$ charge particles.
- ⇒ So, after free electrons from one atom nucleus moves towards neighbour atom.

→ The electron was discovered by
J.J. Thomson.

⇒ The atom which donate electrons to the other atoms is known as +ve charge.

⇒ The atom which received electrons becomes -ve known as -ve charge.

⇒ So, +ve and -ve charge are atoms having deficient of electrons or excess of electrons.

⇒ Loss of electrons of an atom +ve charge.

⇒ Gain of electrons of an atom -ve charge.

⇒ The energy which are able to released electrons from atoms are heat energy, Thermal energy, magnetic energy, chemical energy etc.

→ Current (I)

⇒ The current may be defined as flow of charge (electrons) per unit time.

⇒ Unit - Ampere

⇒ Charge unit → Coulomb.

⇒
$$\text{Current} = \frac{\text{Charge}}{\text{Time}}$$

$$I = \frac{Q}{t}$$

$$\Rightarrow 1A = \frac{1C}{1s} = 1C/sec.$$

1A is defined as the 1 coulomb of charge that displace or flow with 1 second.

$$1KA = 10^3 A \quad \leftarrow \text{Higher unit}$$

$$1MA = 10^6 A$$

Lower unit \rightarrow

$$1mA = 10^{-3} A$$

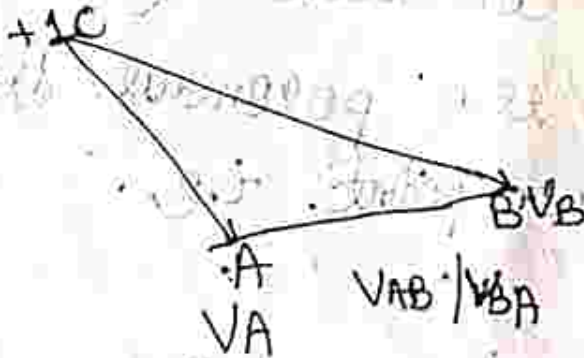
$$1\mu A = 10^{-6} A$$

* Potential \Rightarrow Dt: 02.08.20

\Rightarrow It is the workdone to bring a unit +ve charge from infinity to a particular point.

\Rightarrow It is denoted by 'V'.

\Rightarrow Let; V_A and V_B are two potential.



\Rightarrow Similarly the positive 1C charge moves to B' point and potential at B' point is $V_{B'}$.

* Potential difference in voltage \Rightarrow ΔV
 \Rightarrow It is defined as the difference of potential of two certain points.

$$V_{AB} = V_A - V_B$$

$$V_{BA} = V_B - V_A$$

\Rightarrow unit is Volt.

\Rightarrow Higher unit

$$1 \text{KV} = 10^3 \text{V}$$

$$1 \text{MV} = 10^6 \text{V}$$

\Rightarrow Lower unit

$$1 \text{mV} = 10^{-3} \text{V}$$

$$1 \mu\text{V} = 10^{-6} \text{V}$$

\Rightarrow Ohm's Law

\Rightarrow At constant temperature the current flowing through the conductor is directly proportional to the potential difference between two points. i.e.

$$V \propto I$$

$$\Rightarrow V = IR$$

$R =$ Resistance of conductor.

* Resistance (R)

⇒ It is defined as the property of materials which opposed the flow of charge ~~within~~ within certain potential difference.

⇒ Resistance may be defined as the ratio of flow of 1A of current within the potential difference of 1V.

⇒ Unit \rightarrow Ohm (Ω)

$$R = \frac{V}{I}$$

$$\Rightarrow 1\Omega = \frac{1V}{1A}$$

⇒ Higher units

$$1M\Omega = 10^6\Omega$$

$$1K\Omega = 10^3\Omega$$

⇒ Lower units

$$1m\Omega = 10^{-3}\Omega$$

$$1\mu\Omega = 10^{-6}\Omega$$

DL: 10.08.2020

Laws of Resistance

It is a property of a material which opposes flow of current or flow of charge. The material which obey this property is known as resistance.

The resistance seen in a material is directly proportional to the length of the material and inversely proportional to the cross-sectional area.

$$R \propto l \text{ (Length)}$$

$$R \propto \frac{1}{a} \text{ (Cross-sectional Area)}$$

$$\Rightarrow R \propto \frac{l}{a}$$

$$\Rightarrow R = \rho \frac{l}{a}$$



ρ is equal the proportionality constant. (Respectively).

$$\Rightarrow \rho = \frac{Ra}{l} = \frac{\Omega \times \text{cm}^2}{\text{cm}} = \boxed{\Omega \text{ cm}}$$

* Resistance & Temperature relationship:

Let R_0 = Resistance of material at 0°C .

R_t = Resistance of material at $t^\circ\text{C}$.

$$\boxed{R_t = R_0 (1 + \alpha t)}$$

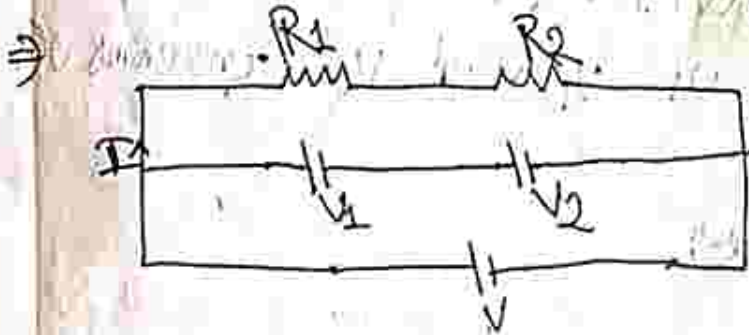
α = coefficient of resistance

$R_0 > R_e$

~~⇒ If temperature~~

* Resistance in series

⇒ If one or more resistances are connected end to end position, then the connection is known as series connection.



⇒ Here, R_1 and R_2 are two resistances and are connected in series across ' V ' volt.

⇒ The current flows ' I ' and the voltage ' V ' is divided across ' R_1 ' and ' R_2 ' in ' V_1 ' and ' V_2 '.

⇒ In series connection voltage should be divided but current flow is same.

$$\text{So; } V = V_1 + V_2$$

⇒ According to Ohm's law:

$$V = I R_{se}, V_1 = I \times R_1, V_2 = I \times R_2$$

where, R_{se} = Total series resistances.

Putting the above values:

$$V = V_1 + V_2$$

$$\Rightarrow I R_{se} = I R_1 + I R_2$$

where, $R_{se} = \text{Total series resistance}$

$$\Rightarrow R_{se} = R_1 + R_2$$

$$\Rightarrow R_{se} = R_1 + R_2$$

* Voltage Division Rule

\Rightarrow In voltage division rule we have to find out value of V_1 and V_2 in terms of V .

\Rightarrow We know that;

$$V = IR_{se}$$

$$\Rightarrow V = I(R_1 + R_2)$$

$$\Rightarrow I = \frac{V}{R_1 + R_2}$$

\Rightarrow Again, we know that

$$V_1 = IR_1$$

$$\Rightarrow V_1 = \frac{V}{R_1 + R_2} \times R_1$$

\Rightarrow Similarly,

$$V_2 = \frac{V}{R_1 + R_2} \times R_2$$

* Resistance in parallel
~~mix mix mix mix~~



⇒ In parallel connection, the similar ends of resistances are groups in two distinct points and voltage is apply across it, this type of connection is known as parallel connection.

⇒ In this circuit diagram R_1 and R_2 are two resistances are connected in parallel across A and B . And the voltage V is apply across it.

⇒ So, voltage V appears R_1 and R_2 whereas the current taking by R_1 and R_2 are I_1 and I_2 and the total current is I .

⇒ In parallel connection, voltage across each resistances are same, whereas current is divided.

⇒ According to ohm's law;

$$I = \frac{V}{R_p}, I_1 = \frac{V}{R_1}, I_2 = \frac{V}{R_2}$$

$$\therefore I = I_1 + I_2$$

$$\Rightarrow \frac{V}{R_p} = \frac{V}{R_1} + \frac{V}{R_2}$$

$$\Rightarrow \frac{V}{R_p} = V \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$$

$$\Rightarrow \frac{1}{R_p} = \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$$

$$\Rightarrow \frac{1}{R_p} = \frac{R_1 + R_2}{R_1 R_2}$$

$$\Rightarrow \frac{1}{R_p} = \frac{R_1 + R_2}{R_1 R_2}$$

$$\Rightarrow R_p = \frac{R_1 R_2}{R_1 + R_2}$$

Where R_p = Total parallel resistance.

* Current Division Rule \Rightarrow

\Rightarrow In parallel circuit ~~we~~ we know that voltage across each resistance are same but current is divided.

\Rightarrow So; we have to find out in terms of I_1 and I_2 .

$$\Rightarrow V = IR_p$$

$$\Rightarrow I = \frac{V}{R_p}$$

$$R_p = \frac{R_1 R_2}{R_1 + R_2}$$

$$I_1 = \frac{V}{R_1} = \frac{IR_p}{R_1}$$

$$\Rightarrow I_1 = \frac{I}{R_1} \times \frac{R_1 R_2}{R_1 + R_2}$$

$$\Rightarrow I_1 = \frac{IR_2}{R_1 + R_2}$$

Similarly

$$I_2 = \frac{IR_1}{R_1 + R_2}$$

Faraday's Law

Faraday also known as father of electricity.

1st Law → When there is change in position of either magnet or conductor then an emf induced in the conductor.

2nd Law → It gives the magnitude of induced emf.

→ According to Faraday, the emf induced is directly proportional to the change of flux. And inversely proportional to the change of time, t_2 .

$\therefore e \propto \Phi_2 - \Phi_1$

where Φ_1 - Flux of time t_1
 Φ_2 - Flux of time t_2

$\Rightarrow e \propto \frac{1}{t_2 - t_1}$

$\Rightarrow e \propto \frac{\Phi_2 - \Phi_1}{t_2 - t_1}$

$\Rightarrow e \propto \frac{d\Phi}{dt}$ (rate of change of flux w.r.t. time)

$\Rightarrow e = \frac{N d\Phi}{dt}$ (N = NO. of turns of the conductor)

* Lenz's law ⇒

⇒ Faraday predicted only about induced emf but does not predict about direction of induced emf which can be later predicted by Lenz.

⇒ Statement ⇒ According to Lenz, the direction of induced emf is such that it opposes the very cause by which it is produced.

So,
$$e = -N \frac{d\phi}{dt}$$

* Fleming's Right Hand Rule ⇒

⇒ The three fingers of right hand (Fore finger, middle finger and thumb) are stretched in such a way that they are mutually perpendicular to each other such that the thumb represents relative motion of the conductor, fore finger represents the ^{direction of} magnetic field and the middle finger represents the direction of flow of current.

⇒ This principle is used in dc generator.

$$I = \frac{E}{R}$$

$$E = \frac{d\phi}{dt}$$

* Fleming's Left Hand Rule

- ⇒ The three fingers of left hand are stretched in such a way that they are mutually perpendicular to each other.
- ⇒ If middle finger represents the flow of current in conductor, fore finger represents the direction of magnetic field then thumb represents the motion of the conductor.
- ⇒ This law is applicable for DC motor.

* Inductance

- ⇒ It is the property of a material which does not allow sudden change of current.
- ⇒ It is denoted by letter L or L' .
- ⇒ Unit is Henry.
- ⇒ It is wire wound having several number of turns. The function of inductor is to store energy (electrical energy).
- ⇒ Energy stored by inductor $\Rightarrow E = \frac{1}{2} LI^2$
- Where, I = current flow through the conductor, which obeys this E known as inductor.
- L = Inductance of inductor.
- E = energy

* Capacitance ⇒

⇒ It is the property of a material which does not allow sudden change of voltage.

⇒ It is denoted by 'C' or 'c'.

⇒ Unit is 'Farad'.

⇒ The material which obeys this property is known as capacitor. It about stored energy.

in capacitor $E = \frac{1}{2} CV^2$

where; E = Energy

C = capacitance of the capacitor

V = Voltage

⇒ The charge stored in capacitor when voltage is applied so, charge stored by the capacitor is directly proportional to voltage.

i.e. $Q \propto V$

⇒ $Q = CV$

DT: 20-08-2020

* Parameter ⇒ R-L-C

⇒ The various circuit elements of an electric circuit are called its parameter.

* Linear circuit ⇒ The circuit which have linear element whose value does not ^{change} whatever the current or voltage may be.

* Non-Linear Circuit \Rightarrow

\Rightarrow The circuit which have, ~~linear~~ elements that change according to current or voltage are known as non-linear circuit.

* Bilateral Circuit \Rightarrow

\Rightarrow It is a circuit whose properties or characteristics are the same in either direction.
Ex- Transmission line.

* Uni-lateral Circuit \Rightarrow

\Rightarrow It is a circuit whose properties or characteristics change with the direction of operation.

* Active Network (Circuit) \Rightarrow

\Rightarrow The network in which one or more sources are present is known as active network.

* Passive Network \Rightarrow

\Rightarrow In this type of network no emf sources are present.

* Power (P) \Rightarrow The rate of doing work, is called power.

\Rightarrow Its unit is watt, kilowatt, mega-watt.

\Rightarrow Symbol is 'P'.

\Rightarrow $P = VI$; $P = I^2 R$; $P = \frac{V^2}{R}$

\Rightarrow There are three types of power, they are:-

1. Active power or True power or Real power.

2. Reactive power.

3. Apparent power.

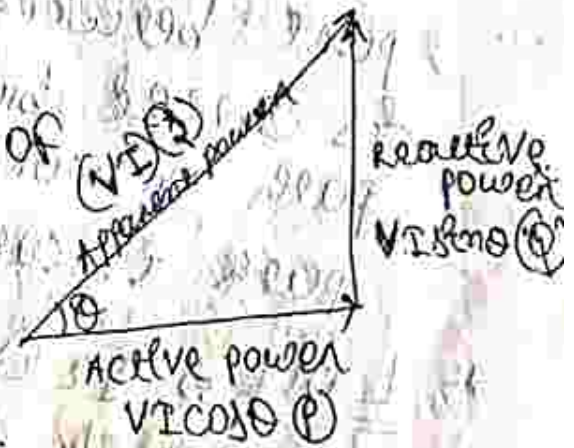
\Rightarrow Power triangle is a right angle triangle which represents the relationship between active, reactive, and apparent power.

(a) Active power \Rightarrow

\Rightarrow Active power is a product of voltage, current and power factor.

\Rightarrow $VI \cos \theta$, symbol is 'P'.

\Rightarrow Unit is watt, kW, MW.



(b) Reactive power \Rightarrow

\Rightarrow The power which is consumed by reactance of the circuit.

\Rightarrow $VI \sin \theta$, symbol is (Q).

\Rightarrow Unit is VAR, KVAR, MVAR. (VAR = Volt ~~reactive~~ Ampere Reactive)

© Apparent power \Rightarrow

maximum

\Rightarrow It is a product of voltage and current taken by the load.

$\Rightarrow VI$, symbol is S .

\Rightarrow units are VA, KVA, MVA.

DT 24.08.2020

* Node

\Rightarrow It is a junction in a circuit where two or more circuit elements are connected together that is called node point.

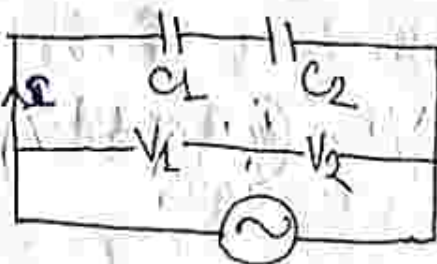
* Branch \Rightarrow It is a connecting link or path between any two node points that is called branch; that branch may one path or more than one path that one path is called branch.

* Loop \Rightarrow It is a closed path in a circuit in which no elements or node points are encountered.

* mesh \Rightarrow mesh is a loop in which no other loop is encountered.

* Capacitors are in series \Rightarrow
 $\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$

\Rightarrow



\Rightarrow In series connection current flow is same on voltage is divided.

$$V = V_1 + V_2$$

$$\Rightarrow \frac{Q}{C} = \frac{Q}{C_1} + \frac{Q}{C_2}$$

$$\Rightarrow \frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2}$$

$$\Rightarrow C = \frac{C_1 C_2}{C_1 + C_2}$$

* Capacitors are in parallel \Rightarrow
 $\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$



\Rightarrow In parallel connection of capacitor voltage flow is same on current is divided.

$$I = I_1 + I_2$$

$$\Rightarrow Q = Q_1 + Q_2$$

$$\Rightarrow CV = C_1V + C_2V \quad (\because Q = CV)$$

$$\Rightarrow \boxed{C = C_1 + C_2}$$

DT: 27.08.2020

* Resistance \Rightarrow

\Rightarrow It is defined as the property of materials which oppose the flow of current when certain potential difference

* Resistor \Rightarrow It is the material or elements which obey the resistance property.

\Rightarrow Denoted by $\rightarrow R$ or ρ .

\Rightarrow Unit $\rightarrow \text{ohm } \frac{V}{A}$

* Laws of Resistance \Rightarrow

\Rightarrow The resistance seen of a material or element is directly proportional to the length of the material or element and inversely proportional to the cross-sectional area of the element.

$\Rightarrow R \propto l$ (length of the element or material)

$$\Rightarrow R \propto \frac{l}{a}$$

$$\Rightarrow R \propto \frac{l}{a} \Rightarrow R = \rho \frac{l}{a}$$

where, ' ρ ' is known as proportionality constant or resistivity or specific resistance of the materials.

$$\text{So, } \rho = \frac{R \times a}{l}$$

\Rightarrow unit, ohm metre

(\Rightarrow) ohm.cm

* Temperature coefficient of the resistance \Rightarrow

\Rightarrow The resistance of a material at a certain temperature is directly proportional to the change of temperature and also proportional to the initial resistance.

$$\text{So, } \Delta R \propto R_0$$

$$\Rightarrow \Delta R \propto t_2 - t_1$$

$$\Rightarrow \Delta R \propto R_0 (t_2 - t_1)$$

$$\Rightarrow \Delta R = \alpha R_0 (t_2 - t_1)$$

where, R_0 = Initial value of resistance of the materials.

ΔR = Change of Resistance

t_1 = Initial Temperature.

$t_2 =$ Final Temperature

$\alpha =$ Proportionality constant

$\Delta t = (t_2 - t_1) =$ Change of Temperature

$R_t =$ Resistance of the material at temperature t on decreasing temperature

$$\text{So, } R_t = R_0 + \Delta R$$

$$\Rightarrow R_t = R_0 + \alpha R_0 (t_2 - t_1)$$

$$\Rightarrow R_t = R_0 + \alpha R_0 \Delta t$$

$$\Rightarrow R_t = R_0 (1 + \alpha \Delta t)$$

Direction

* Resistance are in series

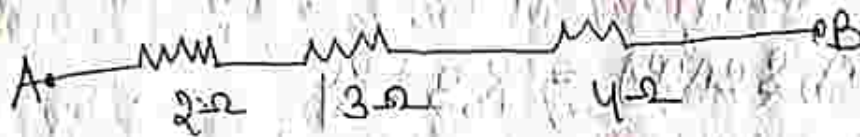


\Rightarrow If the identical ends of resistances are connected at various distinct points then the connection form is known as series connection.

Here, ' R_1 ' and ' R_2 ' are connected in series across a voltage of V volt.

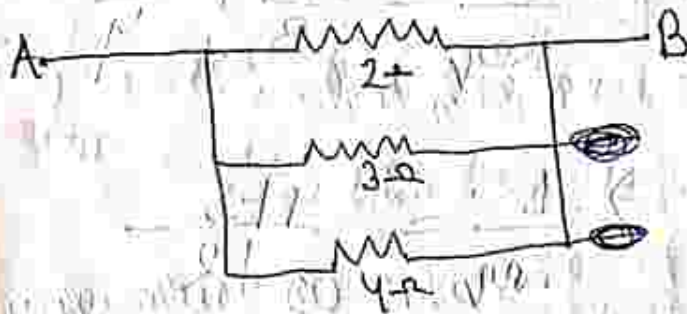
Q101 Find the equivalent resistance between the terminals A and B?

Soln.



$$\therefore R_{eq} = R_1 + R_2 + R_3 = 2 + 3 + 4 = 9\Omega$$

Q102



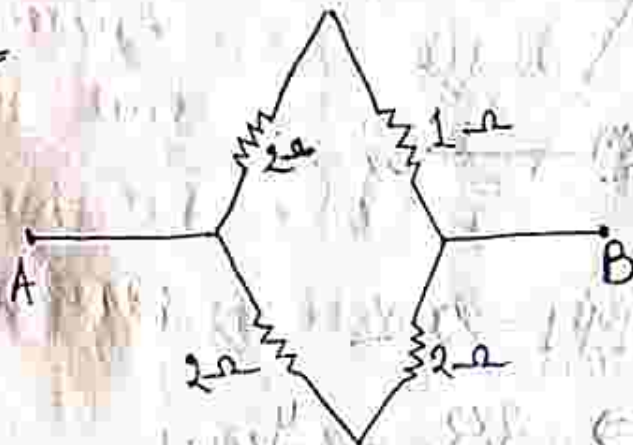
$$\therefore R_{eq} \text{ for parallel} \rightarrow \frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

$$= \frac{1}{2} + \frac{1}{3} + \frac{1}{4}$$

$$= \frac{13}{12}$$

$$\therefore R_{eq} = \frac{12}{13} \Omega$$

Q103



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* Kirchhoff's Law \Rightarrow

(1) KCL (Kirchhoff's Current Law) on ~~node~~ Junction

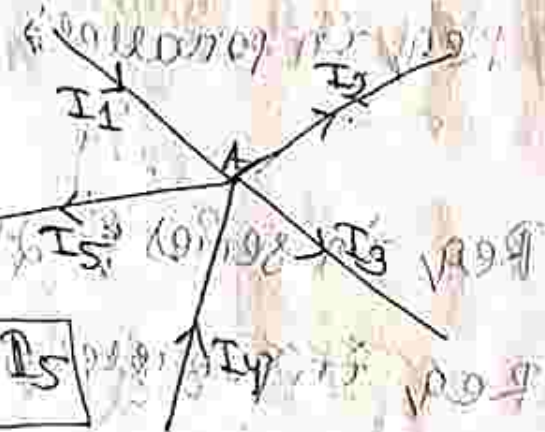
\Rightarrow In any electrical network, the algebraic sum of the currents meeting at a point or (Junction) is zero.

\Rightarrow Incoming currents are taken as +ve and the outgoing currents are taken as -ve.

$$\Rightarrow I_1 + (-I_2) + (-I_3) + (-I_4) + (-I_5) = 0$$

$$\Rightarrow I_1 + I_4 - I_2 - I_3 - I_5 = 0$$

$$\Rightarrow \boxed{I_1 + I_4 = I_2 + I_3 + I_5}$$



\Rightarrow Hence, Total incoming current = Total outgoing current.

\Rightarrow From KCL, it is confirmed that total incoming current to the node is equal to the total outgoing current from node.

(2) KVL \Rightarrow Kirchhoff's Voltage Law (on Loop or mesh)

\Rightarrow Statement \Rightarrow The algebraic sum of the products of currents and resistances in each of the conductors for any closed path (or mesh) in a network, plus the algebraic sum of the e.m.f.s in that path is zero.

$$\Rightarrow \boxed{\sum IR + \sum e.m.f. = 0}$$

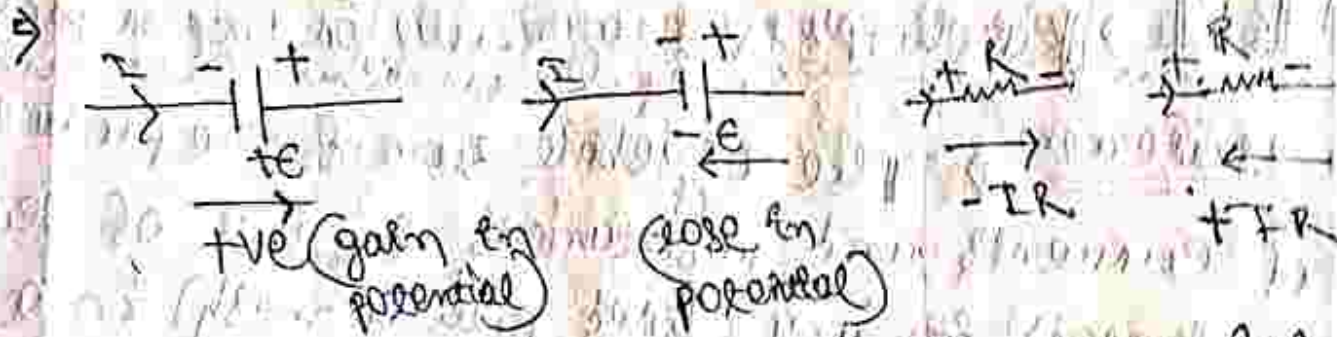
\Rightarrow Step (1) \Rightarrow We have to consider the path in which we have to follow (Always in clockwise direction).

\Rightarrow Step (2) \Rightarrow In this step we have to mention the current direction in each element and current sources.

