

LECTURE NOTES
ON
THEORY OF MECHANICS
4TH SEMESTER,
(MECHANICAL ENGINEERING)



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Machine

- Machine is any thing that produces human effort.
- It is the combination of various no. of kinematic links/pairs which have relative motion between them.
- A machine receives some energy & convert it into some useful work. A machine is any thing that is use to do some useful work by receiving some work.

Machine

- Parts of the machine having relative motion between them.
- Parts are known as kinematic link.
- Parts are always in motion.

Structure

- Parts of the structure don't having any motion bet. them.
- Parts are also known as link.

Rigid body

- one body which doesn't deform by applying force, this known as rigid body.
- In actual & in practical there is no rigid body.

Resistant body

- one body which deform by applying force is known as resistant body.
- If the deformation is negligible then it will be used for precision work.

Kinematic Link

- one parts of the machine which have relative motion they are known as kinematic pair.

types of link

- ① Rigid link
- ② flexible link
- ③ fluid link

① Rigid link

when there is no relative motion between the links is known as rigid body

② flexible link

when there are some relative motion between the link then it is known as flexible link.

③ fluid link

when a link comes in contact with a fluid having some relative motion between them is called fluid link

kinematic pairs

when the motion is restricted to a different area

they are 3 types

- ① completely constrained motion
- ② incompletely constrained motion
- ③ successfully constrained motion

Types of kinematic pairs

- 1) sliding pair - lower pair
- 2) rolling pair
- 3) turning pair
- 4) screw pair
- 5) spherical pair

According to the point of contact

- 1) lower pair (surface contact)
- 2) higher pair (point line contact)

1) lower pair
When the two elements of a kinematic pair have a surface contact between them then it is known as lower pair.

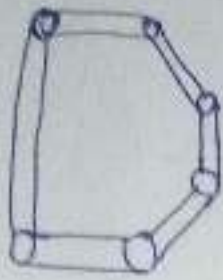
2) higher pair
Ex: cam & follower.
According to the connection:

- 1) self closed
- 2) force closed

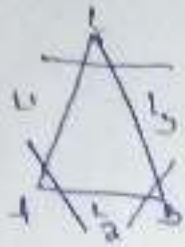
1) self closed
When the elements are connected mechanically to obtain the definite relative motion is known as self closed kinematic pair.

2) force closed
When the elements are not connected mechanically then it is known as force closed.

Kinematic chain



LHS < RHS is unconstrained kinematic chain
 LHS = RHS is constrained kinematic chain
 LHS > RHS is locked chain



Link = 3
 Joint = 3
 Pairs = 3

$$L = 2P - 4$$

$$3 = 2 \cdot 3 - 4$$

$$\Rightarrow 3 = 2$$

$$3 > 2$$

$$\text{LHS} > \text{RHS}$$

$$D = \frac{3}{2} L - 2$$

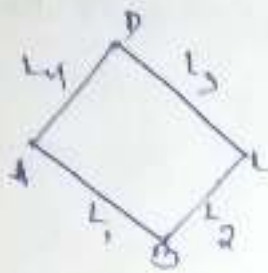
$$3 = \frac{3}{2} \times 3 - 2$$

$$3 = 4.5 - 2$$

$$3 = 2.5$$

$$3 > 2.5$$

$$\text{LHS} > \text{RHS}$$



L = 4
 P = 4
 T = 4

$$L = 2P - 4$$

$$\Rightarrow 4 = 2 \times 4 - 4$$

$$\Rightarrow 4 = 8 - 4$$

$$\Rightarrow 4 = 4 \text{ i.e. LHS} = \text{RHS}$$

Compound kinematic chain

A chain having more than 4 links is known as compound kinematic chain.

Types of joint

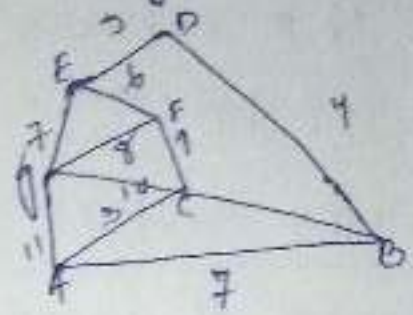
- (1) Binary joint
- (2) Quaternary joint
- (3) Ternary joint

Binary joint

When 2 links are joint at the same connection the joint is known as binary joint.

b) Quaternary joint
 when 4 links are connected at the joint is called

quaternary joint at the same connection



c) ternary joint

when 3 links are joint at the same connection the joint is known as ternary joint.