\Rightarrow Step (3) \Rightarrow Before applying KVL we must consider a direction in which we move and show the element.

\Rightarrow Step (4) \Rightarrow The direction must be left to right.

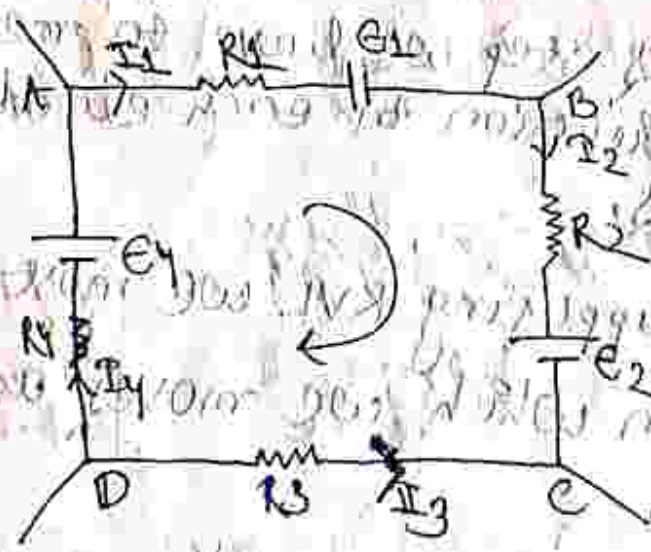
\Rightarrow Step (5) \Rightarrow ~~The direction must be a~~ During movement, there are 4 conditions arise.



⇒ The algebraic sum of all the potential meeting across a closed circuit or closed loop is equal to zero.

$$\sum V - \sum IR = 0$$

⇒ Solve by KVL



(i) ABCDA is closed circuit so KVL is applied to the circuit.

(ii) we should now consider the path that we follow the path is always clockwise i.e. ABCDA.

80; $\sum E + \sum IR = 0$

$\Rightarrow -I_1 R_1 - E_1 - I_2 R_2 - E_2 + I_3 R_3 - I_4 R_4 + E_4 = 0$

$\Rightarrow -(I_1 R_1 + E_1 + I_2 R_2 + E_2 - I_3 R_3 + I_4 R_4 - E_4) = 0$

$\Rightarrow (E_1 + E_2 - E_4) + (I_1 R_1 + I_2 R_2 - I_3 R_3 + I_4 R_4) = 0$

New chapter (Superposition Theorem) Dt. 30.9.20

* Superposition Theorem \Rightarrow

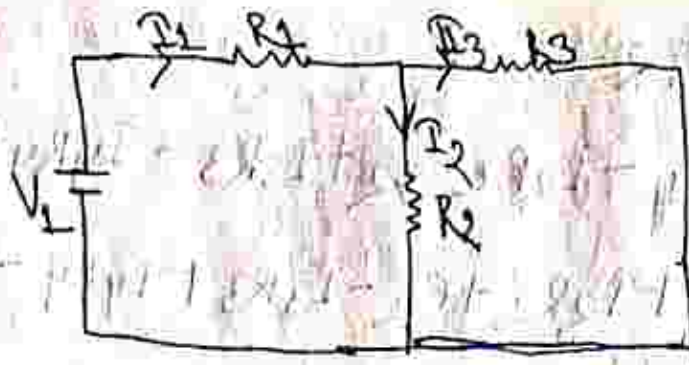
statement \Rightarrow In a linear, bilateral, active network containing more than one source, the current flowing through any circuit elements or resistance is determined by considering individual source one at a time, while other sources get ignore leaving behind its internal resistances.

* steps

① To determine current across R_2 by superposition theorem.



step 2 considering V_1 source at that time V_2 source get ignore i.e. V_2 source get short circuit.

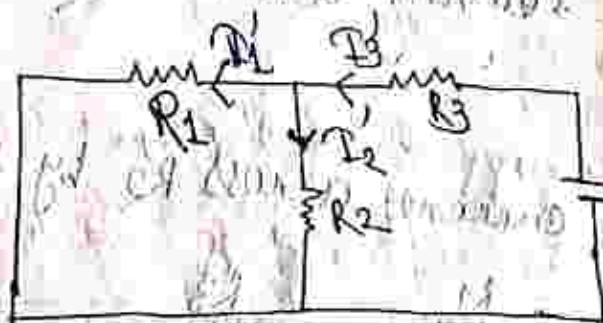


$$I_1 = \frac{V_1}{R_{eq(1)}} \quad , \quad R_{eq(1)} = (R_2 || R_3) + R_1$$

\therefore So, I_2 (According to current division rule)

$$I_2 = \frac{I_1 \times R_3}{R_2 + R_3} \quad (\text{Direction up} \rightarrow \text{Down})$$

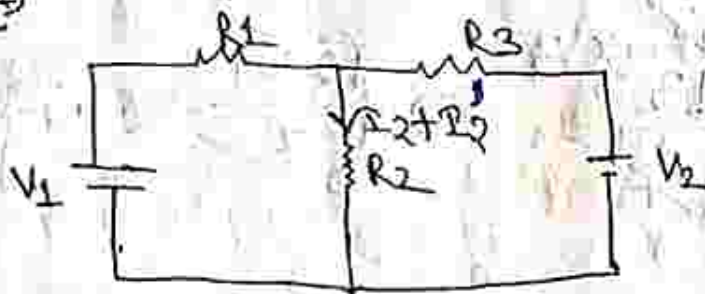
Step 2 Considering V_2 source at that time we'll get ignore on short circuit.



$$I_3' = \frac{V_2}{R_{eq(2)}} \quad , \quad R_{eq(2)} = R_3 + (R_1 || R_2)$$

$$I_2' = \frac{I_3' \times R_1}{R_1 + R_2} \quad (\text{Direction is up} \rightarrow \text{down})$$

step 3



$I_2 \text{ (total)} = I_2 + I_2'$ (as both the directions are same).

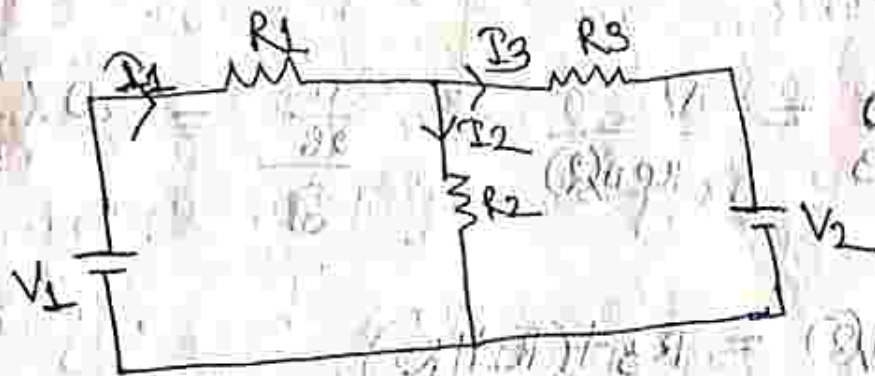
Q301

$V_1 = 10V, V_2 = 20V$

$R_1 = 2\Omega, R_2 = 4\Omega, R_3 = 3\Omega$

Determine the current across R_2 ?

soln.



step 1



$I_1 = \frac{V_1}{R_{eq(1)}} = \frac{10}{\frac{26}{7}} = 10 \times \frac{7}{26} = \frac{35}{13} A$

$R_{eq(1)} = (R_2 || R_3) + R_1$
 $= \frac{4 \times 3}{4 + 3} + 2 = \frac{12}{7} + 2 = \frac{26}{7} \Omega$

$$I_2 = \frac{30 \sqrt{3}}{13} \times 3$$



Answer $I_2 = \frac{15 \sqrt{3}}{13} \text{ A}$

Step 2



$$I_3 = \frac{V_2}{R_{eq(2)}} = \frac{20}{\frac{26}{6}} = 20 \times \frac{6}{26} = \frac{60}{13}$$

$$R_{eq(2)} = R_3 + (R_1 || R_2)$$

$$= 3 + \frac{2 \times 4}{2+4}$$

$$= 3 + \frac{8}{6} = \frac{18+8}{6}$$

$$= \frac{26}{6} \Omega$$

$$I_2 = \frac{\frac{60}{13} \times 2}{2+4} = \frac{60 \times 2}{13 \times 6} = \frac{20}{13} \text{ A}$$

step (3)



$$I_2(\text{Total}) = I_2 + I_2 = \frac{15}{13} + \frac{20}{13} = \frac{35}{13} \text{ A}$$

06.07.09.2020
mukund

* Cramer's Rule \Rightarrow

\Rightarrow For a complicated circuit having more than one close loop a number of KVL equation obtained where we found a number of currents which are to be determined, so, where a number of unknown currents having a number of KVL equation to solve or find out current we use Cramer's Rule. i.e.

$$a_{11}x + b_{12}y + c_{13}z = d_1$$

$$a_{21}x + b_{22}y + c_{23}z = d_2$$

$$a_{31}x + b_{32}y + c_{33}z = d_3$$

\Rightarrow By representing in matrix form of the above equation.

we have;

$$\begin{bmatrix} a_{11} & b_{12} & c_{13} \\ a_{21} & b_{22} & c_{23} \\ a_{31} & b_{32} & c_{33} \end{bmatrix} = \begin{bmatrix} x \\ y \\ z \end{bmatrix} \cdot \begin{bmatrix} d_1 \\ d_2 \\ d_3 \end{bmatrix}$$

⇒ For solving above matrix in chamber rule we have to find out Δ , Δ_1 , Δ_2 & Δ_3 , where;

$$\Rightarrow \Delta = \begin{vmatrix} a_{11} & b_{12} & c_{13} \\ a_{21} & b_{22} & c_{23} \\ a_{31} & b_{32} & c_{33} \end{vmatrix}$$

$$\Rightarrow \Delta_1 = \begin{vmatrix} d_1 & b_{12} & c_{13} \\ d_2 & b_{22} & c_{23} \\ d_3 & b_{32} & c_{33} \end{vmatrix}$$

$$\Rightarrow \Delta_2 = \begin{vmatrix} a_{11} & d_1 & c_{13} \\ a_{21} & d_2 & c_{23} \\ a_{31} & d_3 & c_{33} \end{vmatrix}$$

$$\Rightarrow \Delta_3 = \begin{vmatrix} a_{11} & b_{12} & d_1 \\ a_{21} & b_{22} & d_2 \\ a_{31} & b_{32} & d_3 \end{vmatrix} \quad \text{Here}$$

$$x = \frac{\Delta_1}{\Delta}$$

$$y = \frac{\Delta_2}{\Delta}$$

$$z = \frac{\Delta_3}{\Delta}$$

Q#10

$$3x + 2y + 7z = 4 \rightarrow \textcircled{1}$$

$$4x + 3y + 2z = 5 \rightarrow \textcircled{2}$$

$$3x + 5y + 3z = 7 \rightarrow \textcircled{3}$$

Ans

$$\Delta = \begin{vmatrix} 3 & 2 & 7 \\ 4 & 3 & 2 \\ 3 & 5 & 3 \end{vmatrix} = 3(9-10) - 2(12-6) + 7(20-9)$$

$$= -3 - 12 + 77$$

$$= 62$$

$$\Delta_1 = \begin{vmatrix} 4 & 2 & 7 \\ 5 & 3 & 2 \\ 7 & 5 & 3 \end{vmatrix} = 4(9-10) - 2(15-14) + 7(25-21)$$

$$= -4 - 2 + 28 = 22$$

$$\Delta_2 = \begin{vmatrix} 3 & 4 & 7 \\ 4 & 5 & 2 \\ 3 & 7 & 3 \end{vmatrix} = 3(15-14) - 4(12-6) + 7(28-15)$$

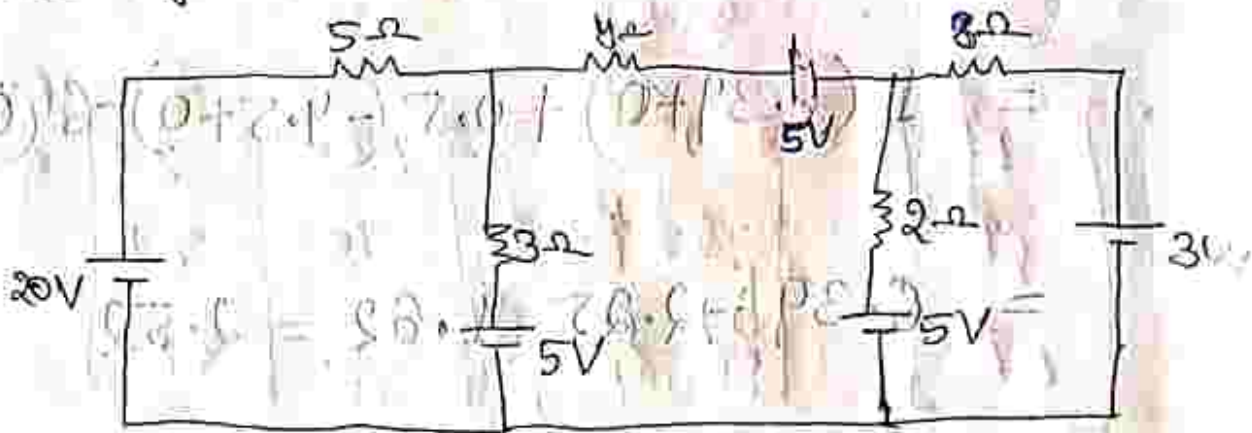
$$= 3 - 24 + 91 = 70$$

Date: 19.09.2020

mesh analysis

Q. 1

Determine the current supplied by each battery in the circuit.



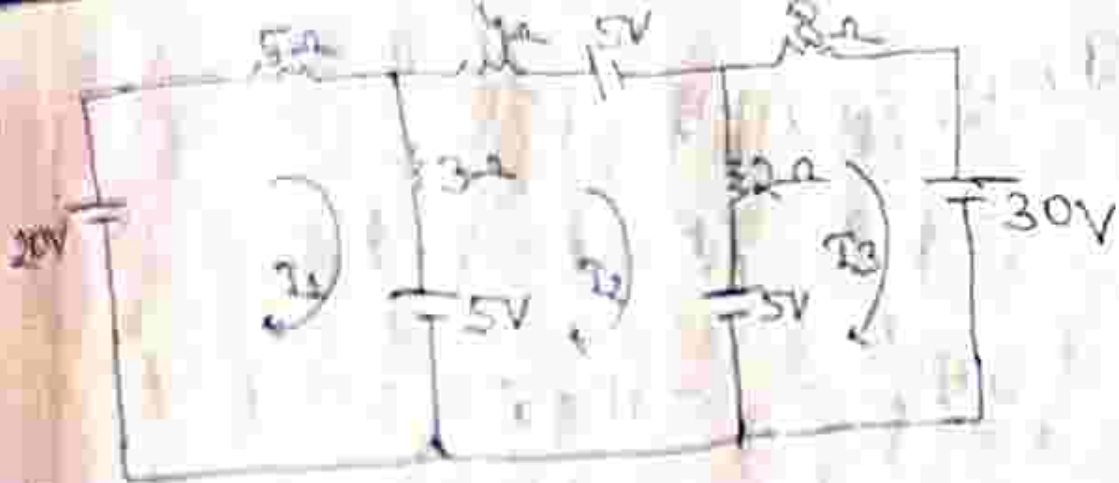
Soln.

In mesh analysis method we have use of Ohm's law.

$$V = IR$$

$$\text{or, } [V] = [I][R]$$

$$\begin{bmatrix} V_1 \\ V_2 \\ V_3 \end{bmatrix} = \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} \begin{bmatrix} R_{11} & R_{12} & R_{13} \\ R_{21} & R_{22} & R_{23} \\ R_{31} & R_{32} & R_{33} \end{bmatrix}$$



Resistance matrix

Self resistance

$$R_{11} = 5 + 3 = 8 \Omega$$

$$R_{22} = 4 + 2 + 3 = 9 \Omega$$

$$R_{33} = 2 + 2 = 4 \Omega$$

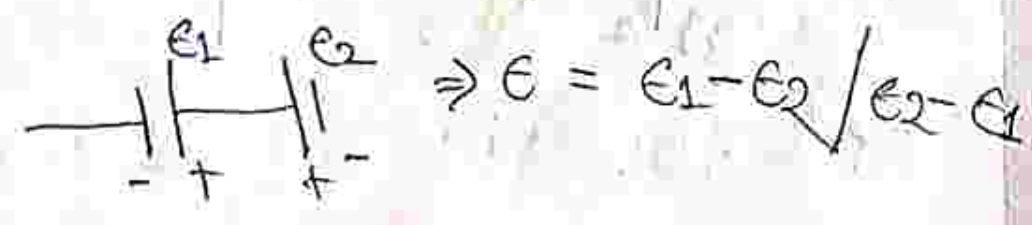
Mutual resistance

$$R_{12} = R_{21} = -3 \Omega$$

$$R_{13} = R_{31} = 0$$

$$R_{23} = R_{32} = -2 \Omega$$

Emf matrix



$$80) \quad E_1 = 20 - 5 = 15V$$

$$E_2 = 5 + 5 + 5 = 15V$$

$$E_3 = -30 - 5 = -35V$$

80)

$$\begin{bmatrix} 15 \\ 15 \\ -35 \end{bmatrix} = \begin{bmatrix} 8 & -3 & 0 \\ -3 & 9 & -2 \\ 0 & -2 & 10 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix}$$

$$\Delta = \begin{vmatrix} 8 & -3 & 0 \\ -3 & 9 & -2 \\ 0 & -2 & 10 \end{vmatrix} = 598$$

$$\Delta_1 = \begin{vmatrix} 15 & -3 & 0 \\ 15 & 9 & -2 \\ -35 & -2 & 10 \end{vmatrix} = 1530$$

$$\Delta_2 = \begin{vmatrix} 8 & 15 & 0 \\ -3 & 15 & -2 \\ 0 & -35 & 10 \end{vmatrix} = 1090$$

$$\Delta_3 = \begin{vmatrix} 8 & -3 & 15 \\ -3 & 9 & 15 \\ 0 & -2 & -35 \end{vmatrix} = -1875$$

$$I_1 = \frac{\Delta_1}{\Delta} = \frac{1530}{598} = 2.55 \text{ A}$$

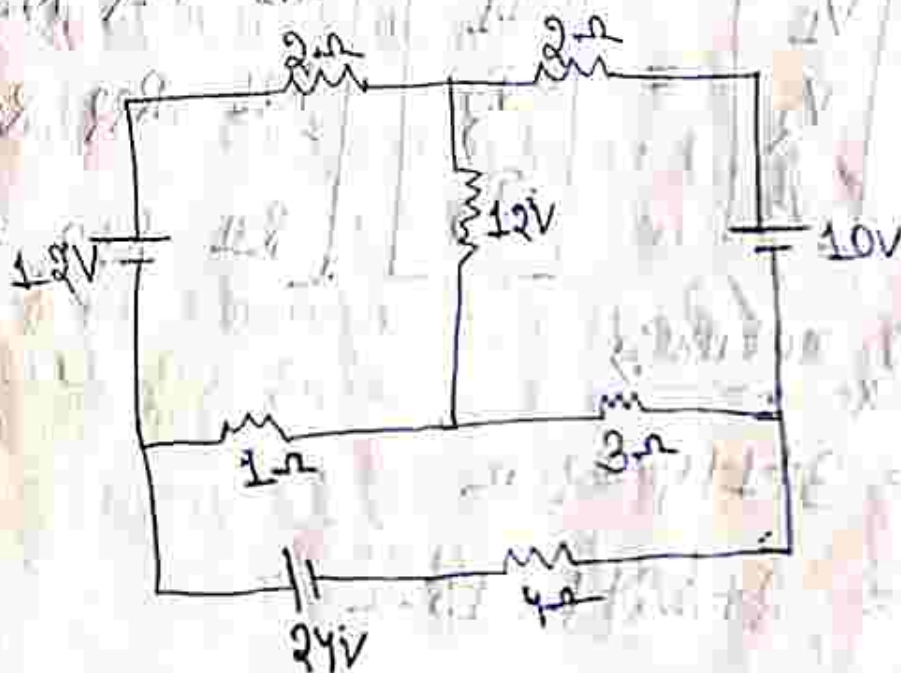
$$I_2 = \frac{\Delta_2}{\Delta} = \frac{1090}{598} = 1.82 \text{ A}$$

$$I_3 = \frac{\Delta_3}{\Delta} = \frac{-1875}{598} = -3.13 \text{ A (i.e. direction is observed)}$$

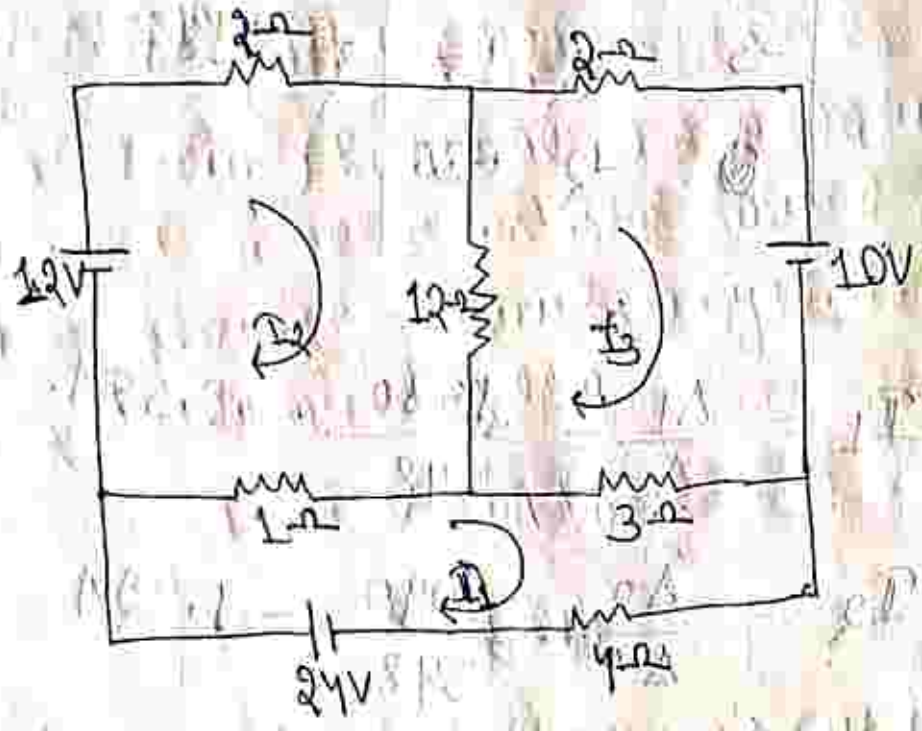
Q#10

Date: 21.09.2020

⇒ Determined the current in the 4-Ω branch in the circuit.



Soln.



⇒ According to Ohm's Law,

$$V = IR$$

$$\Rightarrow [V] = [I][R]$$

$$\Rightarrow \begin{bmatrix} V_1 \\ V_2 \\ V_3 \end{bmatrix} = \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} \begin{bmatrix} R_{11} & R_{12} & R_{13} \\ R_{21} & R_{22} & R_{23} \\ R_{31} & R_{32} & R_{33} \end{bmatrix}$$

⇒ Resistance matrix ⇒

$$R_{11} = 3 + 1 + 4 = 8 \Omega$$

$$R_{22} = 2 + 12 + 1 = 15 \Omega$$

$$R_{33} = 2 + 3 + 12 = 17 \Omega$$

$$R_{12} = R_{21} = -1, R_{13} = R_{31} = -3, R_{23} = R_{32} = -1$$

Voltage matrix \Rightarrow

$$V_1 = 24V, V_2 = 12V, V_3 = -10V$$

so;

$$\begin{bmatrix} 24 \\ 12 \\ -10 \end{bmatrix} = \begin{bmatrix} 8 & -1 & -3 \\ -1 & 15 & -12 \\ -3 & -12 & 17 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix}$$

$$\Delta = \begin{vmatrix} 8 & -1 & -3 \\ -1 & 15 & -12 \\ -3 & -12 & 17 \end{vmatrix} = 8(255 - 144) + 1(17 - 36) - 3(12 + 45) = 664$$

$$\Delta I_1 = \begin{vmatrix} 24 & -1 & -3 \\ 12 & 15 & -12 \\ -10 & -12 & 17 \end{vmatrix} = 24(255 - 144) - 12(17 - 36) - 10(12 + 45) = 2730$$

\Rightarrow I_1 current is flowing through 4Ω so;

$$I_1 = \frac{\Delta I_1}{\Delta} = \frac{2730}{664} = 4.1A$$

DE: 24.09.2020

* THEVENIN'S THEOREM

⇒ In a linear, bilateral, active network containing more than one source, the current flowing through any load resistor R_L is determined by the

$$I_L = \frac{V_{TH} \text{ or } V_{OC}}{R_L + R_{TH}}$$

⇒ which determine from Thevenin's equivalent circuit after thevenize the given circuit.

where; V_{TH} / V_{OC} = Thevenin's equivalent voltage across the load resistance after thevenizing the load resistance after removing the load resistor.

R_L = Load resistance across which current is to find out.

R_{TH} = Thevenin's equivalent resistance or total external resistance of the circuit.

I_L = Load current.

Steps for Thevenize the circuit

Step-1) \Rightarrow we have to find out current across

given R_L .

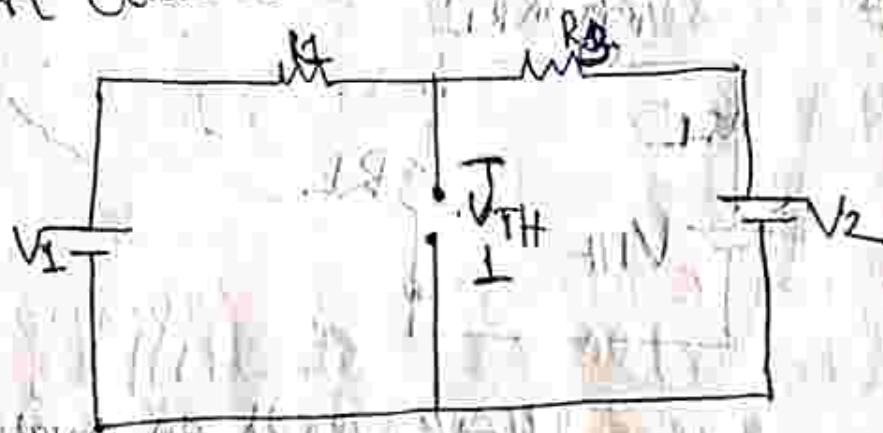
So, the load resistance R_L across which current is to be found out.



In the given circuit we have to find out current across R_L . $\therefore R_L = R_2$.

Step-2) (V_{OC} or V_{TH})

\Rightarrow Removing the load resistance R_L from the circuit, now the voltage appear across open circuit terminal is V_{OC} or V_{TH} .

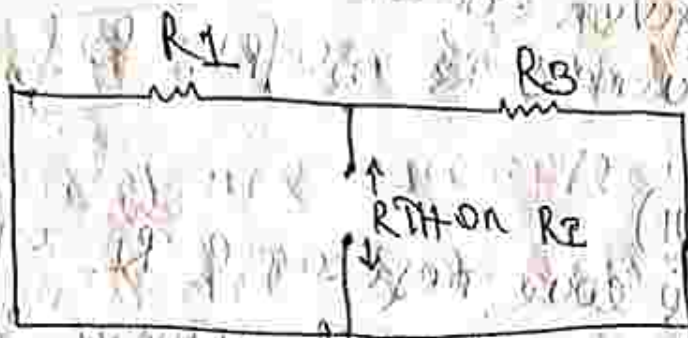


\Rightarrow Here, V_{TH} or V_{OC} is found out by applying KVL or voltage division rule.

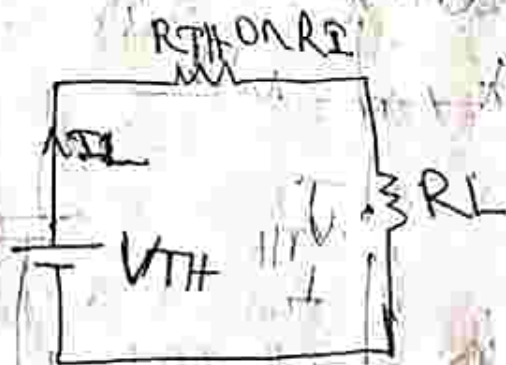
Step (3) (RTH OR RT)

→ For finding out value of R_{TH} or R_T , all the sources are removed i.e. the voltage sources are short circuited and current sources are open circuited, R_L terminal is open and we have to find out R_{across} open circuit terminal to find out R_{TH} .

$$R_{TH} = R_1 \parallel R_2$$



Step (4)



THEVENIN'S EQUIVALENT CIRCUIT

$$I_L = \frac{V_{TH} \text{ OR } V_{OC}}{R_{TH} + R_L}$$

* Norton's Theorem :

⇒ In a linear, bilateral, active network containing more than one source, the current through any resistance R_L is found out by applying the relation:

$$I_L = \frac{I_N R_N}{R_N + R_L}$$

where: I_L = Load current which is to be found out.

R_N = Norton's equivalent resistance on total external resistances.

R_L = Load resistance across which current is to be found out.

I_N = Norton's equivalent current on Norton's circuit current flowing through load resistance R_L when R_L replaced by ordinary conductor having negligible resistance.

* Steps for Nortonizing a circuit :

Step (1) ⇒ We have to find out first the load resistance R_L across which current is to be found out.

So, the load resistance R_L is the resistance across which the current is to be found out.

⇒

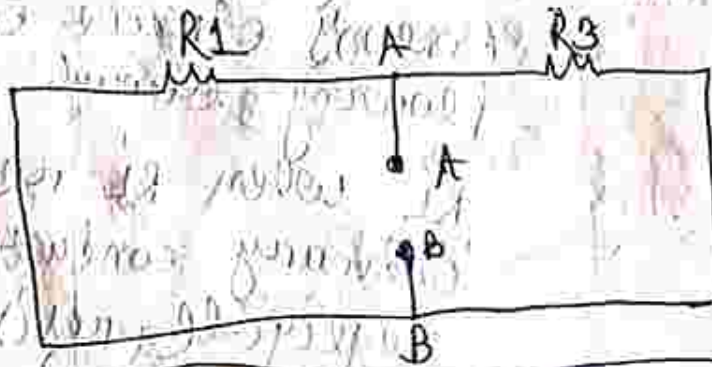


⇒ In the above circuit we have to find out current across R_2 so load resistance

$$R_L = R_2$$

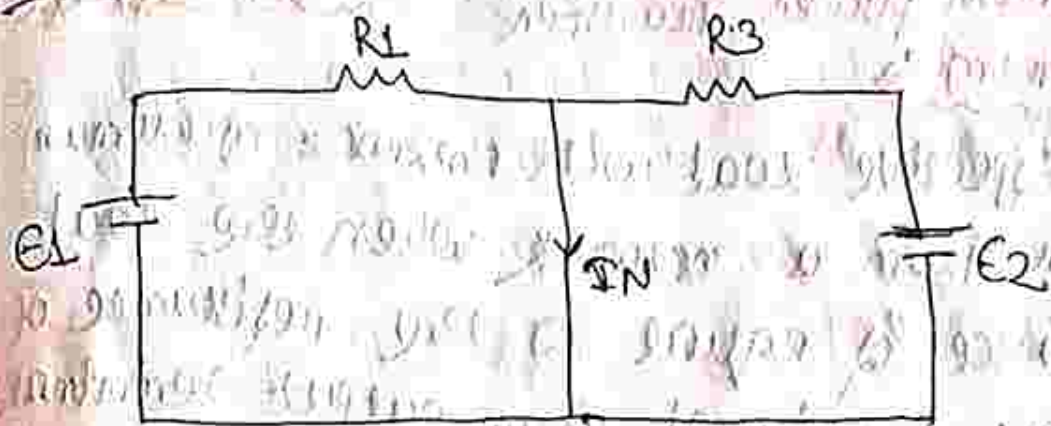
STEP → ① (step for R_N OR R_P)

⇒ For finding out the value of R_N all the sources are removed i.e. the voltage sources are short circuited and current sources are open circuited.



$$\text{So, } R_N \text{ OR } R_P = R_1 \parallel R_3$$

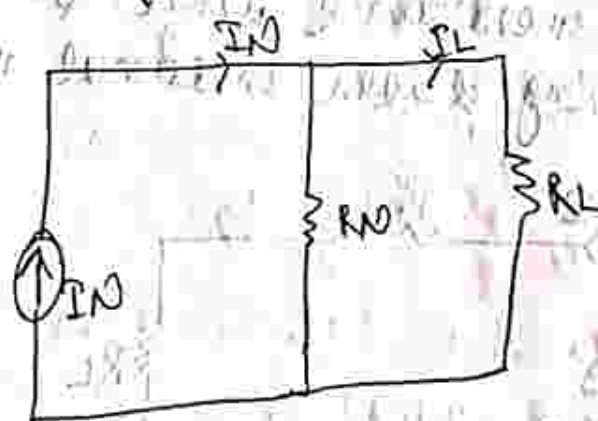
Step (3) (Step for I_N)



⇒ So, the above circuit I_N can be found out by applying KCL or current division rule.

Step (4) (Step for Norton's equivalent ckt)

⇒ After finding out I_N , R_N & R_L on design the Norton's equivalent circuit.



So applying current division rule,

$$I_L = \frac{I_N \times R_N}{R_N + R_L}$$

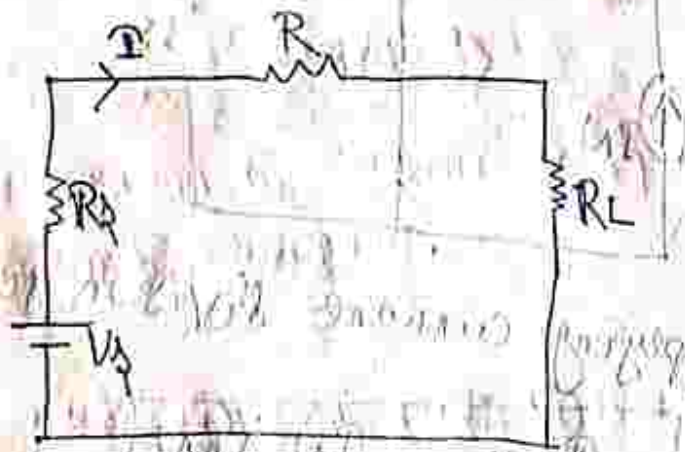
* Maximum power transfer

DE: 03.10.2011
mix mix mix

Theorem \Rightarrow

\Rightarrow A respective load will observe maximum power from a network when the load resistance is equal to the resistance of a network is viewed from output terminals of load resistance; all energy source are removed behind their internal resistance.

\Rightarrow It means that maximum power transfer for source to load if R_L is equal to R_T , where R_T is the internal resistance of the circuit viewed across open circuit terminal of the load resistance while source are ignore leaving their internal resistance.



\Rightarrow In the circuit, V_s is equal to the generation voltage or source voltage.

R_s = source internal source

R = Resistance seen across the circuit

R_L = Load Resistance \Rightarrow

$$\text{So } \boxed{R_T = R + R_s}$$

where; R_T = Total Internal Resistance of the circuit.

So; in the circuit current flow is given

$$\text{by } \boxed{I = \frac{V_s}{R_T + R_L}}$$

Power transfer to the load.

$$\boxed{P = I^2 R_L}$$

$$\Rightarrow P = \left(\frac{V_s}{R_T + R_L} \right)^2 R_L$$

So; maximum power will be transfer if;

$$\frac{dP}{dR_L} = 0 \quad (R_L \rightarrow 0, P \rightarrow 0)$$

$$\Rightarrow \frac{d}{dR_L} \left(\frac{V_s^2 R_L}{(R_T + R_L)^2} \right) = 0$$

$$\Rightarrow \frac{d}{dR_L} (V_s^2 R_L) (R_T + R_L)^{-2} = \frac{d}{dR_L} (R_T + R_L)^{-2} \times V_s^2 R_L$$

$$\left(\because \frac{d}{dt} \left(\frac{a}{b} \right) = \frac{\frac{d}{dt} a \times b - \frac{d}{dt} b \times a}{b^2} \right)$$

$$\Rightarrow V_s^2 (R_I + R_L)^2 - 2(R_I + R_L) \times V_s^2 R_L = 0$$

$$\Rightarrow \cancel{V_s^2} (R_I + R_L)^2 = 2(R_I + R_L) \times \cancel{V_s^2} R_L$$

$$\Rightarrow \frac{(R_I + R_L)^2}{R_I + R_L} = 2R_L$$

$$\Rightarrow R_I + R_L = 2R_L$$

$$\Rightarrow R_I = 2R_L - R_L$$

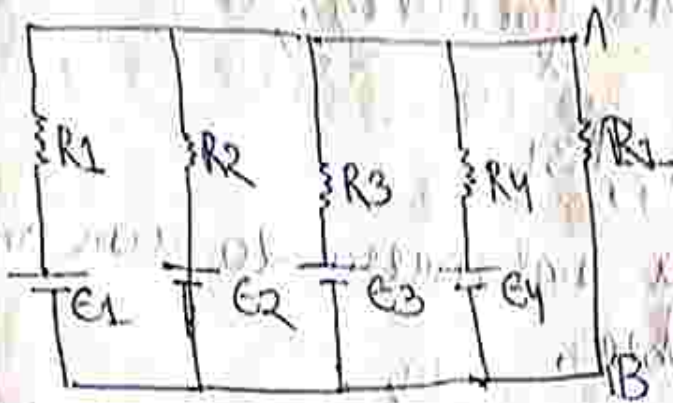
\Rightarrow $R_I = R_L$ This is the condition for maximum power transfer in a network.

i.e. when load resistance is equal to the total external resistance of the circuit.

* **Millman's Theorem** \Rightarrow

\Rightarrow This theorem is combination of both Thevenin and Norton's theorem.

\Rightarrow It is used to find out voltage across any network containing a number of parallel voltage sources series with resistance.

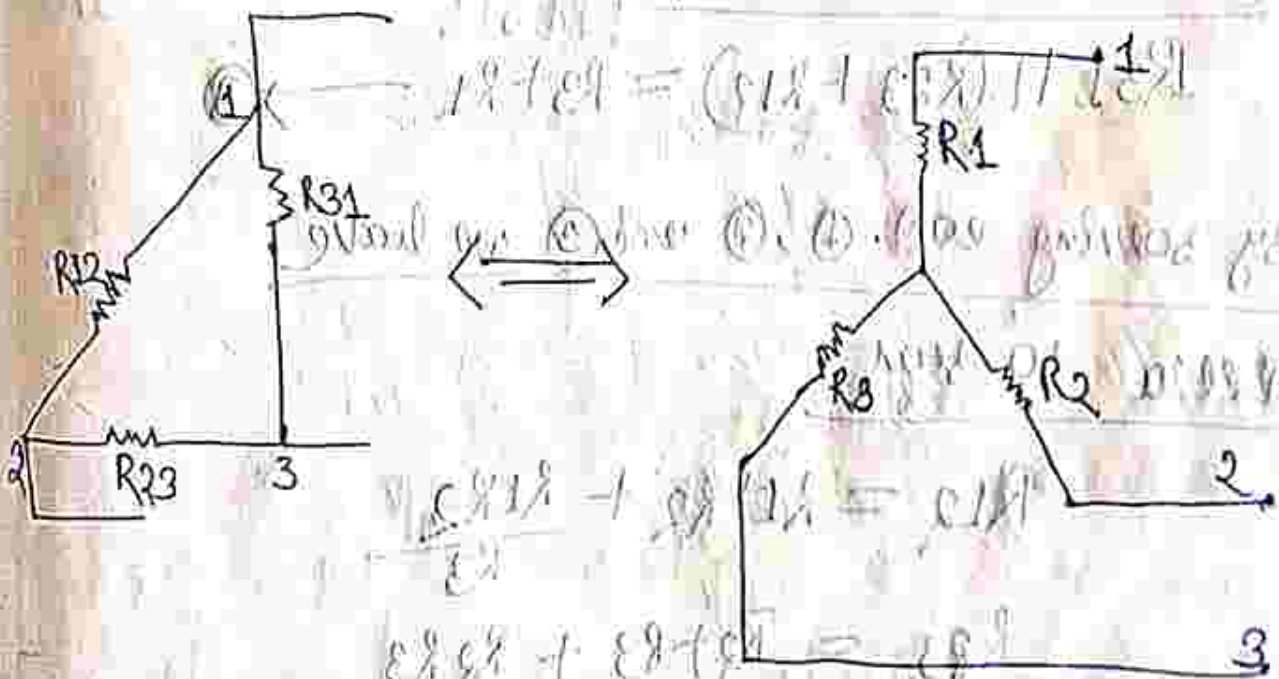


$$\Rightarrow V_{AB} = \frac{E_1}{R_1} + \frac{E_2}{R_2} + \frac{E_3}{R_3} + \dots + \frac{E_n}{R_n}$$

$$\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots + \frac{1}{R_n}$$

$$\Rightarrow V_{AB} = \frac{I_1 + I_2 + I_3 + \dots + I_n}{G_1 + G_2 + G_3 + \dots + G_n}$$

Star to Delta and Delta to Star connection



* Star to Delta connection \Rightarrow

$$R_1 = R_{12} \times R_{31}$$

\Rightarrow Star to Delta and Delta to star connections are convertible.

Resistance in between 1 & 2 \Rightarrow

In Delta

$$R_{12} \parallel (R_{31} + R_{23}) = R_1 + R_2 \rightarrow \textcircled{1}$$

Resistance betⁿ. 2 & 3

$$\textcircled{2} R_{23} \parallel (R_{12} + R_{31}) = R_2 + R_3 \rightarrow \textcircled{2}$$

Resistance betⁿ. 3 & 4

$$R_{31} \parallel (R_{23} + R_{12}) = R_3 + R_1 \rightarrow \textcircled{3}$$

* By solving eqn. $\textcircled{1}$, $\textcircled{2}$ and $\textcircled{3}$ we have:

Delta to star

$$R_{12} = R_1 + R_2 + \frac{R_1 R_2}{R_3}$$

$$R_{23} = R_2 + R_3 + \frac{R_2 R_3}{R_1}$$

$$R_{31} = R_3 + R_1 + \frac{R_3 R_1}{R_2}$$

Plan to Delta connection

$$R_1 = \frac{R_{23} \times R_{31}}{R_{12} + R_{23} + R_{31}}$$

$$R_2 = \frac{R_{12} \times R_{23}}{R_{12} + R_{23} + R_{31}}$$

$$R_3 = \frac{R_{31} \times R_{23}}{R_{12} + R_{23} + R_{31}}$$

* Reciprocity Theorem

In a linear, bilateral network of a source E for any branch produces a current I in other branch, then the same source emf E acting in the second branch produces the same current I in the first branch.

Ex: Check the reciprocity of the following network.



Soln.

Let the current flowing in the Ammeter be I A.

Step-1 We have to find out current in
Ammeter (A) due to presence of 36V source
in 1st branch.

$$\text{So } I_1 = \frac{V}{R_{eq}}$$

$$R_{eq} = \{(3+1) \parallel 12\} + 4+2$$

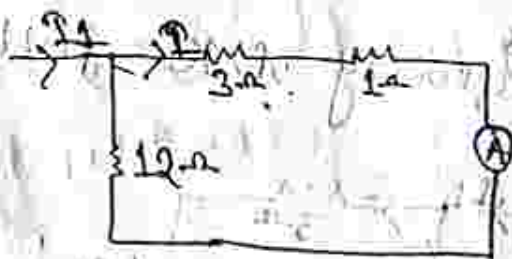
$$= 9\Omega$$

$$I_1 = \frac{36}{9} = 4A$$

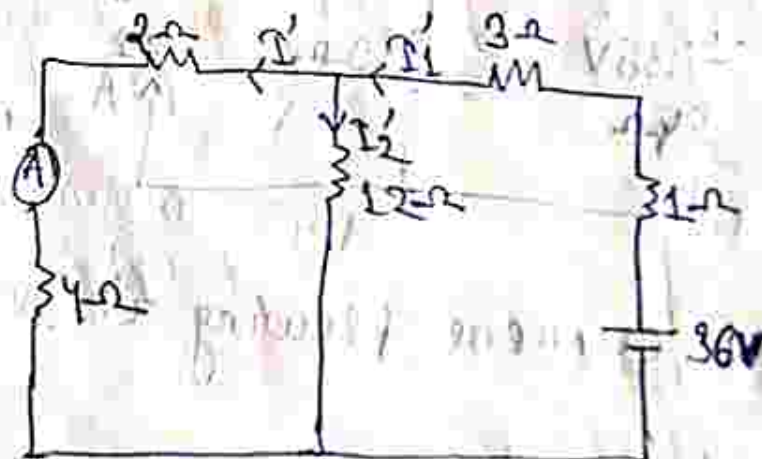
Now applying current division rule.

$$\Rightarrow I = \frac{I_1 \times 12}{12+3+1}$$

$$= \frac{4 \times 12}{12+3+1} = \frac{48}{16} = 3 \text{ Amp.}$$



Step-2



So; we first find out I_1 & then I_2

$$I_1 = \frac{V}{R_{eq}}$$

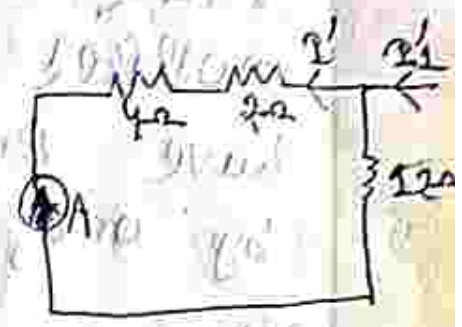
$$R_{eq} = \{(4+2) \parallel 12\} + 3+1 = 8 \Omega$$

$$I_1 = \frac{36}{8} = 4.5A$$

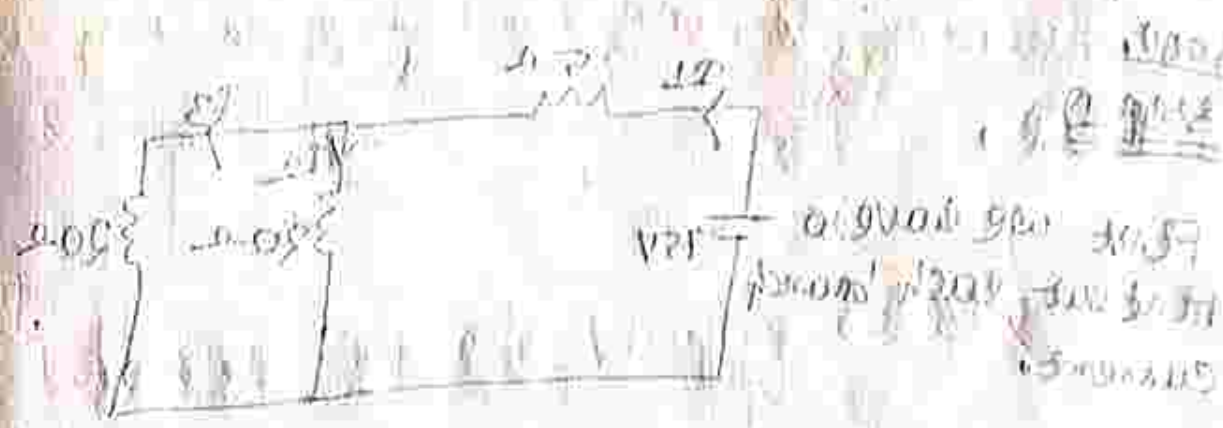
Now applying current division rule

$$I_2 = \frac{I_1 \times 12}{12+2+4}$$

$$= \frac{4.5 \times 12}{12+2+4} = 3A$$



→ Hence it is proof that the source present both branch produced equal current respective opposite branch.

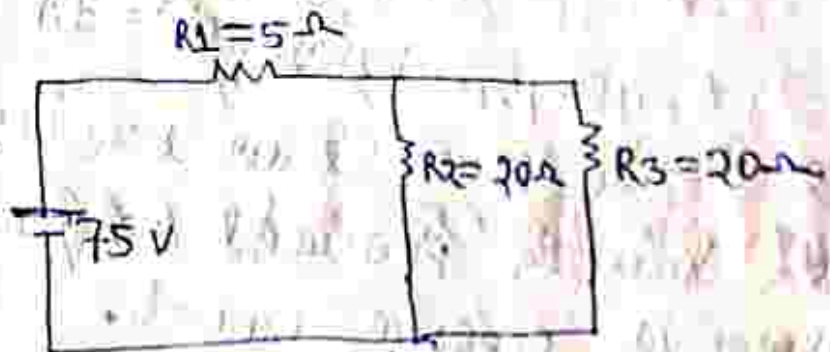


* Compensation Theorem :

→ If the resistance of any branch of a network is changed from R to $R \pm \Delta R$ when the current originally flowing is I , the change of current at any other place in the network may be calculated by assuming that an emf of $I \Delta R$ have been injected into the modified branch while all other sources have their emf ignore and are replaced by only their internal resistance.

Exp :

Q. 10

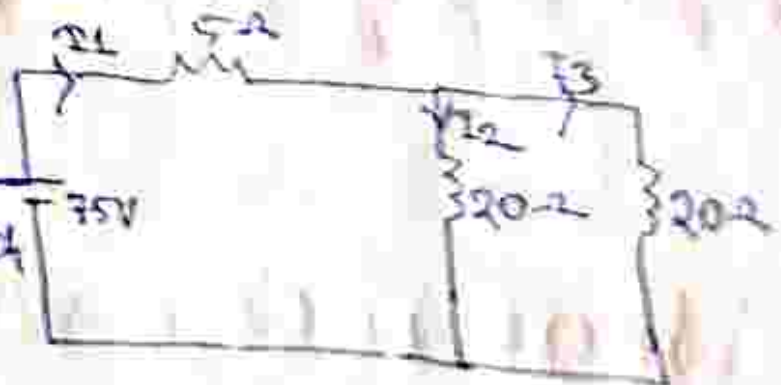


In the circuit if R_3 increase by 30% then find out current change in another branch.

Soln.

Step 1

First we have to find out each branch current.



$$R_{eq} = (20 \parallel 20) + 5$$

$$R_{eq} = \frac{20 \times 20}{20 + 20} + 5 = \frac{400}{40} + 5$$

$$R_{eq} = \frac{40}{4} + 5 = \frac{40 + 20}{4} = \frac{60}{4} = 15 \Omega$$

$$I_1 = \frac{V}{R_{eq}} = \frac{75}{15} = 5A \text{ (Left } \rightarrow \text{ Right)}$$

$$I_2 = \frac{I_1 \times R_3}{R_2 + R_3} = \frac{5A \times 20}{20 + 20} = 2.5A \text{ (U } \rightarrow \text{ D)}$$

$$I_3 = I_1 - I_2 = 5A - 2.5A = 2.5A \text{ (U } \rightarrow \text{ D)}$$

Step 2 \Rightarrow The resistance R_3 increase by 30% \therefore

$$\Delta R_3 = R_3 \times 30\% = 20 \times \frac{30}{100} = 6 \Omega \text{ Hence}$$

emf source inserted in the modified branch

$$-I_3 R_3 = -2.5 \times 6 = -15V$$

$$R_3' = R_3 + \Delta R_3 = 20 + 6 = 26 \Omega$$



$$\Rightarrow \Delta I_3 = \frac{I_3 \times \Delta R_3}{R_{eq}'} \quad \& \quad R_{eq}' = \left\{ (5 \parallel 20) + 26 \right\}$$

$$= \frac{5 \times 20}{5 + 20} + 26 = 30 \Omega$$

$$\therefore \Delta I_3 = \frac{2.5 \times 6}{30} = 0.5A \text{ (D } \rightarrow \text{ U)}$$

Now applying current division Rule;

$$\Delta I_1 = \frac{0.5 \times 20}{20+5} = 0.4 \text{ A (R} \rightarrow \text{L)}$$

$$\Delta I_2 = 0.5 - 0.4 = 0.1 \text{ A (U} \rightarrow \text{D)}$$

Step \rightarrow ③



Thus, $I_{1N} = I_1$ (current new)
 $(\Delta I_1 = I_1, \Delta I_2 = I_2, \Delta I_3 = I_3)$

$$I_{1N} = I_1 - \Delta I_1 = 5 - 0.4 = 4.6 \text{ A (L} \rightarrow \text{R)}$$

$$I_{2N} = I_2 + \Delta I_2 = 2.5 + 0.1 = 2.6 \text{ A (U} \rightarrow \text{D)}$$

$$I_{3N} = I_3 - \Delta I_3 = 2.5 - 0.5 = 2 \text{ A (U} \rightarrow \text{D)}$$

Note \rightarrow If resistances increase the emf injected value is $-I \Delta R$ whereas if the resistances decrease the injected emf is

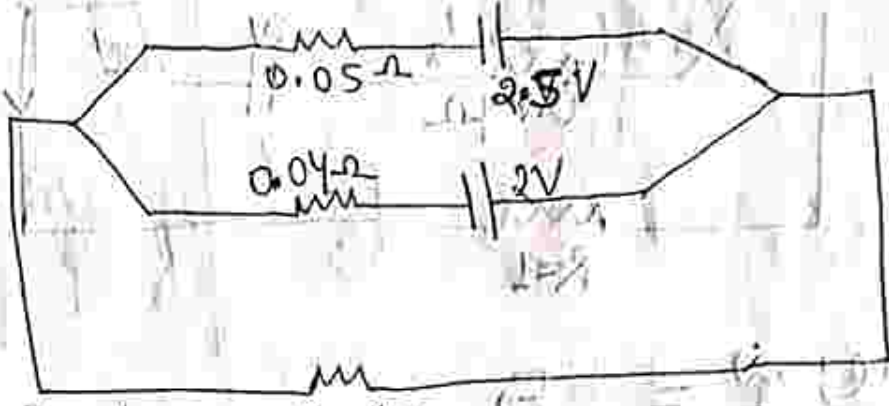
$$+I \Delta R = \frac{E \Delta R}{R + \Delta R} = E \Delta R$$

$$(U = 0) \text{ A} = 0$$

02/15/10/2020
 maximum

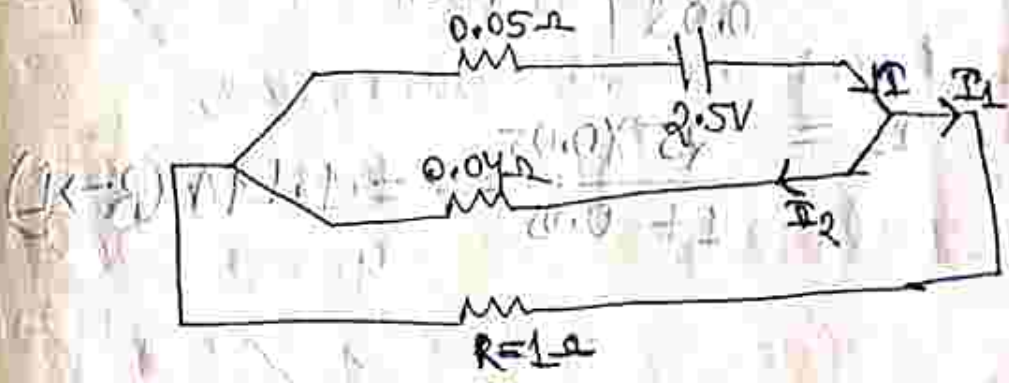
Q.70
 Imp

By using superposition theorem, find out current in the resistance R.



Soln: $R = 1\Omega$

Step-1 Taking 2.5V source at that time 2V source ignore



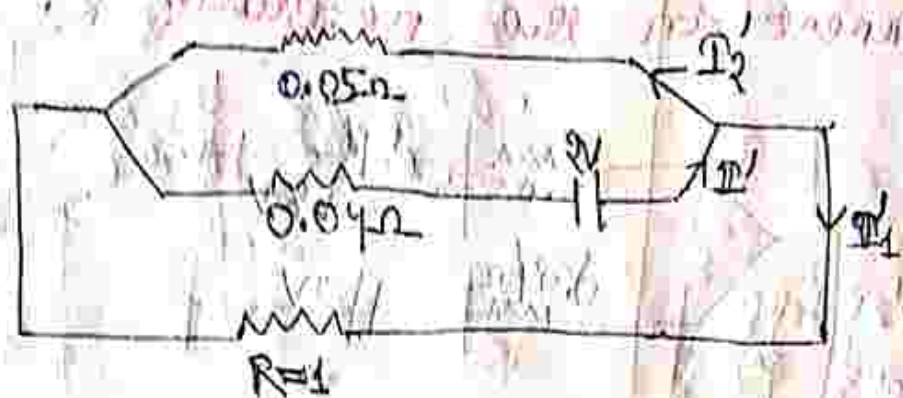
Here, $I = \frac{E_1}{R_{eq}}$ and $R_{eq} = (1 || 0.04) + 0.05 = 0.08\Omega$

So, $I = \frac{2.5}{0.08} = 31.25A$

Now, $I_1 = \frac{31.25 \times 0.04}{1 + 0.04}$ (By using current division rule)

$= \frac{31.25 \times 0.04}{1.04} = 1.20A (R \rightarrow L)$

~~Step-2~~ Considering 2V source at each time of 2V source is ignored.

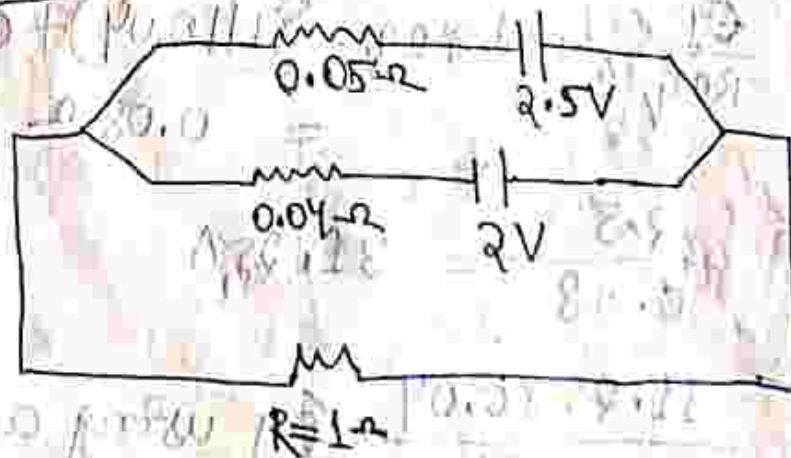


Here, $I' = \frac{E_2}{R_{eq}}$ and $R_{eq} = (0.05 \parallel 1) + 1$
 $= 0.08 \Omega$

$$I' = \frac{2}{0.08} = 25A$$

Here, $I_1 = \frac{25 \times 0.05}{1 + 0.05} = 1.19A (R \rightarrow L)$

Step-3



Here, $I_{1T} = I_1 + I_2$
 $= 1.20 + 1.19$
 $= 2.39A (R \rightarrow L)$

Q.3 Find out current across 4Ω resistor by using Thevenin's Theorem.



Soln.

Step-1

For R_L \Rightarrow Here current is to be found out across 4Ω , so $R_L = 4\Omega$

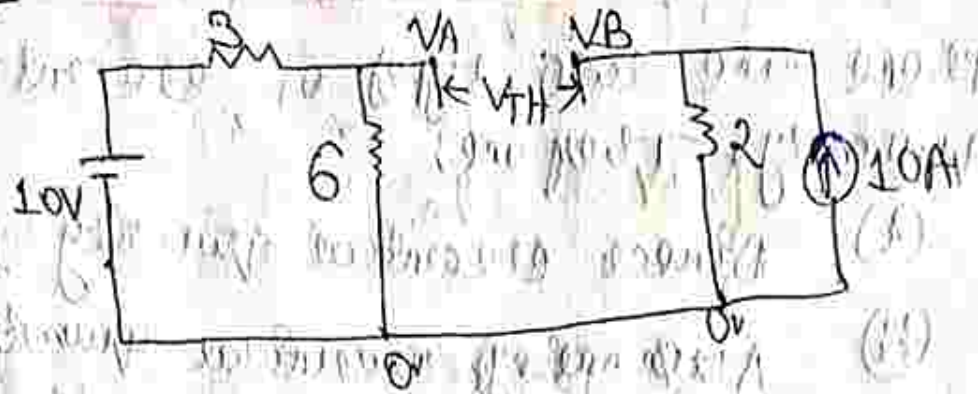
Step-2

For R_{TH} \Rightarrow The voltage source is short circuited whereas the current source is open circuited and the resistance view from open terminals across R_L .



$$\begin{aligned} \text{Now } R_{TH} \text{ or } R_{TE} &= (3/6) + 2 \\ &= 4\Omega \end{aligned}$$

Step-3



So) Here $V_{TH} = V_A - V_B$

So, here; $V_B = 10 \times 2$
 $(V = IR) = 20V$



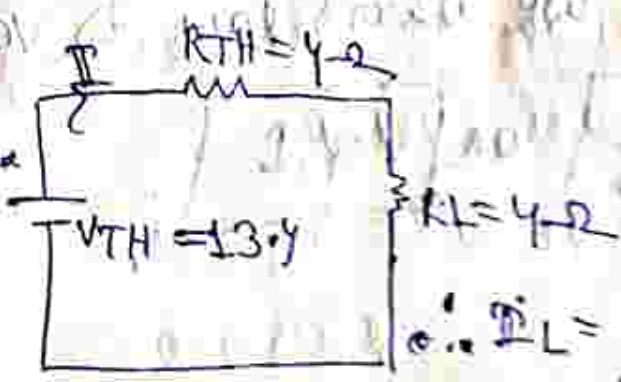
According to voltage division rule

$$V_A = \frac{10 \times 6}{3+6} = 6.6V \text{ (with respect to } 0V)$$

So; $V_{TH} = V_B - V_A = 20 - 6.6 = 13.4V$

Step 4

(Thevenin equivalent circuit)



$$\therefore I_L = \frac{V_{TH}}{R_L + R_{TH}} = \frac{13.4V}{4+4} = \frac{13.4}{8} = 1.675A$$

⇒ There are two types of electrical quantity. They are:

- (i) Direct electrical quantity
- (ii) Alternating electrical quantity

(i) Direct electrical quantity

⇒ The direct electrical quantity are those whose magnitude and direction does not change with respect to time.

⇒ In an d.c. electrical quantity voltage and current always same at every instant of time.

⇒ There is no frequency as the value is constant.

⇒ There are no inductance and capacitance phenomenon but there is resistance phenomenon.

⇒ So in this use ohm's law is valid to.

$I = \frac{V}{R}$

or $V \propto I$

$\frac{110V}{110\Omega} = \frac{11V}{11\Omega} = 1A$



Alternating Electrical quantity \Rightarrow

\Rightarrow The alternating electrical quantity are those whose magnitude and direction get change with respect to time.

\Rightarrow In an electrical quantity, are ~~valued~~ ^{Varies} according to the sinusoidal functions.

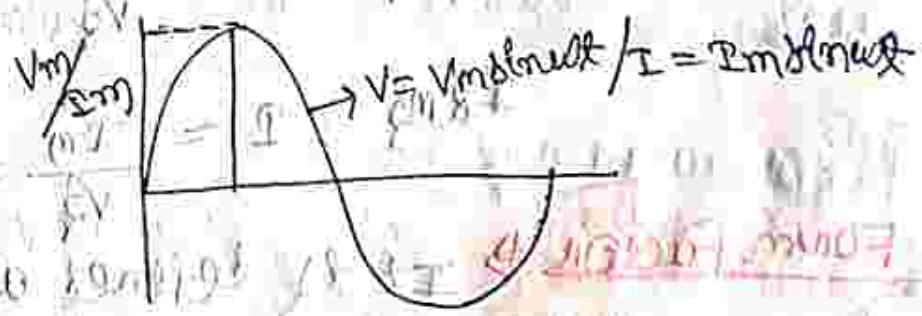
Instantaneous $V = V_m \sin \omega t$ or $E = E_m \sin \omega t$.

$I = I_m \sin \omega t$, where V_m , I_m and E_m are maximum value of a.c. electrical quantity.

V , I and E are instantaneous of A.C. electrical quantity.

\Rightarrow This is a frequency associated with A.C. electrical quantity.

\Rightarrow The wave form of AC electrical quantity are:



Average value \Rightarrow The average value of a.c. electrical quantities are those which when flowing through a given circuit transfer some charge.

of that of D.C. \Rightarrow

So, $I_{av} = \frac{2 I_m}{\pi} = 0.637 I_m$

$V_{av} = \frac{2 V_m}{\pi} = 0.637 V_m$

$E_{av} = \frac{2 E_m}{\pi} = 0.637 E_m$

* RMS Value (Root mean square value)

⇒ RMS value of A.C. is that value of D.C. which when flowing through a given circuit, for a given time produce same heat as that of D.C.

$V_{RMS} = V = \frac{V_m}{\sqrt{2}} = 0.707 V_m$

$E_{RMS} = E = \frac{E_m}{\sqrt{2}} = 0.707 E_m$

$I_{RMS} = I = \frac{I_m}{\sqrt{2}} = 0.707 I_m$

* Form Factor ⇒ It is defined as the ratio of rms value of A.C. electrical quantity to average value.

⇒ It is denoted by K_F .

$K_F = \frac{RMS \text{ value}}{\text{Average value}} = \frac{0.707 V_m}{0.637 V_m}$

$$\Rightarrow \boxed{K_F = 1.414} \quad \underline{V_{0\text{imp}}}$$

* Peak Factor

It is defined as the ratio of maximum value of an A.C. electrical quantity to R.M.S value of ~~the~~ A.C. electrical quantity.

$$K_P / K_C = \frac{\text{maximum value}}{\text{RMS value}}$$

$$= \frac{V_m / I_m / E_m}{\dots}$$

$0.707 V_m / I_m / E_m$

$$\Rightarrow \boxed{K_P / K_C = 1.414} \quad \underline{V_{0\text{imp}}}$$

DT: 22.10.2020

* AC through pure resistance

Let the resistance R be connected across A.C. supply for $V = V_m \sin \omega t$ and current flowing is I .

According to Ohm's law we know that

$$V = IR$$

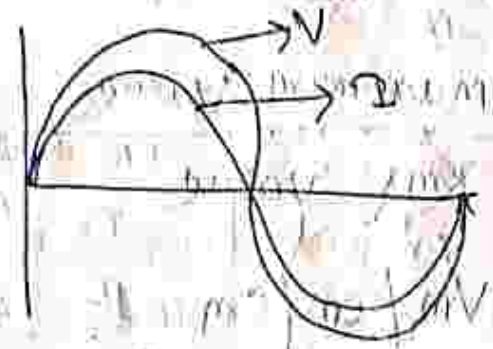
$$\Rightarrow \boxed{I = \frac{V}{R}}$$

So; putting $V = V_m \sin \omega t$

$$I = \frac{V_m \sin \omega t}{R} \Rightarrow \boxed{I = I_m \sin \omega t}$$

at $\omega t = 0$	at $\omega t = \frac{\pi}{2} = 90^\circ$	at $\omega t = 180^\circ$ or π
$V = 0$	$V = V_m$	$V = 0$
$I = 0$	$I = I_m$	$I = 0$

Wave form



⇒ Here in the pure resistance ckt. the voltage and current are vary simultaneously on both are vary at a time. ∴ voltage and current are in phase.

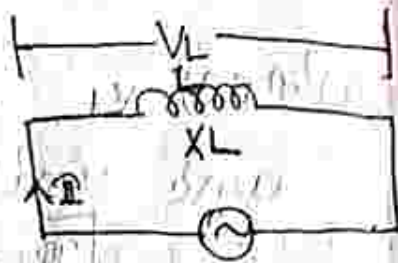
Phase Diagram



Here $\phi = 0^\circ$ ($\phi =$ angle between volt. and current)

* A.C. Through pure Inductance \Rightarrow

\Rightarrow Inductance is the property of the material which does not allow sudden change of current.



$$V = V_m \sin \omega t$$

\Rightarrow An inductance 'L' is connected across A.C. supply of $V = V_m \sin \omega t$ and the current flow is I .

\Rightarrow Let the voltage drop across the inductor is V_L .

$$\Rightarrow V_L = L \frac{dI}{dt}$$

$$\Rightarrow dI = \frac{V_L}{L} dt$$

Integrating both sides

$$\int dI = \int \frac{V_L}{L} dt$$

$$\Rightarrow I = \int \frac{V_m \sin \omega t}{L} dt$$

$$= \frac{V_m}{L} \int \sin \omega t dt$$

$$\Rightarrow I = \frac{V_m}{\omega L} \left\{ -\sin\left(\frac{\pi}{2} - \omega t\right) \right\}$$

$$\Rightarrow I = \frac{V_m}{\omega L} \sin\left(-\frac{\pi}{2} + \omega t\right)$$

($\because \sin(\theta) = -\sin(\theta)$ odd function)

$$\Rightarrow I = \frac{V_m}{X_L} \sin(\omega t - \frac{\pi}{2})$$

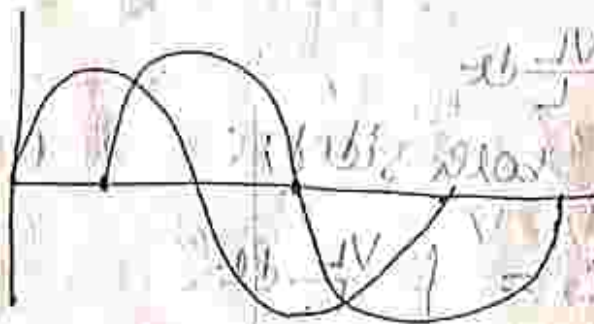
where X_L inductive reactance of the coil
and ω is rad/s

$$i = I_m \sin(\omega t - \frac{\pi}{2})$$

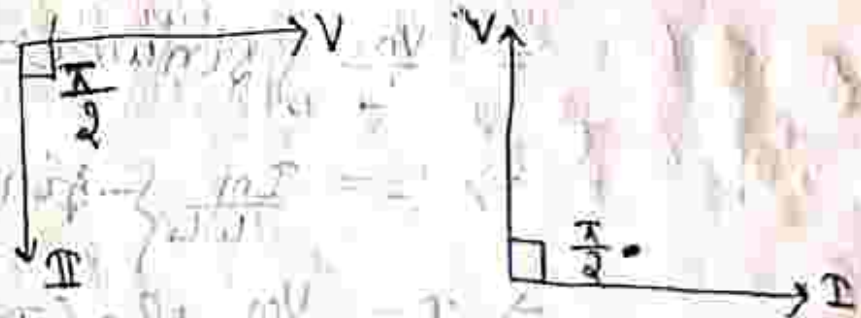
where $I_m = \frac{V_m}{X_L}$

If $\omega t = 0$	$\omega t = \frac{\pi}{2}$	$\omega t = \pi$ or 180°
$V = 0$	$V = V_m$	$V = 0$
$I = -I_m$	$I = 0$	$I = I_m$

* wave form \Rightarrow



* Phasor Diagram \Rightarrow



the $\omega t = 0$ is $(\sin 0 = 0)$
(reference)

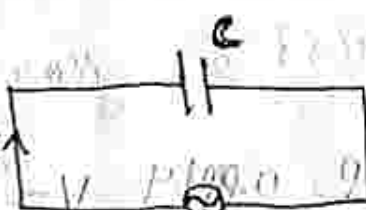
Date: 02.11.2020

A.C Through pure capacitive circuit \Rightarrow

\Rightarrow capacitance is the property of the circuit on materials which does not allow sudden change of voltage.

\Rightarrow Here the 'C' capacitor is connected across A.C. supply of $V = V_m \sin \omega t$ and the current flowing is 'I'.

\Rightarrow We know that capacitors store charge.



so charge store by capacitor

$$Q = CV$$

\Rightarrow But we again know that rate of transfer of charge is current flow.

$$\frac{dQ}{dt} = \frac{d}{dt} \{ CV \}$$

$$\Rightarrow I = C \frac{d}{dt} V = C \frac{d}{dt} \{ V_m \sin \omega t \}$$

$$\Rightarrow I = C V_m \frac{d}{dt} \sin \omega t$$

$$= C V_m \omega \cos \omega t$$

$$= \frac{V_m}{\frac{1}{\omega C}} \cos \omega t$$

$$\geq \frac{V_m}{X_C} \cos \omega t$$

$$= \frac{V_m}{X_c} \sin\left(\frac{\pi}{2} + \omega t\right) \quad (\because \sin(90^\circ + \theta) = \cos \theta)$$

X_c is known as capacitive reactance and

$$X_c = \frac{1}{\omega C} \text{ unit is } \Omega \text{ (ohm)}$$

so $I_m = \frac{V_m}{X_c}$, putting above values

$$I = I_m \sin\left(\omega t + \frac{\pi}{2}\right)$$

we apply $V = V_m \sin \omega t$ and current flow

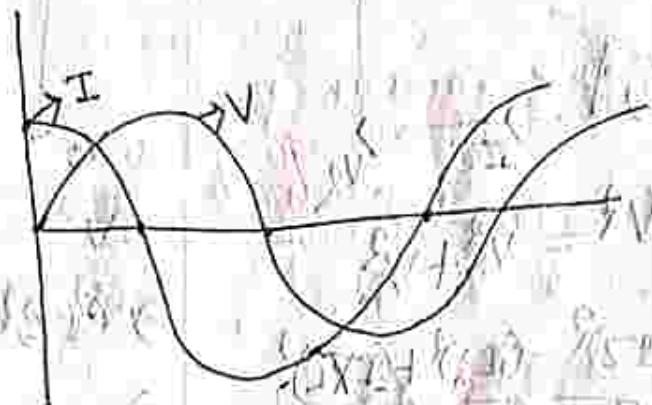
$$I = I_m \sin\left(\omega t + \frac{\pi}{2}\right)$$

<p>If $\omega t = 0$ $V = 0$ $I = I_m$</p>	<p>If $\omega t = \frac{\pi}{2} \text{ or } 90^\circ$ $V = V_m$ $I = 0$</p>	<p>If $\omega t = \pi \text{ or } 180^\circ$ $V = 0$ $I = -I_m$</p>
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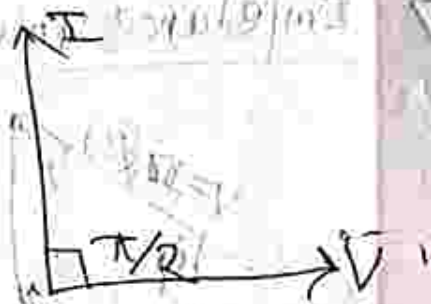
⇒ Here from eqs (1) & (2) seen that the current travels ahead of voltage by $\frac{\pi}{2}$ or current leads the voltage by $\frac{\pi}{2}$ or 90° .

$$\frac{V_m}{X_c} = \frac{V_m}{\frac{1}{\omega C}} = V_m \omega C$$

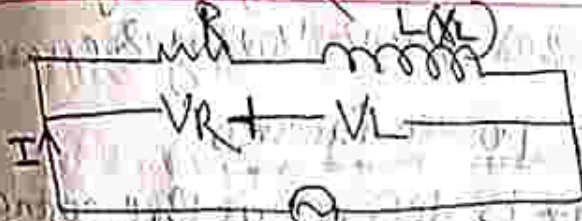
Wave form



Phasor Diagram



R-L Series Circuit



$$V = V_m \sin \omega t$$

Here, resistance R and inductance L having inductive reactance X_L are connected in series across ac supply of $V = V_m \sin \omega t$ and the current flowing is I .

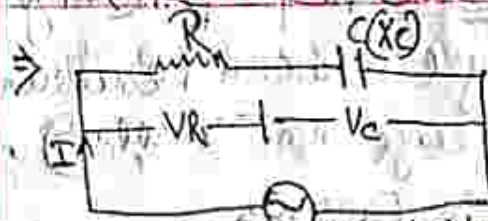
$$V_R = IR \text{ (Voltage Drop across } R)$$

$$V_L = IX_L \text{ (Voltage Drop } L)$$

$$V = IZ \text{ (Voltage Drop across } Z)$$

Z is impedance & unit of Z of R-L series ckt

R-C Series Circuit



$$V = V_m \sin \omega t$$

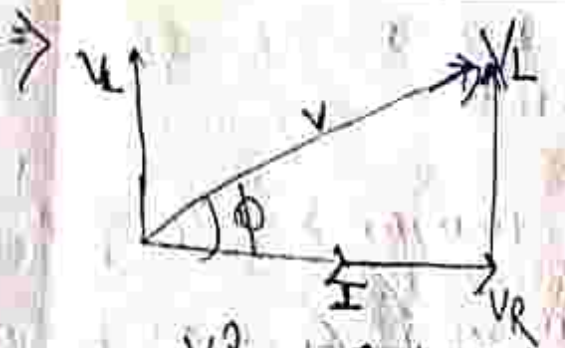
Here, resistance R and capacitor C having capacitive reactance X_C are connected in series across ac supply of $V = V_m \sin \omega t$, and the current flowing is I .

$$V_R = IR \text{ (Voltage Drop across } R)$$

$$V_C = IX_C \text{ (Voltage Drop across } C)$$

$$V = IZ \text{ (Voltage Drop across } Z)$$

Z is impedance & unit of Z of R-C series ckt

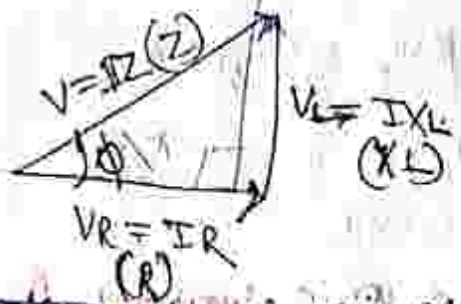


$$V^2 = V_R^2 + V_L^2$$

$$\Rightarrow (IZ)^2 = (IR)^2 + (IX_L)^2$$

$$\Rightarrow \boxed{Z = \sqrt{R^2 + X_L^2}}$$

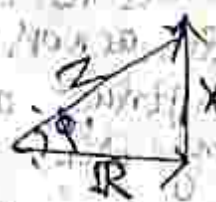
Impedance Triangle



$\phi =$ phase angle (angle between resultant voltage and current)

Power factor

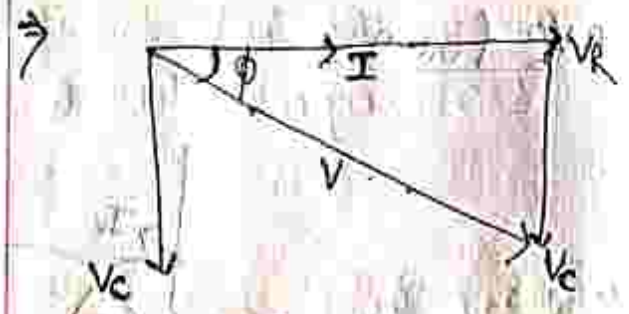
It is defined as the cosine of phase angle i.e. $\cos \phi$. It has no units.



Here; $\cos \phi = \frac{R}{Z} = \frac{R}{\sqrt{R^2 + X_L^2}}$

power \rightarrow Here power consumed by R-L series ckt; $P = VI \cos \phi$ where V & I are rms value of voltage & current.

$$\cos \phi = \frac{R}{Z} = \frac{R}{\sqrt{R^2 + X_L^2}}$$



$$V^2 = V_R^2 + V_C^2$$

$$\Rightarrow (IZ)^2 = (IR)^2 + (IX_C)^2$$

$$\Rightarrow Z^2 = R^2 + X_C^2$$

$$\Rightarrow \boxed{Z = \sqrt{R^2 + X_C^2}}$$

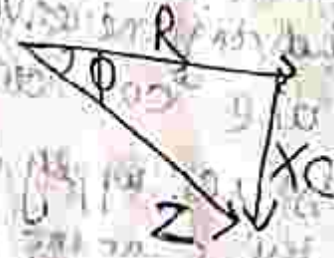
Impedance Triangle



$\phi =$ phase angle (angle between resultant voltage & current)

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It is defined as the cosine of phase angle i.e. $\cos \phi$. It has no units.

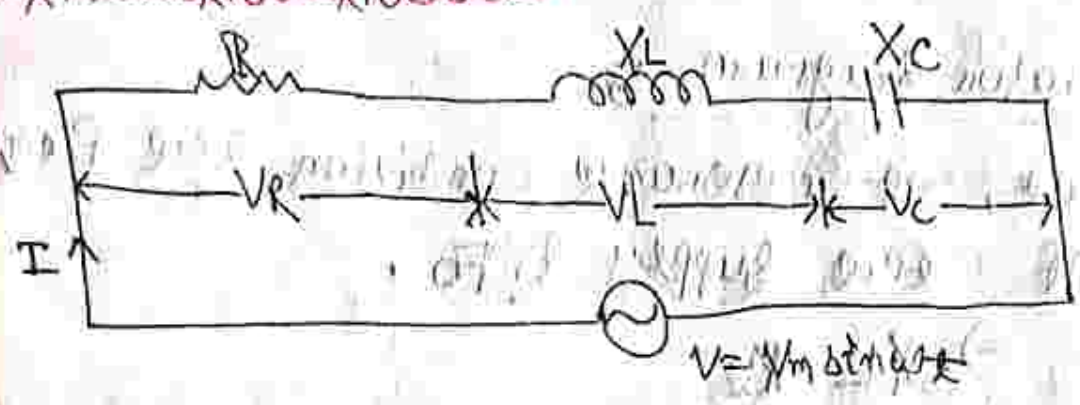


Here; $\cos \phi = \frac{R}{Z} = \frac{R}{\sqrt{R^2 + X_C^2}}$

power \rightarrow Here power consumed by R-C series ckt; $P = VI \cos \phi$ where V & I also rms value of voltage and current.

$$\cos \phi = \frac{R}{Z} = \frac{R}{\sqrt{R^2 + X_C^2}}$$

* R-L-C series circuit



⇒ Here, resistance (R), inductive reactance (XL) & capacitive reactance (XC) are connected in series across ac supply of $V = V_m \sin \omega t$ and the current flowing is I .

⇒ $V_R = IR$ (Voltage drop across resistance).

⇒ $V_L = IX_L$ (Voltage drop across inductance).

⇒ $V_C = IX_C$ (Voltage drop across capacitance).

⇒ The nature of circuit depends upon the value of X_L & X_C , so there are three conditions arise:

- (a) $X_L = X_C$
- (b) $X_L > X_C$
- (c) $X_L < X_C$

(a) $X_L = X_C$ ⇒ when inductive reactance is equal to capacitive reactance then the condition is called resonance condition.

∵ $X_L = X_C$ ∴ $IX_L = IX_C$ ⇒ $V_L = V_C$

⇒ At resonance condition, voltage across inductor & voltage across capacitor.

* Phasor Diagram

Let, at resonance condition, the frequency of the supply is f_0 .

$$\Rightarrow X_L = X_C$$

$$\Rightarrow \omega_0 L = \frac{1}{\omega_0 C}$$

$$\Rightarrow \omega_0^2 = \frac{1}{LC}$$

$$\Rightarrow \omega_0 = \sqrt{\frac{1}{LC}} \Rightarrow \omega_0 = \frac{1}{\sqrt{LC}}$$

⇒ Now, Angular Velocity = $\frac{\text{Angular displacement}}{\text{Time}}$

$$\omega = \frac{\theta}{T}$$

$$\Rightarrow \omega = \frac{2\pi}{T}$$

$$\Rightarrow \omega = 2\pi F$$

[Time → Time period (T),
i.e. Time required to complete one cycle]

[Frequency = $\frac{1}{\text{Time period}}$]

[Frequency is reciprocal of time period]

Here, $2\pi F = \frac{1}{\sqrt{LC}}$

$$\Rightarrow F_0 = \frac{1}{2\pi\sqrt{LC}} \quad \left[F_0 \text{ is resonance frequency} \right]$$

⇒ At the resonance condition both the voltage V_L & V_C are cancelled each other. Hence only V_R is dominant.

⇒ So, at resonance condition the entire R-L-C series circuit behaves as a resistive circuit.

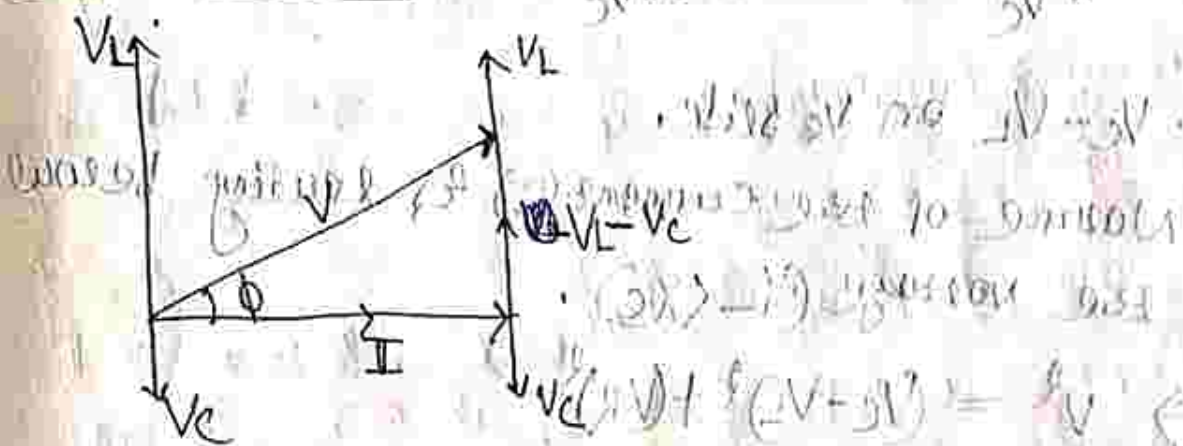
① $X_L > X_C$

⇒ $I X_L > I X_C$

⇒ $V_L > V_C$

⇒ $V_L - V_C > 0$

← Phasor Diagram ⇒



⇒ $V_L - V_C$ is on V_L side

⇒ Nature of the current (I) is lagging behind the voltage ($X_L > X_C$)

$$\Rightarrow V^2 = (V_L - V_C)^2 + V_R^2$$

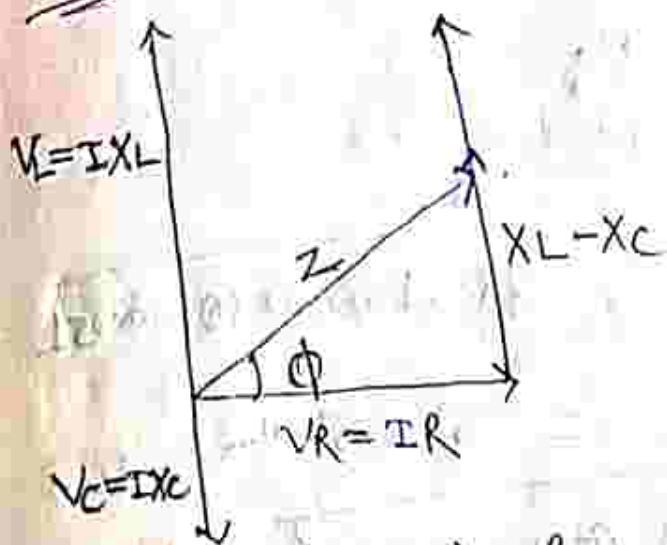
$$\Rightarrow (IZ)^^2 = (IX_L - IX_C)^2 + (IR)^2$$

$$\Rightarrow Z^2 = (X_L - X_C)^2 + R^2$$

$$\Rightarrow Z = \sqrt{R^2 + (X_L - X_C)^2}$$

* $X_L > X_C$

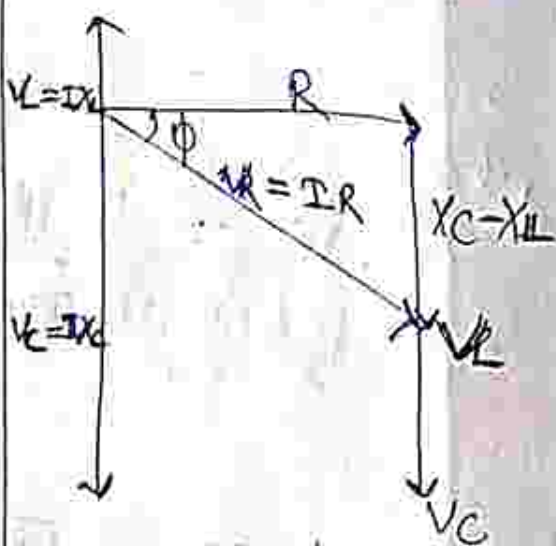
* power factor \Rightarrow



$$\cos \phi = \frac{R}{Z}$$

* $X_L < X_C$

* power factor



$$\cos \phi = \frac{R}{Z}$$

* Problem

In a R-L-C series circuit $R = 30 \Omega$,

$L = 15 \text{ mH}$ and $C = 51 \mu\text{F}$. If the source voltage and frequency are 12 V and 60 Hz ; what is the current and power factor of the circuit.

Soln

Data given

$R = 30 \Omega$

$L = 15 \text{ mH} = 0.015 \text{ H}$

$C = 51 \mu\text{F} = 51 \times 10^{-6}$

$V = 12 \text{ V}$

$F = 60 \text{ Hz}$

$$X_L = 2\pi fL$$

$$= 2\pi \times 60 \times 0.015$$

$$= 5.655 \Omega$$

$$X_C = \frac{1}{2\pi fC} = \frac{1}{2 \times 3.15 \times 60 \times 0.000051}$$

$$= 5.65 \Omega$$

$$Z = \sqrt{(30)^2 + (5.65 - 5.65)^2}$$

$$= 55.21 \Omega$$

$$I = \frac{V}{Z} = \frac{12}{55.21} = 0.217 A$$

$$\cos \phi = \frac{R}{Z} = \frac{30}{55.21} = 0.54$$

At 12.11.2020

* R-L-C Parallel Circuit

⇒ There are two methods for solving R-L-C Parallel Circuits

1. Vector or phasor method
2. Phasor algebra method

1. Phasor Algebra method

⇒ In this case to represent a circuit we use (j) denotation in the complex instead of (i).

⇒ The inductive reactance taken by +ve sign whereas the capacitive reactance taken as -ve sign. So a branch in the circuit written as $R + jX_L$ & $R - jX_C$.

⇒ The complex form is known as rectangular form but it can be represented by another form known as polar form or angle form.

$R + jX_L$ & $R - jX_C \rightarrow$ Rectangular form.

$R \angle \theta$ or $R \angle -\theta \rightarrow$ Polar form.

These both are inter-convertible.

⇒ Rectangular to Polar



$\text{POL}(R, X_L)$ or $\text{POL}(R, -X_C)$

Ans $Z \angle \theta$

Ans $Z \angle -\theta$

⇒ Polar to Rectangular

$\text{Rec}(Z, \theta)$

i.e. $\text{Rec}(Z, \theta) = R + jX_L$

$\text{Rec}(Z, -\theta) = R - jX_C$

⇒ The addition and subtraction of complex impedance done for Rectangular form.

$$R_1 + jX_{L1} = Z_1 \angle \theta_1$$

$$R_2 + jX_{L2} = Z_2 \angle \theta_2$$

* Phase is a path in which is a path of current flow but voltage seen in electrical circuit.

* Polyphase \Rightarrow It means more than one path for current flow but voltage is seen in electrical circuits only.

* Different types of current \Rightarrow
ministry ministry ministry ministry ministry

\Rightarrow There is two types of current \Rightarrow

1. Phase current.

2. Line current.

(1) Phase current \Rightarrow It is the current which is flowing from one phase to neutral. It is denoted by the letter

(I_{Ph}). Its unit is ampere.

$$[I_{Ph} = I_{RN} = I_{YN} = I_{BN}]$$

where;

I_{Ph} = Current in phase.

I_{RN} = current between Red phase and Neutral.

I_{YN} = current between yellow phase and Neutral.

I_{BN} = current between Blue phase and Neutral.

① Line current \Rightarrow It is the current flowing between any two phases.

\Rightarrow R to Y ; Y to B ; B to R.

$$\Rightarrow [I_{RY} = I_{YB} = I_{RB} = I_L]$$

* Different Types of voltage \Rightarrow There are two types of voltage, i.e. 1. Phase voltage
2. Line voltage

1. Phase voltage \Rightarrow It is the voltage lies between any phase to neutral i.e. $[V_{RN} = V_{BN} = V_{YN} = V_{ph}]$

2. Line voltage \Rightarrow It is the voltage lies between any two phases. i.e. $[V_{RY} = V_{YB} = V_{RB} = V_L]$

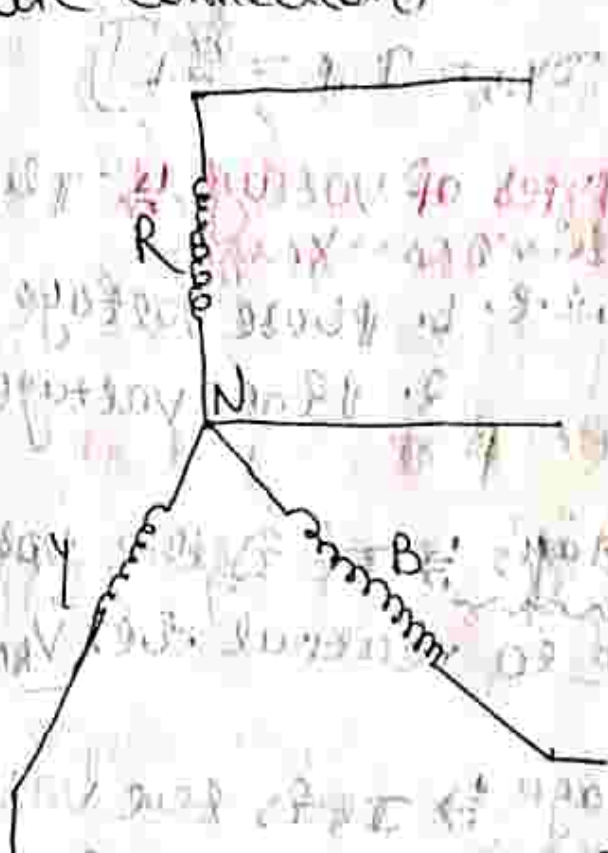
\Rightarrow In case of three phase circuit there are two types of configurations is possible.

i.e. (a) Star (Y) connection or star (Y) configuration.

(b) Delta (Δ) connection or Delta (Δ) configuration.

① Star connection \Rightarrow If the similar ends of three individual winding are connected in a single point and the output is taken by other three points of winding then the configuration is known as star connection or configuration.

\Rightarrow As we know that the AC supply generated by AC generator or alternator to that the winding of alternator are star connection,



\Rightarrow In this case the output is obtained by the four wire system.

* Relations between different types of current

(I_{ph}) or $(I_L) \Rightarrow$

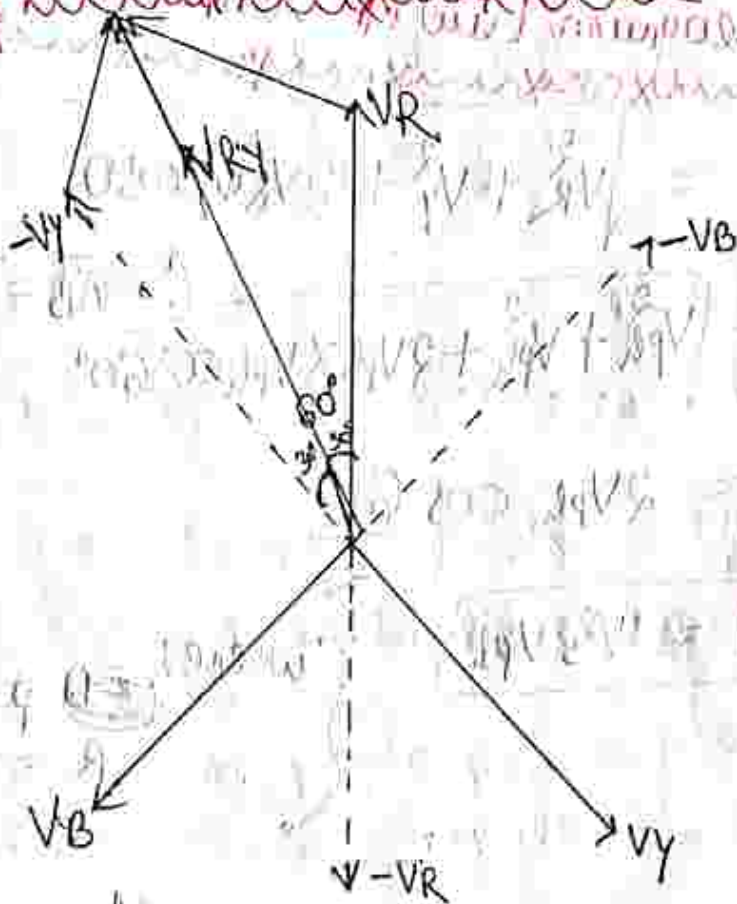
\Rightarrow If the current flowing between R to N, Y to N and B to N then it is called Phase current (I_{ph}) .

\Rightarrow Similarly, the current flowing between R to Y, Y to B and B to R are known as Line current (I_L) .

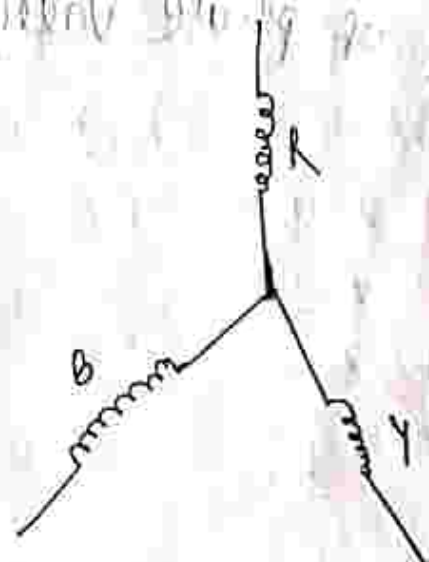
\Rightarrow So, it seems that each line is in series with its individual phase winding. Hence the line current in each line is the same as that the phase winding current to which the line is connected.

So here, $I_L = I_{ph}$

Relations between different voltage



$\Rightarrow V_{RN} = V_{BN} = V_{YN} = V_R / \sqrt{3} = V_{ph}$



$$\Rightarrow \vec{V}_{RY} = \vec{V}_{YB} = \vec{V}_{BR} = \vec{V}_L$$

$$\Rightarrow \vec{V}_{RY} = \vec{V}_R - \vec{V}_Y$$

$$\Rightarrow \vec{V}_{YB} = \vec{V}_Y - \vec{V}_B$$

$$\Rightarrow \vec{V}_{BR} = \vec{V}_B - \vec{V}_R$$

* Parallelogram Law of Vector Addition

$$\Rightarrow \vec{V}_{RY} = \sqrt{V_R^2 + V_Y^2 + 2V_R V_Y \cos \theta}$$

$$\Rightarrow \vec{V}_L = \sqrt{V_{ph}^2 + V_{ph}^2 + 2V_{ph} \times V_{ph} \cos 60^\circ} \quad \left(\vec{A} \cdot \vec{B} = A \cdot B \cos \theta \right)$$

$$\Rightarrow \vec{V}_L = \frac{2V_{ph} \cos 60^\circ}{2}$$

$$\Rightarrow \boxed{\vec{V}_L = \sqrt{3} V_{ph}}$$

where

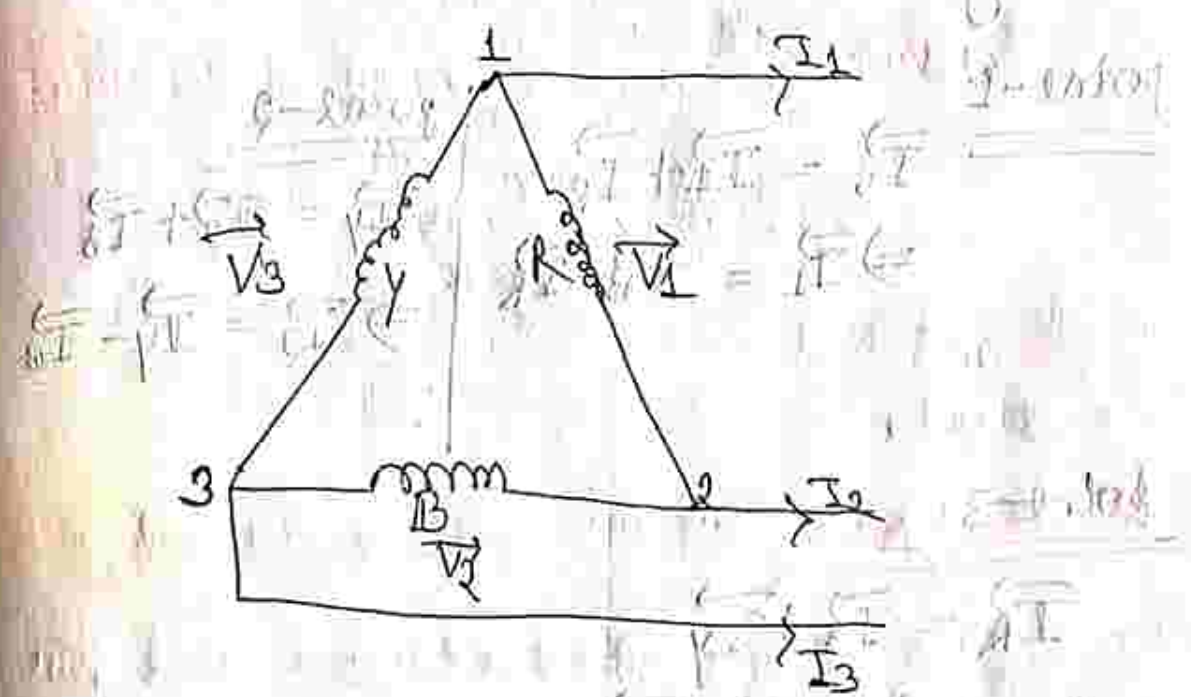
$$p = Q$$

$$R = \frac{2p \cos \theta}{2}$$

\Rightarrow In star connection, the line voltage is $\sqrt{3}$ times of phase voltage.



* Delta Connection In the delta connection the two distant ends of two windings are connected in a single point i.e. the three windings distant ends are connected three distinct points to form a closed path.



* Relation between different types of voltage

⇒ In delta connection among the 3 phases, two phases are acts as incoming and one phase is acts as a neutral. so we say that the voltage between any two phase, is either V_{ph} or V_L . so $V_L = V_{ph}$.

* Relation between line current and phase current

* Here the line currents are $I_1 = I_2 = I_3 = I_L$.

* Here $\vec{I}_1, \vec{I}_2, \vec{I}_3$ are line currents, whereas I_R, I_Y and I_B .

$$\Rightarrow \vec{I}_1 = \vec{I}_0 = \vec{I}_3 = \vec{I}_L$$

$$\Rightarrow \vec{I}_R = \vec{I}_Y = \vec{I}_B = \vec{I}_{Ph}$$

Applying KCL to point 1, 2, 3 \Rightarrow

point-1

$$\vec{I}_B = \vec{I}_1 + \vec{I}_R$$

$$\Rightarrow \vec{I}_1 = \vec{I}_B - \vec{I}_R$$

point-2

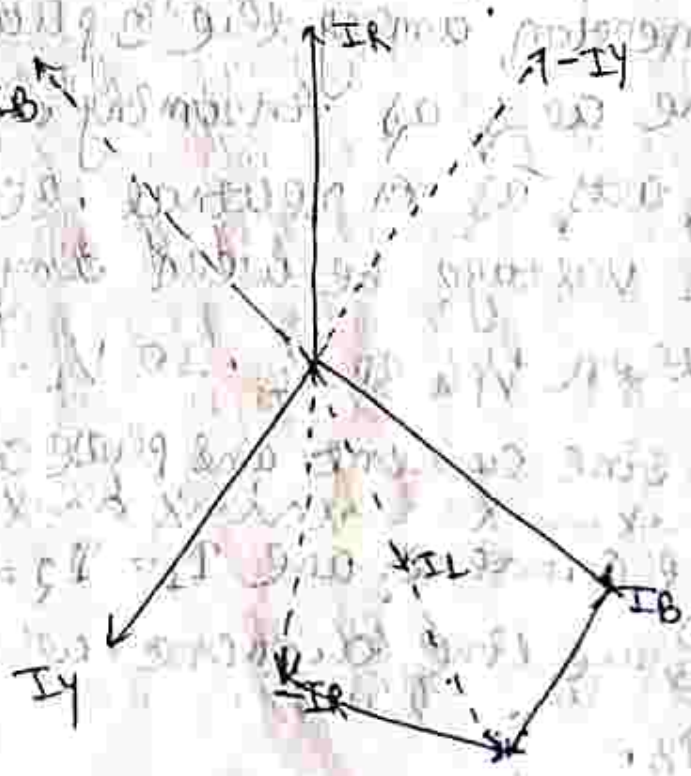
$$\vec{I}_Y = \vec{I}_2 + \vec{I}_B$$

$$\Rightarrow \vec{I}_2 = \vec{I}_Y - \vec{I}_B$$

point-3

$$\vec{I}_R = \vec{I}_3 + \vec{I}_Y$$

$$\Rightarrow \vec{I}_3 = \vec{I}_R - \vec{I}_Y$$



$$\Rightarrow \vec{I} = \sqrt{I_B^2 + I^2 R + 2 I_B I R \cos \theta}$$

$$\Rightarrow \vec{I} = \sqrt{I_{ph}^2 + I_{ph}^2 + 2 I_{ph} \cdot I_{ph} \cos 60^\circ}$$

Here: $p = Q$

$$\text{So: } R = 2 p \cos \theta$$

$$\Rightarrow \vec{I}_L = 2 \vec{I}_{ph} \cos 60^\circ$$

$$\Rightarrow \vec{I}_L = 2 \vec{I}_{ph} \cos 30^\circ$$

$$\Rightarrow \boxed{\vec{I}_L = \sqrt{3} \vec{I}_{ph}}$$

* 3 ϕ power for both 'y' and ' Δ ' connections \Rightarrow
~~xxxxxxx~~

\Rightarrow As we know that the 1 ϕ power (p) = $V I \cos \phi$ or
 $V_{ph} I_{ph} \cos \phi$; so, in both ' Δ ' and 'y' connections
 the 3 ϕ power;

$$\Rightarrow 3\phi \text{ power} = 3 V_{ph} I_{ph} \cos \phi$$

\Rightarrow In Δ In Δ connection we know that

$$V_L = V_{ph} \text{ \& } I_L = \sqrt{3} I_{ph}$$

$$\text{So: } P(3\phi) = 3 V_{ph} I_{ph} \cos \phi$$

$$= 3 V_L \frac{I_L}{\sqrt{3}} \cos \phi$$

$$\Rightarrow \boxed{P(3\phi) = \sqrt{3} V_L I_L \cos \phi}$$

* In Δ (star) \Rightarrow

γ connections we know that

$$I_L = I_{ph} \text{ and } V_L = \sqrt{3} V_{ph}$$

$$\text{So; } P(3\phi) = 3V_{ph} I_{ph} \cos\phi$$

$$= 3 \frac{V_L}{\sqrt{3}} I_L \cos\phi$$

$$\Rightarrow \boxed{P(3\phi) = \sqrt{3} V_L I_L \cos\phi}$$

Both γ and Δ connections the power is constant.

New Chapter Filter Circuits

* Filter is an electrical circuit used for purifying the electrical energy. Mostly AC electrical energy, as it has associated with frequency. So we design such circuit by combining different circuit elements like R-L-C.

* Among of elements R-L and C, the inductor and capacitor are frequency sensitive element. As we know that $X_L = 2\pi fL$

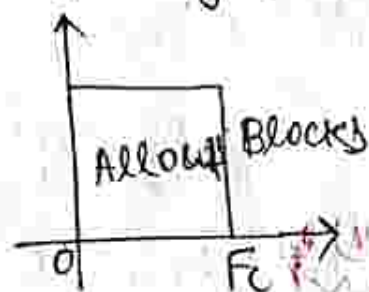
$$\text{and } X_C = \frac{1}{2\pi fC}, \text{ from this relation}$$

it is conclude that $X_L \propto f$ and $X_C \propto \frac{1}{f}$.

So, by combining R-L-C circuit elements we have design such circuit which may allow or reject particular frequency. So according to passing of different ranges of frequency the filters circuit are of four types \Rightarrow

1. Low pass filter
2. High pass filter
3. Band pass filter
4. Band stop filter

① Low pass filter \Rightarrow According to the name suggest it allows only lower order frequency but attenuates (block) all other higher frequency. So it allow frequency from zero (0) to cut-off frequency (f_c).



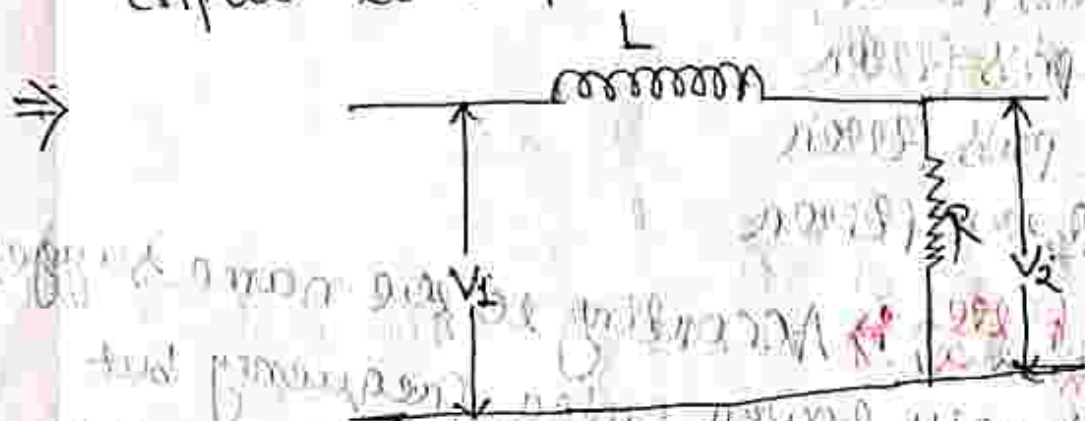
+ Cut-off frequency \Rightarrow It is the frequency upto which or from which the frequency allow by the filter circuit allow or stop frequency response.

\Rightarrow According to the circuit arrangement the low pass filter are of two types \Rightarrow

- (1) R-L low pass filter
- (2) R-C low pass filter

(1) R-L low pass filter

Here inductance (L) is connected in series instead parallel because at low frequency the inductance offer low impedance. So; easily the lower frequency pass from input to output.



$\omega_c = \text{cut off angular velocity} = \frac{R}{L}$
(Taking Laplace transform of above circuit)

$$\Rightarrow 2\pi f_c = \frac{R}{L}$$

$$\Rightarrow f_c = \frac{R}{2\pi L}$$

(2) R-C low pass filter

Here the capacitance is connected in parallel instead of series, because at low frequency it effects a high impedance.

$$\Rightarrow \omega_c = \frac{1}{RC} \text{ (Taking Laplace transform)}$$

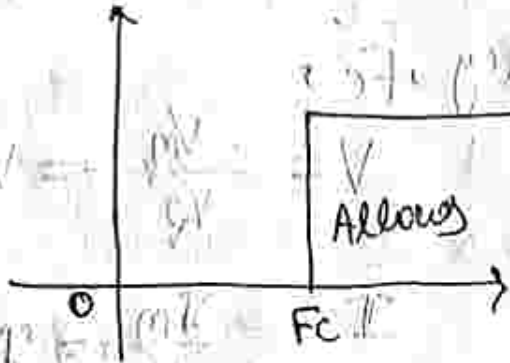
$$\Rightarrow 2\pi f_c = \frac{1}{RC}$$

$$\Rightarrow f_c = \frac{1}{2\pi RC}$$

(2) High pass filter

According to the name suggest it allows higher order frequency or attenuates towards lower order frequency.

⇒



It is also are two types below

(a) R-L high pass filters

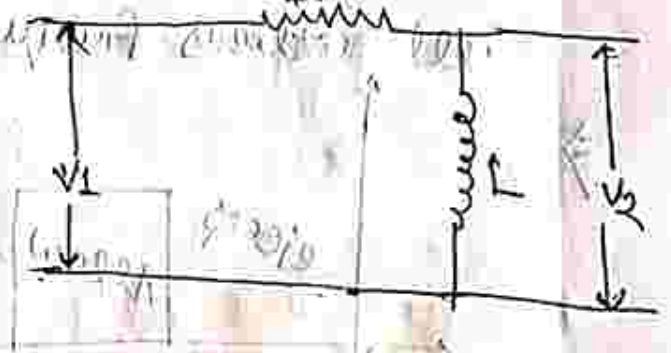
(b) R-C high pass filters

(a) R-L high pass filter

⇒ $\omega L = R$

⇒ $2\pi fL = R$

⇒ $fL = \frac{R}{2\pi}$

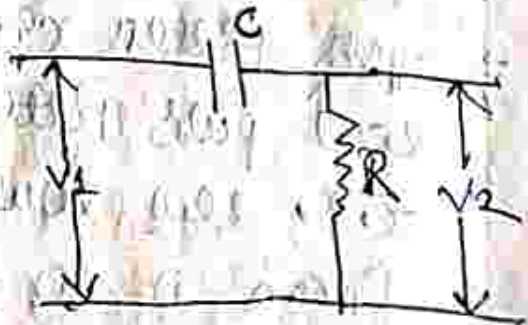


(b) R-C high pass filter

⇒ $\omega C = \frac{1}{R}$

⇒ $2\pi fC = \frac{1}{R}$

⇒ $fC = \frac{1}{2\pi R}$



* Cut-off frequency (f_c) \Rightarrow

\Rightarrow It is the frequency at which magnitude of element parameter (V or I) is $\frac{1}{\sqrt{2}}$ ratio of maximum magnitude (RMS value).

At frequency, f_c ,

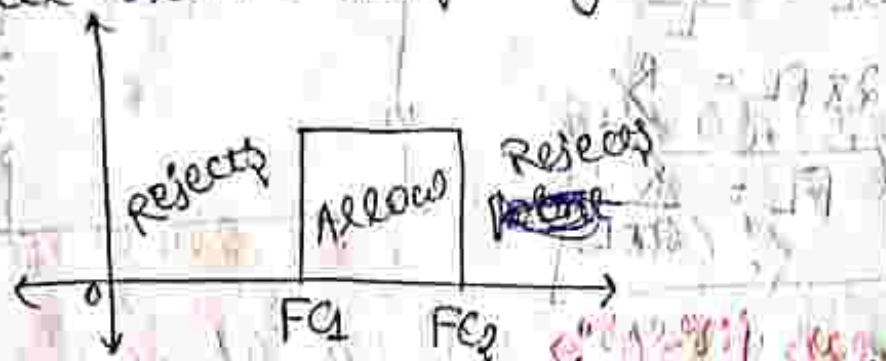
$$V = \frac{V_m}{\sqrt{2}} = V_{RMS}$$

$$I = \frac{I_m}{\sqrt{2}} = I_{RMS}$$

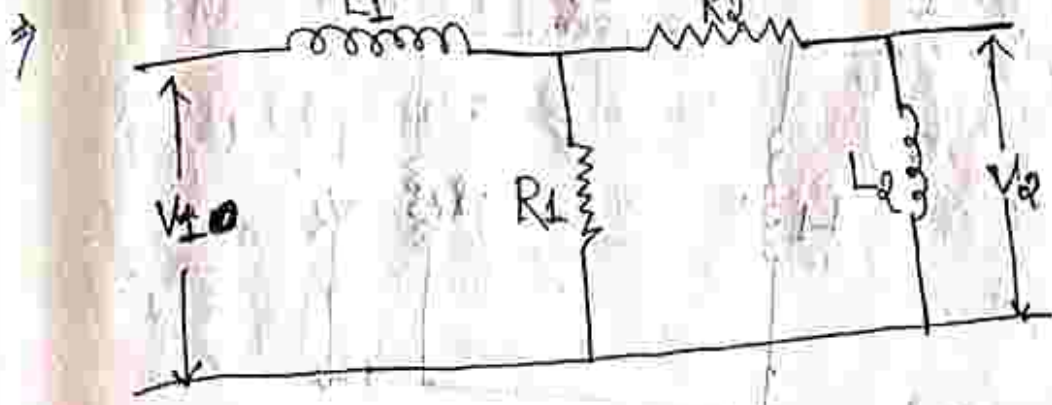
\Rightarrow But power = $\frac{1}{2}$ times of P_m (maximum power).

(3) "Band pass Filter" (BPF)

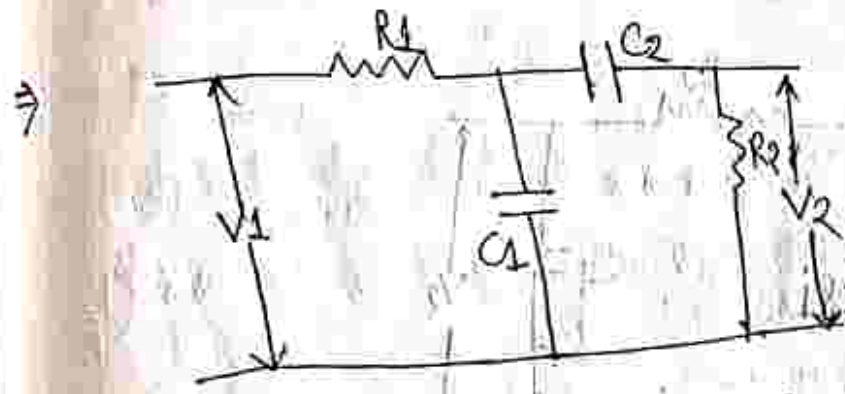
\Rightarrow It is the circuit which allow only particular band of frequency and rejects towards all others frequency.



\Rightarrow This filter circuit is obtained by cascading low pass filter with high pass filter. i.e. the low pass filter allow frequency from 0 to f_{c2} and the high pass filter allow frequency from f_{c1} to ∞ frequency. So cascading both the band f_{c1} to f_{c2} is obtained.

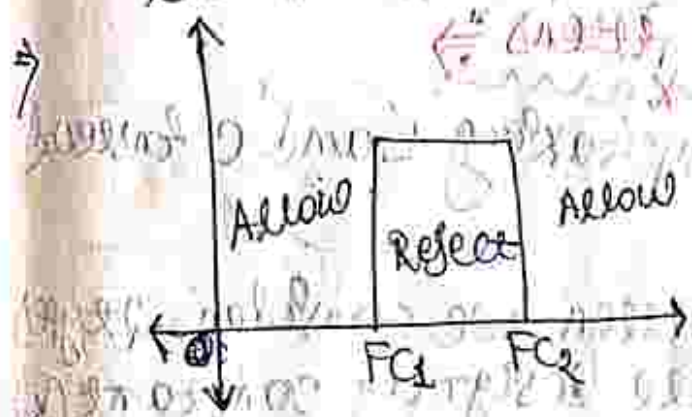


$$F_{CL} = \frac{1}{2\pi R_1 C_1} \quad , \quad F_{CH} = \frac{R_2}{2\pi L_2}$$
 where }
 F_{CL} = Low cut-off frequency
 F_{CH} = High cut-off frequency

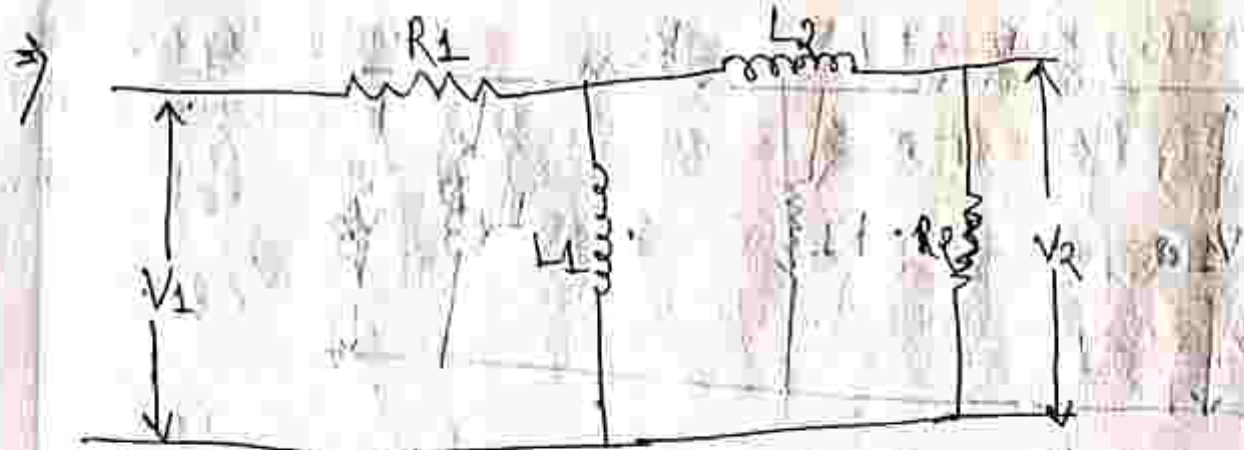


4) Band stop filter (BSF)

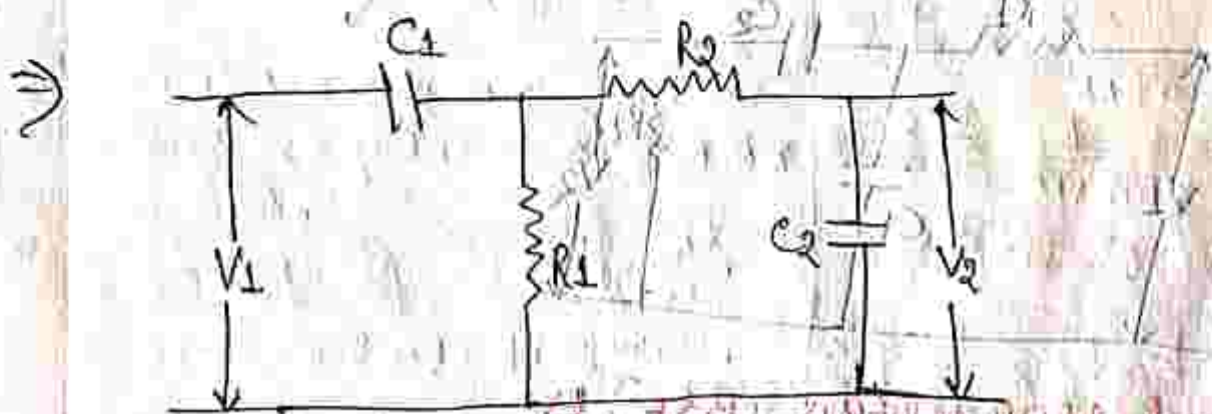
It is the filter circuit which does not allow particular band of frequency except that particular band.



Band stop filter is obtained by cascading high pass filter with low pass filter.



$$F_{CL} = \frac{R_1}{2\pi L_1}$$



$$F_{CH} = \frac{1}{2\pi R_2 C_2}$$

DATE: 03.12.2020

* Constant (K) Types filters

- (i) It can be design by taking 'L' and 'C' instead of R-L and R-C.
- (ii) In this types of filter we consider 2 types of impedance while designing constant (K) type filter. The impedance are Z_1 and Z_2 .
 - ⇒ Z_1 = Series impedance.
 - ⇒ Z_2 = Shunt impedance.

The product of Z_1 and Z_2 is a constant k .

$$\Rightarrow Z_1 \times Z_2 = k = (R_0)^2$$

where R_0 is known as design impedance of particular frequency.

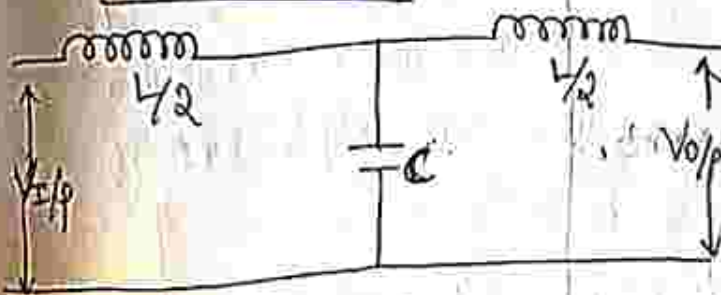
The filter circuit which obeys this above property is called constant k -types filter. So while designing the filter circuit is of two types of configurations are generally possible for every filter circuit.

(1) T-type sections.

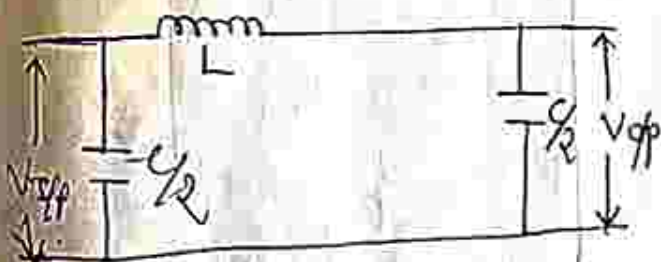
(2) π -type sections.

Low pass filters

T-sections

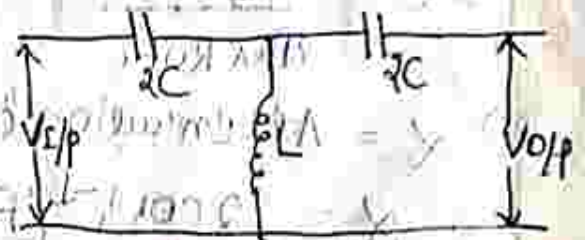


π -sections

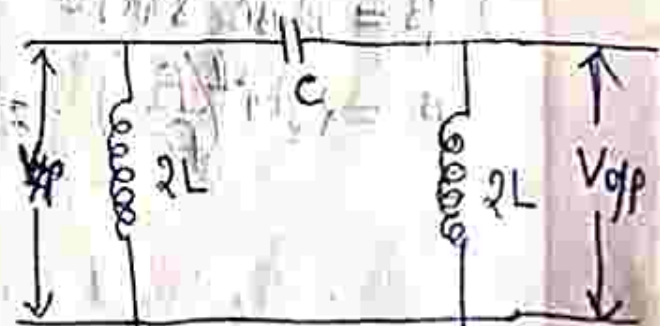


High pass filters

T-sections



π -sections



Low pass Filter

$$\Rightarrow Z_o(\omega) = R_o \sqrt{1 - \left(\frac{F}{F_c}\right)^2}$$

$$\Rightarrow R_o = \sqrt{\frac{L}{C}}$$

$$\Rightarrow F_c = \frac{1}{\pi \sqrt{LC}}$$

$$\Rightarrow Z_o(\pi) = \frac{R_o}{\sqrt{1 - \left(\frac{F}{F_c}\right)^2}}$$

$\Rightarrow Z_o(\omega)$ and $Z_o(\pi)$ are characteristic impedances of Π and π sections.

$\Rightarrow R_o =$ Design Impedance.

$\Rightarrow F_c =$ Cut-off frequency.

$$\Rightarrow L = \frac{R_o}{\pi F_c}$$

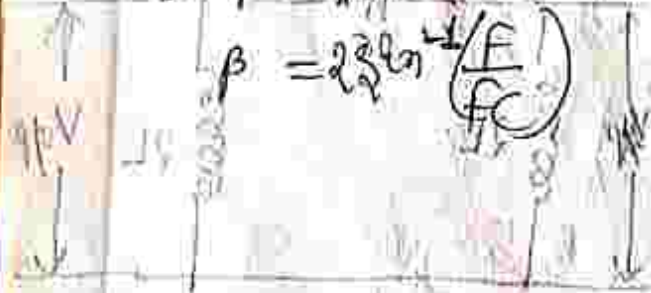
$$\Rightarrow C = \frac{1}{\pi R_o F_c}$$

$\Rightarrow \alpha =$ Attenuation constant.

$$\Rightarrow \alpha = 2 \cosh^{-1} \left(\frac{F}{F_c} \right)$$

$\Rightarrow \beta =$ Phase shift

$$\beta = 2 \sin^{-1} \left(\frac{F}{F_c} \right)$$



High pass Filter

$$\Rightarrow Z_o(\omega) = R_o \sqrt{1 - \left(\frac{F_c}{F}\right)^2}$$

$$\Rightarrow Z_o(\pi) = \frac{R_o}{\sqrt{1 - \left(\frac{F_c}{F}\right)^2}}$$

$$\Rightarrow R_o = \sqrt{L/C}$$

$$\Rightarrow F_c = \frac{1}{4\pi LC}$$

$$\Rightarrow L = \frac{R_o}{4\pi F_c}$$

$$\Rightarrow C = \frac{1}{4\pi R_o F_c}$$

$$\Rightarrow \alpha = 2 \cosh^{-1} \left(\frac{F_c}{F} \right)$$

$$\Rightarrow \beta = 2 \sin^{-1} \left(\frac{F_c}{F} \right)$$



* Two port Network → In the two-port network

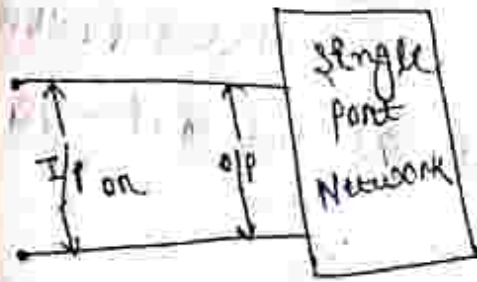
We found input voltage and output voltage resulting which flow a current between input to output.

⇒ So two port network is a network which performed specific task when input is given and at last it shows a specific output voltage.

⇒ There are two types of port networks are present →

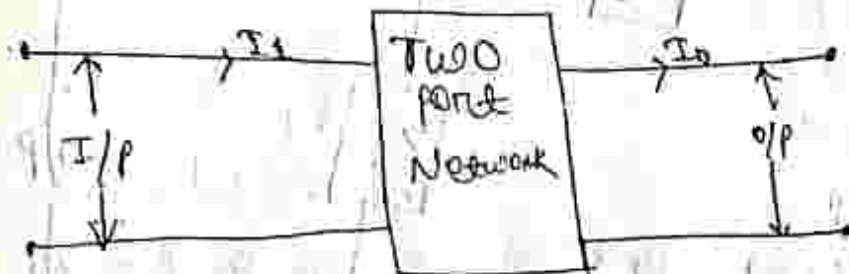
1. Single-port network
2. Two-port network

(1) Single-port Network → Any active or passive network containing only two terminals on a pair of terminals which is acts as both input and output then it is called single-port network.



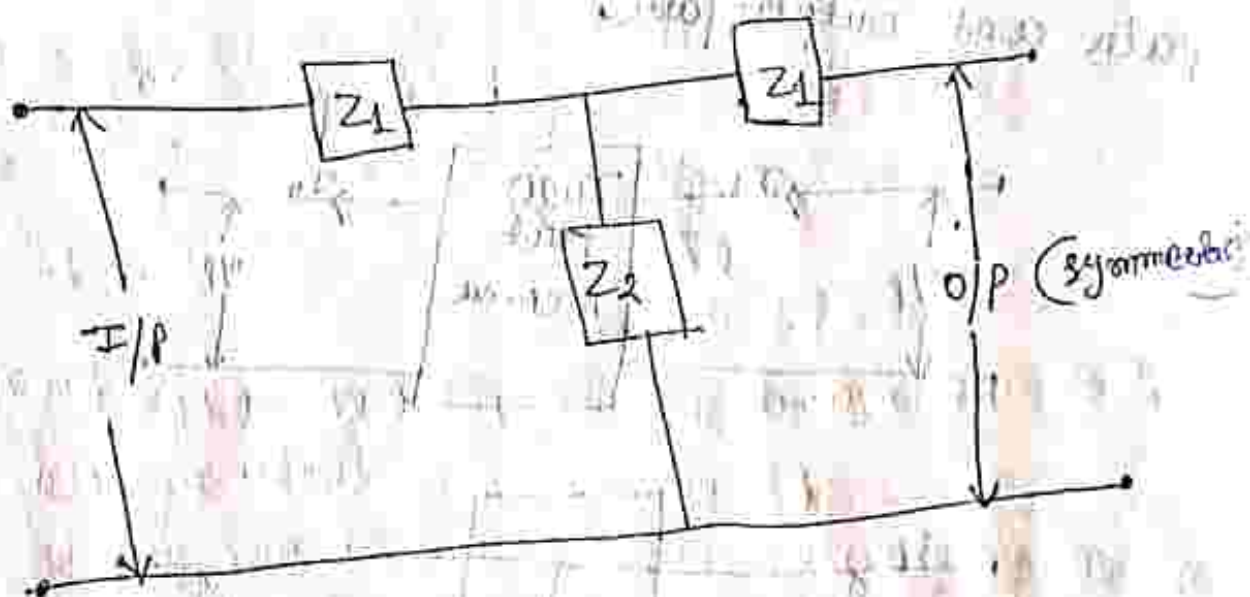
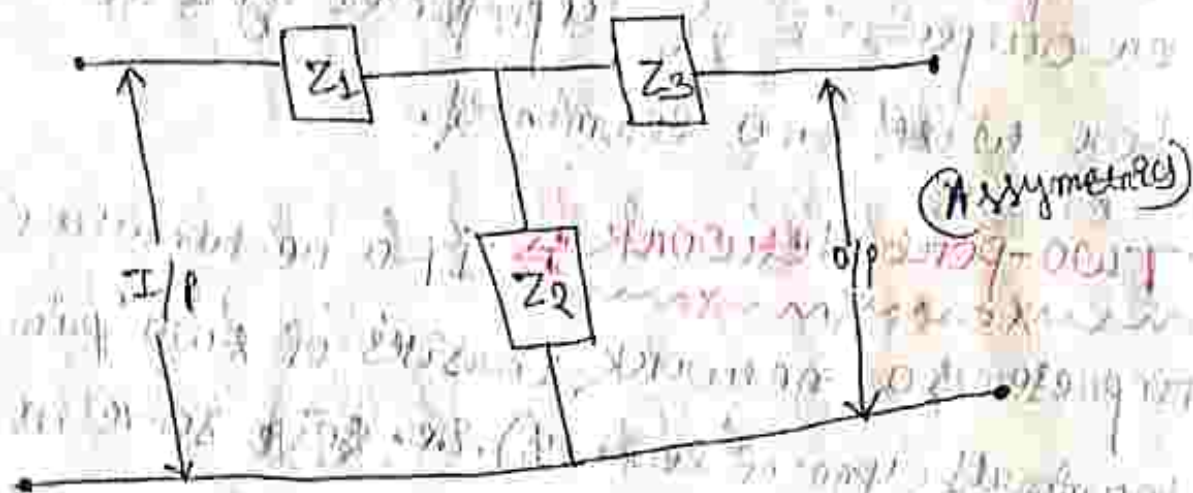
The pair of terminals is of either use as input or output it is represented by a rectangular box with two terminals.

Two-port Network → If a rectangular box that represents a network consists of two pairs of terminals (4 no. of terminals). i.e. ~~two~~ serve as input pair and output pair.



* Network configurations \Rightarrow
 \Rightarrow There are several network configurations among which T and π are mainly used.

T-sections \Rightarrow



Let the output terminal 2 be open circuited.
 i.e. $I_2 = 0$.

So from eqn (2); we get

$$Z_{11} = \frac{V_1}{I_1}$$

and from eqn. (2) $Z_{21} = \frac{V_2}{I_1}$

Let the input terminal 1 be open circuited.

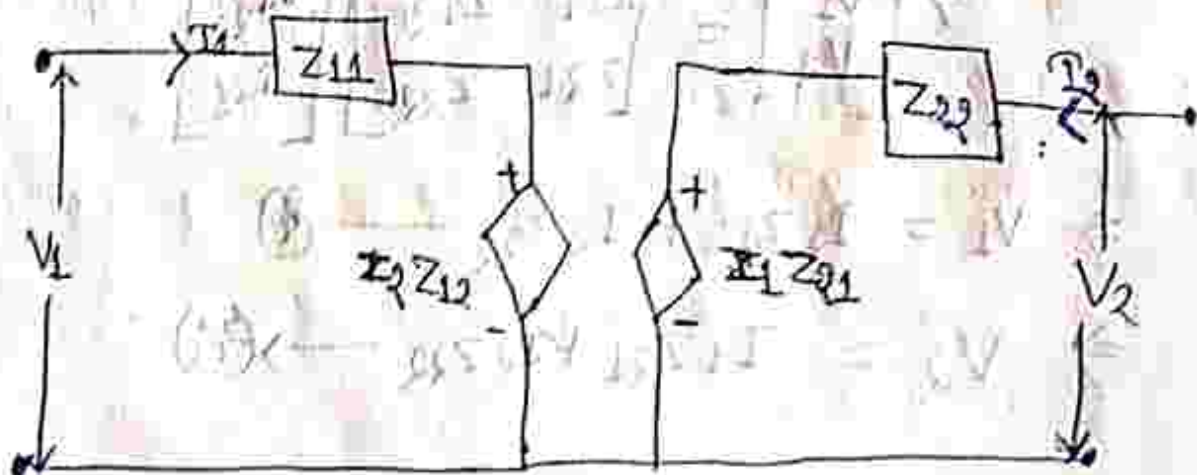
i.e. $I_1 = 0$.

So from eqn. (2) $Z_{12} = \frac{V_1}{I_2}$

and from eqn. (2);

$$\Rightarrow Z_{22} = \frac{V_2}{I_2}$$

⇒ Hence, Z_{11} , Z_{12} , Z_{21} and Z_{22} are obtained by open circuiting the terminal; so they are known as open circuit parameters.



where $I_1 Z_{11}$ and $I_2 Z_{22}$ are current control voltage source (CCVS) and Z_{11} and Z_{22} are input and output side impedance.

* Short circuit parameter or ~~Z-parameters~~ Y -parameters (Admittance) \Rightarrow

\Rightarrow The admittance is defined as the reciprocal of real part of the impedance. i.e. reciprocal of impedance also.

$$Y = \frac{1}{Z}$$

$$\Rightarrow Z = \frac{V}{I} \Rightarrow I = \frac{V}{Z} \Rightarrow I = VY$$

$$\text{or } Y = \frac{I}{V}$$

Here, in matrix form:

$$\Rightarrow [I] = [Y] \times [V]$$

$$\Rightarrow \begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} \times \begin{bmatrix} Y_{11} & Y_{12} \\ Y_{21} & Y_{22} \end{bmatrix}$$

In equation form:

$$I_1 = Y_{11} V_1 + Y_{12} V_2 \quad \text{--- (1)}$$

$$I_2 = Y_{21} V_1 + Y_{22} V_2 \quad \text{--- (2)}$$

where Y_{11} and Y_{12} , Y_{21} & Y_{22} are short circuit parameters or Y -parameter.

⇒ When output terminal is short circuited
then $V_2 = 0$.

From eqn. (1); $I_1 = Y_{11} V_1$

⇒ $Y_{11} = \frac{I_1}{V_1}$

From eqn. (2); $I_2 = Y_{21} V_1$

⇒ $Y_{21} = \frac{I_2}{V_1}$

⇒ When input terminal is short circuited
then $V_1 = 0$.

From eqn. (1) ⇒ $I_1 = Y_{12} V_2$

⇒ $Y_{12} = \frac{I_1}{V_2}$

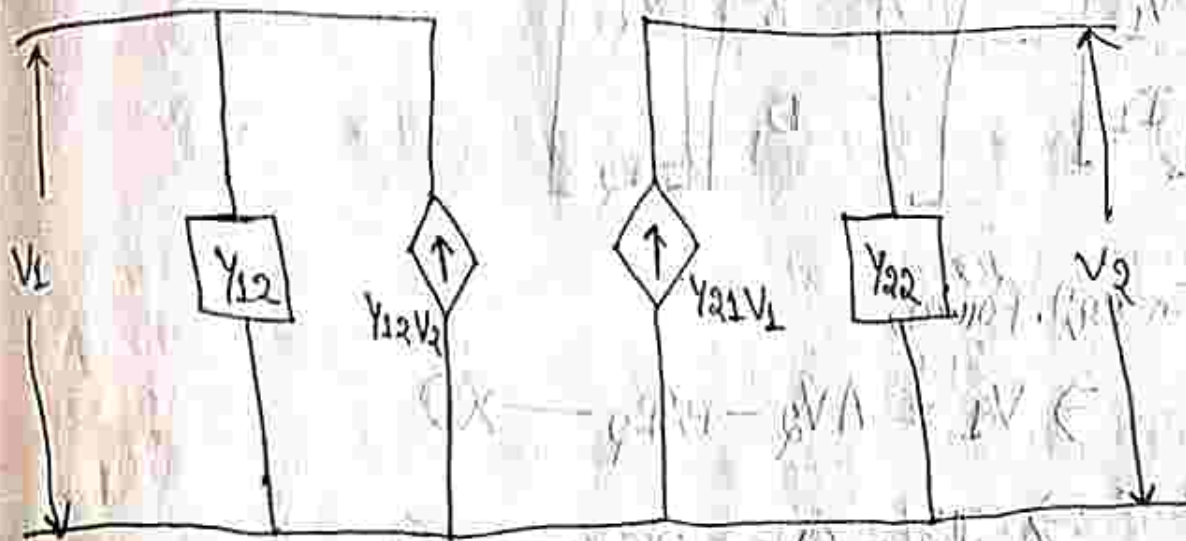
From eqn. (2) ⇒ $I_2 = Y_{22} V_2$

⇒ $Y_{22} = \frac{I_2}{V_2}$

where Y_{11} , Y_{22} are input and output driving point admittance and Y_{12} , Y_{21} are reverse and forward transmission admittance.

Q. X

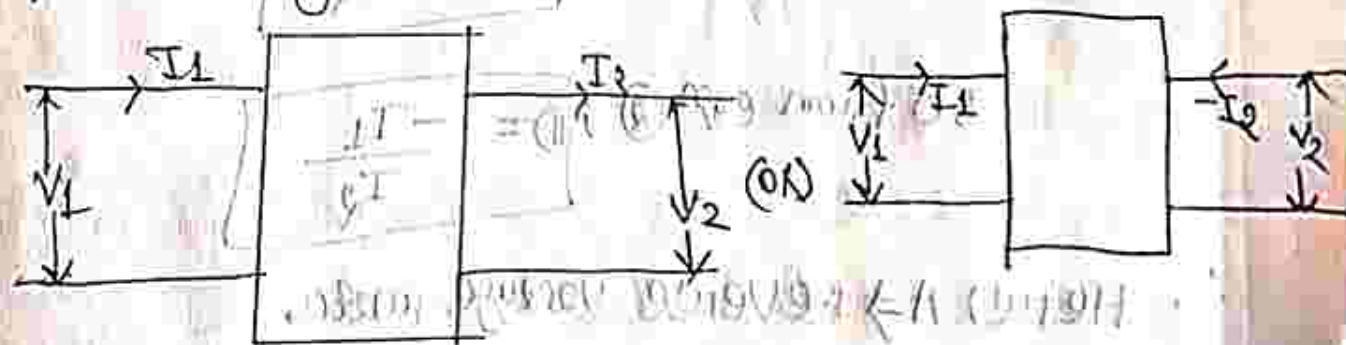
mathematically;



where $Y_{12} V_2$ and $Y_{21} V_1$ are voltage controlled current source.

* ABCD parameters or mixed parameters or Transmission parameters

⇒ ABCD parameters are mostly used to analyse power transfer in a transmission line & known as mixed circuit parameters or transmission parameters. Hence the input side is known as sending ends and output side is known as receiving ends.



$$\Rightarrow \begin{bmatrix} V_1 \\ I_1 \end{bmatrix} = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} V_2 \\ -I_2 \end{bmatrix}$$

⇒ In eqn. form;

$$\Rightarrow V_1 = AV_2 - BI_2 \quad \text{--- (1)}$$

$$\Rightarrow I_1 = CV_2 - DI_2 \quad \text{--- (2)}$$

⇒ When output side is open circuited;

$$\text{so, } I_2 = 0$$

so, from eqn. (1);

$$A = \frac{V_1}{V_2}$$

so, from eqn. (2);

$$C = \frac{I_1}{V_2}$$

⇒ When output is short circuited i.e. $V_2 = 0$

so from eqn. (1);

$$B = \frac{-V_1}{I_2}$$

so from eqn. (2);

$$D = \frac{-I_1}{I_2}$$

Here; A ⇒ Reverse voltage ratio.

C ⇒ Transfer admittance.

B ⇒ Transfer impedance.

D ⇒ Reverse current ratio.

Dt: 17.12.2020

* Coupled circuit → The coupled circuit is based on inductance i.e. the property of induction. The inductance means the property of a material which opposes the change of sudden value of current. It is denoted by L . Its unit is Henry (H).

⇒ Generally, inductors are nothing but a coil i.e. conductor having a number of turns. When current flows through the inductor or coil, flux is produced and that magnetic flux links with own conductor and emf is induced (according to Faraday's law).

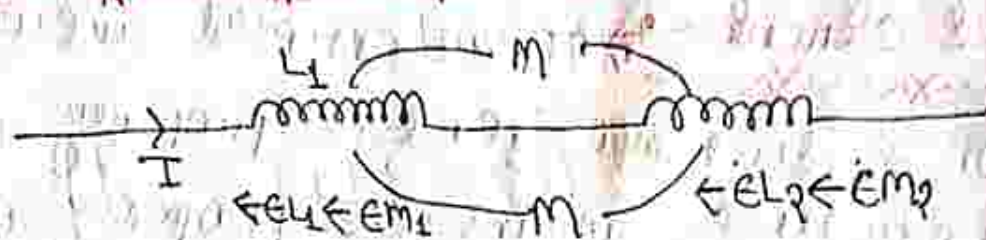
So, $\boxed{\epsilon = -N \frac{d\phi}{dt}}$ where, N is the no. of turns of the coil.

⇒ Due to change of current across the inductor the emf is also induced in the coil. So again,

$\boxed{\epsilon = -L \frac{dI}{dt}}$

where, L is the coefficient of self inductance and $\frac{dI}{dt}$ is the rate of change of current with respect to time.

* Inductance are in series



⇒ Here L_1 and L_2 are connected in series and the current flowing is I . Due to current flowing the flux are produced in both the inductors.

⇒ As both the inductors are closely coupled, so flux L_1 links with inductor L_2 and induces an emf, similarly vice versa, so emf induced;

$$\epsilon_{L_1} = -L_1 \frac{dI}{dt}$$

$$\epsilon_{L_2} = -L_2 \frac{dI}{dt} \quad \left\{ \begin{array}{l} \text{self-inductance emf} \\ (\epsilon_{L_1} \text{ and } \epsilon_{L_2}) \end{array} \right.$$

⇒ EMF induced in ϵ_1

$$\epsilon_{m_1} = -M \frac{dI}{dt} \quad \left(\text{mutual induced emf in } L_1 \right)$$

⇒ EMF induced in ϵ_2 ;

$$\epsilon_{m_2} = -M \frac{dI}{dt} \quad \left(\text{mutual induced emf in } L_2 \right)$$

⇒ Here M is the co-efficient of mutual induction.

⇒ Total applied voltages

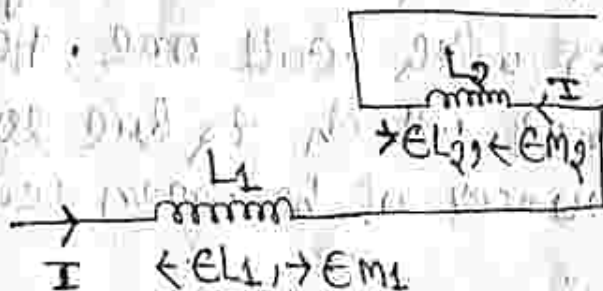
$$\Rightarrow \epsilon = \epsilon_{L1} + \epsilon_{L2} + \epsilon_{m1} + \epsilon_{m2}$$

$$\Rightarrow -L \frac{dI}{dt} = \left(-L_1 \frac{dI}{dt}\right) + \left(-L_2 \frac{dI}{dt}\right) + \left(-m \frac{dI}{dt}\right) + \left(-m \frac{dI}{dt}\right)$$

$$\Rightarrow -L = -L_1 - L_2 - m - m$$

$$\Rightarrow \boxed{L = L_1 + L_2 + 2m}$$

* Inductance are in series opposition



⇒ In case of series opposition the mutual induced emf in both the case oppose the self induced emf. As the direction of current in both the inductor are opposite.

$$\text{Hence: } \epsilon_{L1} = -L_1 \frac{dI}{dt}, \quad \epsilon_{m1} = m \frac{dI}{dt}$$

$$\epsilon_{L2} = -L_2 \frac{dI}{dt}, \quad \epsilon_{m2} = m \frac{dI}{dt}$$

⇒ Total induced emf;

$$\Rightarrow \epsilon = \epsilon_{L1} + \epsilon_{L2} + \epsilon_{m1} + \epsilon_{m2}$$

$$\Rightarrow -L \frac{dI}{dt} = \left(-L_1 \frac{dI}{dt}\right) + \left(-L_2 \frac{dI}{dt}\right) + \left(m \frac{dI}{dt}\right) + \left(m \frac{dI}{dt}\right)$$

$$\Rightarrow -L = -L_1 - L_2 + M + M$$

$$\Rightarrow -L = -L_1 - L_2 + 2M$$

$$\Rightarrow \boxed{L = L_1 + L_2 - 2M}$$

* ~~Mutual Inductance~~

* Mutual Inductance \Rightarrow If two coils are placed nearer to each other (closely coupled) then flux of the coil one links with coil two or more simultaneously flux of coil two links with coil one. Hence an emf is induced, which is due to the mutual inductance of between the two coils.

* Co-efficient of coupling \Rightarrow

\Rightarrow It is denoted by 'k'. It is defined as the fraction of total flux that links with other coil or the ratio of mutual inductance actually present between the two coils to the maximum possible flux.

$$\text{So } \Rightarrow \boxed{k = \frac{\phi_{12}}{\phi_{11}} \text{ (for coil-1)}}$$

$$\Rightarrow \boxed{k = \frac{\phi_{21}}{\phi_{22}} \text{ (for coil-2)}}$$

As ϕ_{12} and ϕ_{21} are less than ϕ_{11} and ϕ_{22} ; \therefore
 the value of K is less than 1. i.e. ($K < 1$).

We know that ; $M = N_1 \frac{d\phi_{21}}{dI_2}$

$$\Rightarrow M = N_1 \frac{\phi_{21}}{I_2} \rightarrow \textcircled{1}$$

Similarly ; again ; $M = N_2 \frac{d\phi_{12}}{dI_1}$

$$\Rightarrow M = N_2 \frac{\phi_{12}}{I_1} \rightarrow \textcircled{2}$$

∴ multiplying eqn $\textcircled{1}$ and $\textcircled{2}$ we get

$$\Rightarrow M^2 = N_1 \frac{\phi_{21}}{I_2} \times N_2 \frac{\phi_{12}}{I_1}$$

$$\Rightarrow M^2 = N_1 \cdot N_2 \frac{\phi_{21}}{I_2} \cdot \frac{\phi_{12}}{I_1}$$

$$\Rightarrow M^2 = K^2 \left(\frac{N_1 \phi_{11}}{I_1} \right) \cdot \left(\frac{N_2 \phi_{22}}{I_2} \right)$$

$$\Rightarrow M^2 = K^2 \cdot L_1 \cdot L_2$$

$$\Rightarrow M = K \sqrt{L_1 \cdot L_2}$$

Here ; $\Rightarrow \partial L_1 = -L_1 \frac{\partial I_1}{\partial I}$; $\partial L_2 = -N_2 \frac{\partial \phi_{11}}{\partial I}$

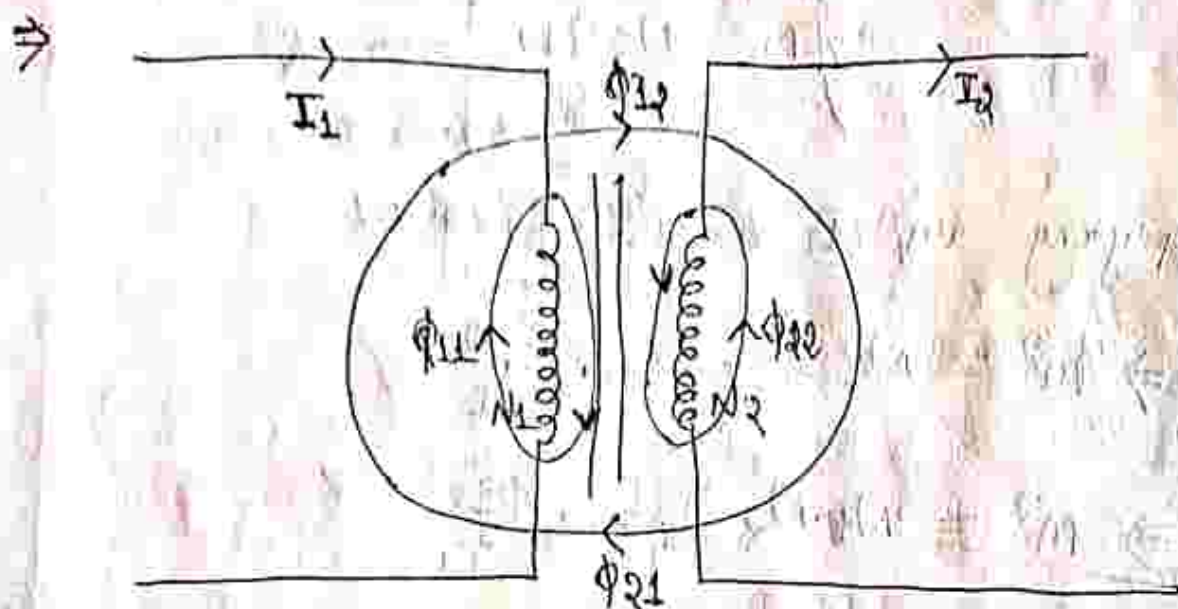
$$\Rightarrow -L_1 \frac{\partial I_1}{\partial I} = -N_1 \frac{\partial \phi_{11}}{\partial I}$$

$$\Rightarrow L_1 = N_1 \frac{d\phi_{11}}{dI_1} = N_1 \frac{\phi_{11}}{I_1}$$

∴ Similarly,

$$\Rightarrow L_2 = N_2 \frac{d\phi_{22}}{dI_2}$$

$$= N_2 \frac{\phi_{22}}{I_2}$$



⇒ Here, coil-1 & coil-2 are closely coupled.

Let I_1 = AC current flows through coil-1.

I_2 = AC current flows through coil-2.

⇒ ϕ_{11} = self leakage flux of coil-1.

⇒ ϕ_{22} = self leakage flux of coil-2.

⇒ ϕ_{12} = mutual leakage flux of coil-1 links with coil-2.

$\Rightarrow \phi_{21}$ = mutual flux of coil-2 links with coil-1.

$\Rightarrow N_1$ = NO. of turns of coil-1.

$\Rightarrow N_2$ = NO. of turns of coil-2.

$\Rightarrow \mathcal{E}M_1$ = EMF induced in coil-1 due to flux coil-2.

$$\Rightarrow \mathcal{E}M_1 = -N_1 \frac{d\phi_{21}}{dt} \quad \text{--- (1)}$$

again, $\Rightarrow \mathcal{E}M_2 = -N_2 \frac{d\phi_{12}}{dt} \quad \text{--- (2)}$

Equating both the equations,

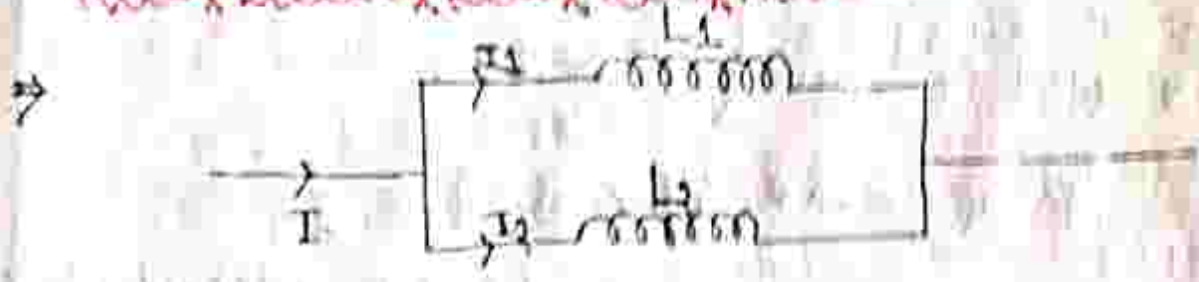
$$\Rightarrow -N_1 \frac{d\phi_{21}}{dt} = -N_2 \frac{d\phi_{12}}{dt}$$

$$\Rightarrow M = N_1 \frac{d\phi_{21}}{dI_2}$$

Similarly, for the 2nd coil,

$$M = N_2 \frac{d\phi_{12}}{dI_1} \quad (\text{By taking } \mathcal{E}M_2)$$

* Inductance are in parallel



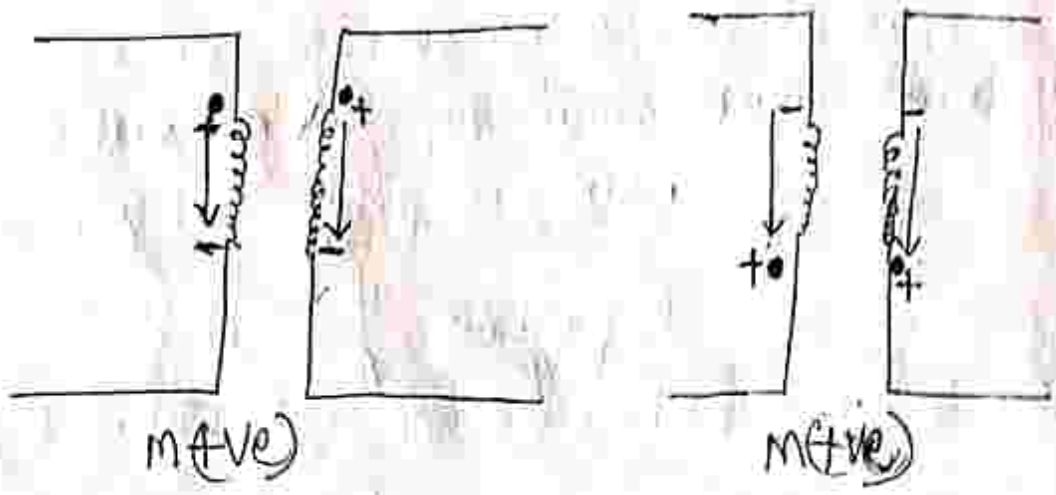
⇒ When; L_1 and L_2 are parallel coils and direction of current flow I_1, I_2 is in the same direction

$$L = \frac{L_1 L_2 - M^2}{L_1 + L_2 - 2M}$$

⇒ If the current direction is opposite then;

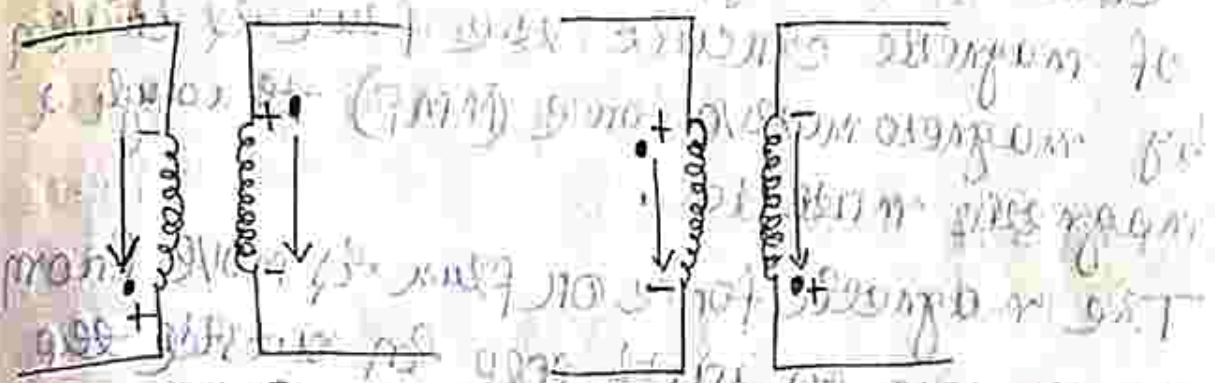
$$L = \frac{L_1 L_2 - M^2}{L_1 + L_2 + 2M}$$

* **Dot convention** → To determine polarity of induced voltage in the coupled coil, we use dot convention. According to the polarity of induced emf in the coil dot marks must be given. On each coil a dot is placed at the terminal which are instantaneously same polarity on the basis of mutual inductance.



⇒ on the basis of dot convention we decided the value of M i.e. either +ve or -ve.

⇒ when the current through each of the mutual coupled coils are going away or going towards the dot then in both the case M is +ve.



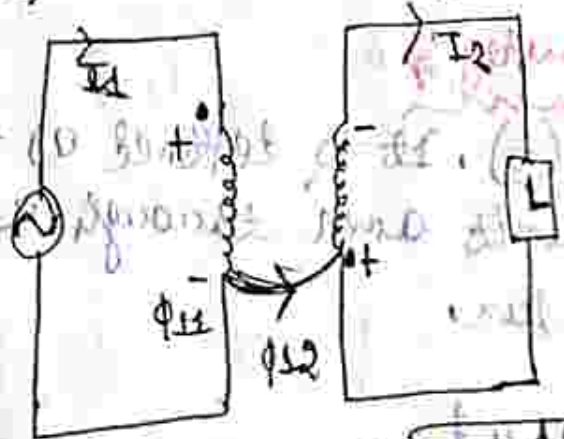
$M(+ve)$

$M(+ve)$

⇒ When the current flowing through the two coils either leaving the dot in 1 coil and about to enter in others coil and vice-versa then in both the case mutual inductance (M) is (-ve).

⇒ Hence the dot point is given on both the coils of same polarity.

+ dot convention is used in case of transformer, i.e. for example;



$$\Rightarrow -M \frac{dI_1}{dt}$$

* Magnetic Circuits \Rightarrow
 \Rightarrow The magnetic circuit is analogous to electrical circuit. The difference is that in case of electrical circuit the emf drives ~~the~~ current through a conductor whereas in case of magnetic circuit the flux is driven by magnetomotive force (MMF) through a magnetic material.

\Rightarrow The magnetic force or flux is move from north pole to south pole on outside the magnet whereas it moves from south poles to north poles inside the magnet.

* Magnetic Force \Rightarrow It is denoted by (H). It is defined as the strength of magnetic field at any point within a magnetic field is equal to the force experienced by an unit north pole of 1 weber placed at that point.

\Rightarrow Unit is Newton/webers.

* Magnetic Flux Density \Rightarrow

\Rightarrow It is denoted by (B). It is defined as the flux passing per unit area through a plane right angles to flux.

$$\text{So } B = \frac{\phi}{A} \text{ weber/m}^2$$

where $\phi \Rightarrow$ Total no. of flux strikes the plane

A \Rightarrow Area of cross-section of the plane.

* Relation between magnetic force and magnetic flux density (B and H) \Rightarrow

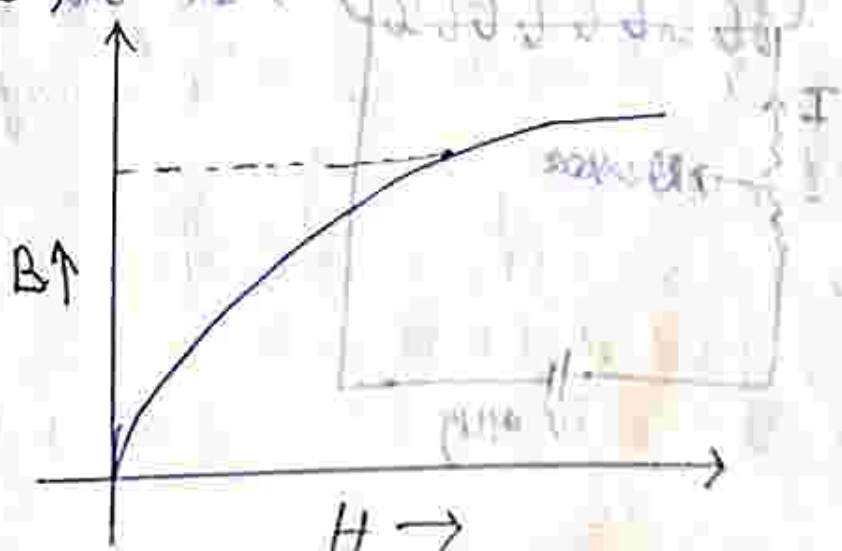
\Rightarrow It is seen that when a magnetic material get magnetised through a magnetic field then the material get magnetised and flux is produced.

\Rightarrow The flux travels through that material from one point to other point ($N \rightarrow S$) through that materials.

\Rightarrow As the flux is travels that material having certain cross-sectional area, hence flux density be seen across that materials.

\Rightarrow If we increase the magnetising force as, we see that the flux density (B) across the material is also be increases.

\Rightarrow This variation of flux density with magnetising force is upto point of saturation (if magnetising force increases flux density also increases upto point of saturation). After of saturation if further magnetising force increases the flux density remains constant, the variation is just like a straight-line.



→ The flux density (B) and the magnetic force a variation of depends upon types of material. So, according to the variation the materials are of three types. They are →

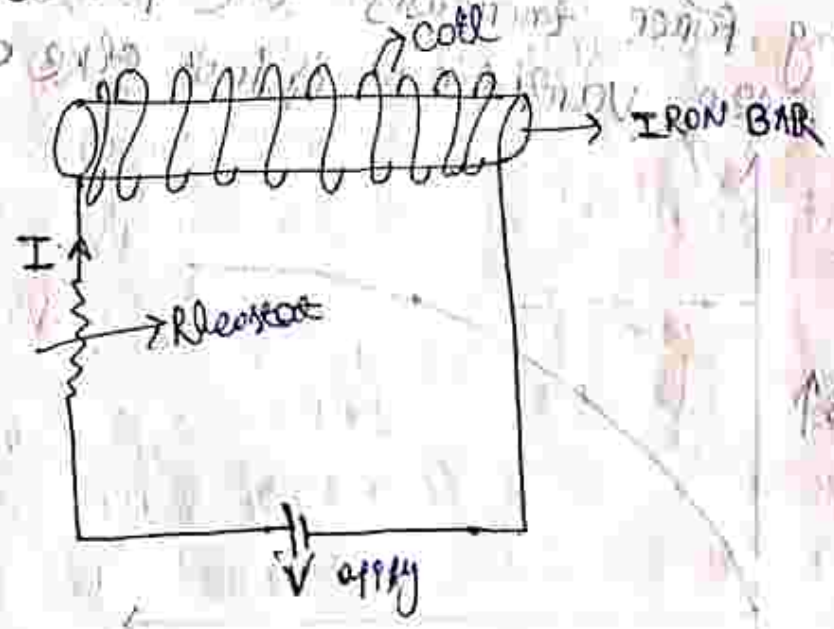
1. Ferro magnetic materials.
2. Dia magnetic materials.
3. Para magnetic materials.

→ The B-H curve holds better in case of ferro magnetic materials.

* Hysteresis Loop →

→ According to B-H characteristics of material we see that there are three types of material i.e. ferro, para, dia magnetic. Among these ferro-magnetic materials is substantially show magnetic behaviour. So a ferro-magnetic material should be taken for study B-H characteristics.

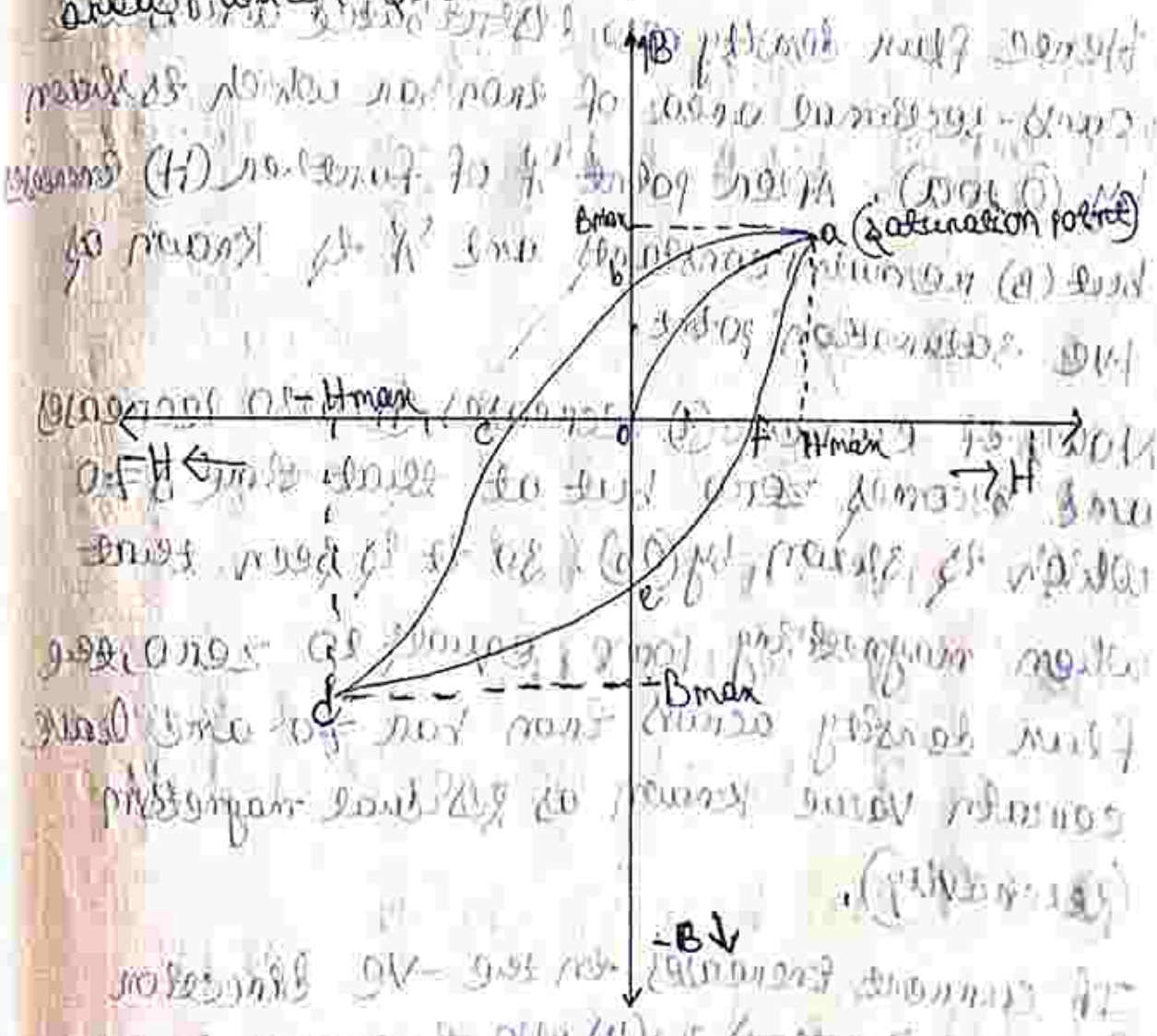
Let us consider an iron bar A.



⇒ Here, iron bar is wound by a coil having several no. of turns. A supply voltage is fed by means of a rheostat to control the current flow through the coil.

⇒ When current flow through the coil producing a magnetising force as creates and which magnetised the iron bar.

⇒ As iron bar has certain cross-sectional area so flux density distribution occurs inside the iron bar. The magnetic flux travels within the certain cross-sectional area, which shows a behaviour.



Notes: The graph shows the relationship between magnetic field strength (H) and magnetic flux density (B). The curve starts at the origin (0,0) and rises to a point 'a' labeled 'saturation point'. From point 'a', a vertical dashed line goes down to the x-axis at point 'b'. A horizontal dashed line goes from point 'a' to the y-axis at point 'c'. The y-axis is labeled 'B' at the top and '-Bmax' at the bottom. The x-axis is labeled 'H' at the right and '-Hmax' at the left. The origin is marked with '0'. The curve is symmetric about the origin, forming a loop.

⇒ Hysteresis produced about lagging of flux density (B) behind the magnetising force (H).
So hysteresis loop may be defined as lagging of magnetic flux density (B) behind the magnetising force (H) which is shown in figure.

⇒ By varying the rheostat (R) the current through coil ϕ vary. So magnetising force also vary. If current increases then magnetising force also increases and when magnetised iron bar.

⇒ Hence flux density also distributed across the cross-sectional area of iron bar which is shown by (a). After point X of further (H) increase but (B) remains constant and X is known as the saturation point.

⇒ Now, if current (I) decreases, (H) also decreases and becomes zero but at that time $B \neq 0$ which is shown by (b). So it is seen that when magnetising force equals to zero, the flux density across iron bar $\neq 0$ and has certain value known as residual magnetism (Retentivity).

⇒ If current increases in the -ve direction (reverse direction) so (H) also increases in the -ve direction (opposite direction) and when

$H = 0$ or $B = 0$ are known as
 D-magnetizing force of magnetic materials.

→ Now, if function (H) increases in the positive direction (B) also increases in the positive direction which is shown by 'c'd' and other points - d, if function (H) increases (B) remains constant so (d) is known as -ve saturation point.

⇒ If further the current direction is changed i.e. flow as that of previous one then H and B both vary and when $H = 0$, $B = 0$ known as negative residual magnetism or -ve retentivity.

⇒ If further (H) increases (B) also vary and when $H = 0$, $B = 0$ and the variation is shown by 'e' and 'f'.

⇒ If these points are joined (a,b,c,d,e,f) then it is seen like loop known as hysteresis loop.

$$B = \mu_0(H + I) = \mu_0 H + \mu_0 I$$

$$B = \mu_0 H + \mu_0 I$$

$$0 = \mu_0 H + \mu_0 I \Rightarrow H = -I$$

$$0 = \mu_0 H + \mu_0 I$$

$$0 = \mu_0 H + \mu_0 I$$

$$0 = \mu_0 H + \mu_0 I$$

$$0 = \mu_0 H + \mu_0 I$$