$L = 9$
 $L = 6$
 $J = 5$

$L = 2r - 4$
 $b = 2 \times 9 - 4$
 $b = 14$
 $b < 14$

$J = \frac{3}{2} L - 2$
 $J = \frac{3}{2} \times 6 - 2$
 $J = 7$

Mechanism

- i) when one of the links of a kinematic chain is fixed when it is known as mechanism.
- ii) when a mechanism is used to do some definite work it is called as machine.
 ex: engine, indicators, type-writer.
- iii) A mechanism with links is known as simple mechanism.
- iv) A mechanism with more than 4 link called compound mechanism.

Degree of Freedom

↳ The maximum no. of independent movement of the links of a kinematic chain mechanism is known as degree of freedom.

Grubler's conditions for plane mechanism

↳ It applies to mechanism with only single degree of freedom.

$$n = 0, n = 1$$

$$1 = 3(1-1) - 2(0) = 0$$

$$1 = 3(2-3) - 2(1)$$

$$= \boxed{2L - 2P - 4 = 0}$$

Conversion

The process of obtaining various mechanism by fixed various link of a kinematic chain by inversion.

Types of kinematic chain

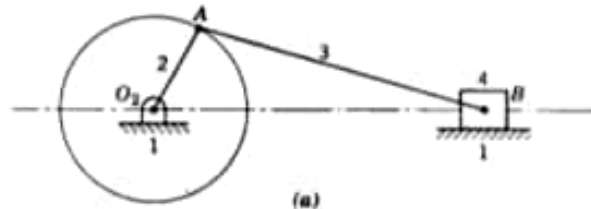
Four bar chain or quadrilateral chain

(i) single slider crank chain

(ii) double slider crank chain

Inversions of Single Slider Chain

Slider crank chain: This is a kinematic chain having four links. It has one sliding pair and three turning pairs. Link 2 has rotary motion and is called crank. Link 3 has got combined rotary and reciprocating motion and is called connecting rod. Link 4 has reciprocating motion and is called slider. Link 1 is frame (fixed). This mechanism is used to convert rotary motion to reciprocating and vice versa.

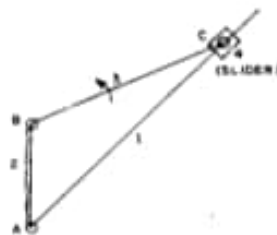


(a)

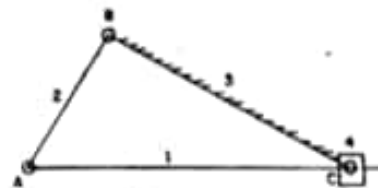
Fig1.27

Inversions of slider crank chain

Inversions of slider crank mechanism is obtained by fixing links 2, 3 and 4.



(a) crank fixed



(b) connecting rod fixed



(c) slider fixed

Fig.1.28

Quick return motion mechanisms.

Quick return mechanisms are used in machine tools such as shapers and power driven saws for the purpose of giving the reciprocating cutting tool a slow cutting stroke and a quick return stroke with a constant angular velocity of the driving crank.

Whitworth quick return motion mechanism–Inversion of slider crank mechanism.

This mechanism is mostly used in shaping and slotting machines. In this mechanism, the link CD (link 2) forming the turning pair is fixed, as shown in Fig. The link 2 corresponds to a crank in a reciprocating steam engine. The driving crank CA (link 3) rotates at a uniform angular speed. The slider (link 4) attached to the crank pin at A slides along the slotted bar PA (link 1) which oscillates at a pivoted point D . The connecting rod PR carries the ram at R to which a cutting tool is fixed. The motion of the tool is constrained along the line RD produced, *i.e.* along a line passing through D and perpendicular to CD .

① Screw Friction

Screw is a fastening that have thread which have made by cutting a continuous helical groove on a cylindrical surface.

② Ex: - v-thread, square thread etc.

Types of thread

① External

② Internal

∴ If the threads are cut on the outer surface of a rod on cylindrical surface is known as external thread.

Ex: Bolt.

Internal

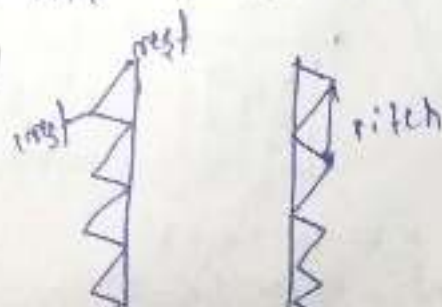
① The threads are cut on the internal surface then it is called internal thread.

② Nut

Various terms use in screw friction

① Helix
It is the curve cut by a point while describing a circular path.

2- pitch
It is the distance between one point of a screw to the adjacent next point

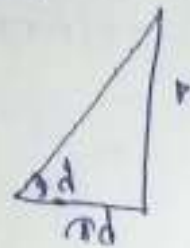


③ Lead
The axial distance travel by a screw one turn is known as lead.

④ Depth of thread
The distance between crest of crest is called as POF.

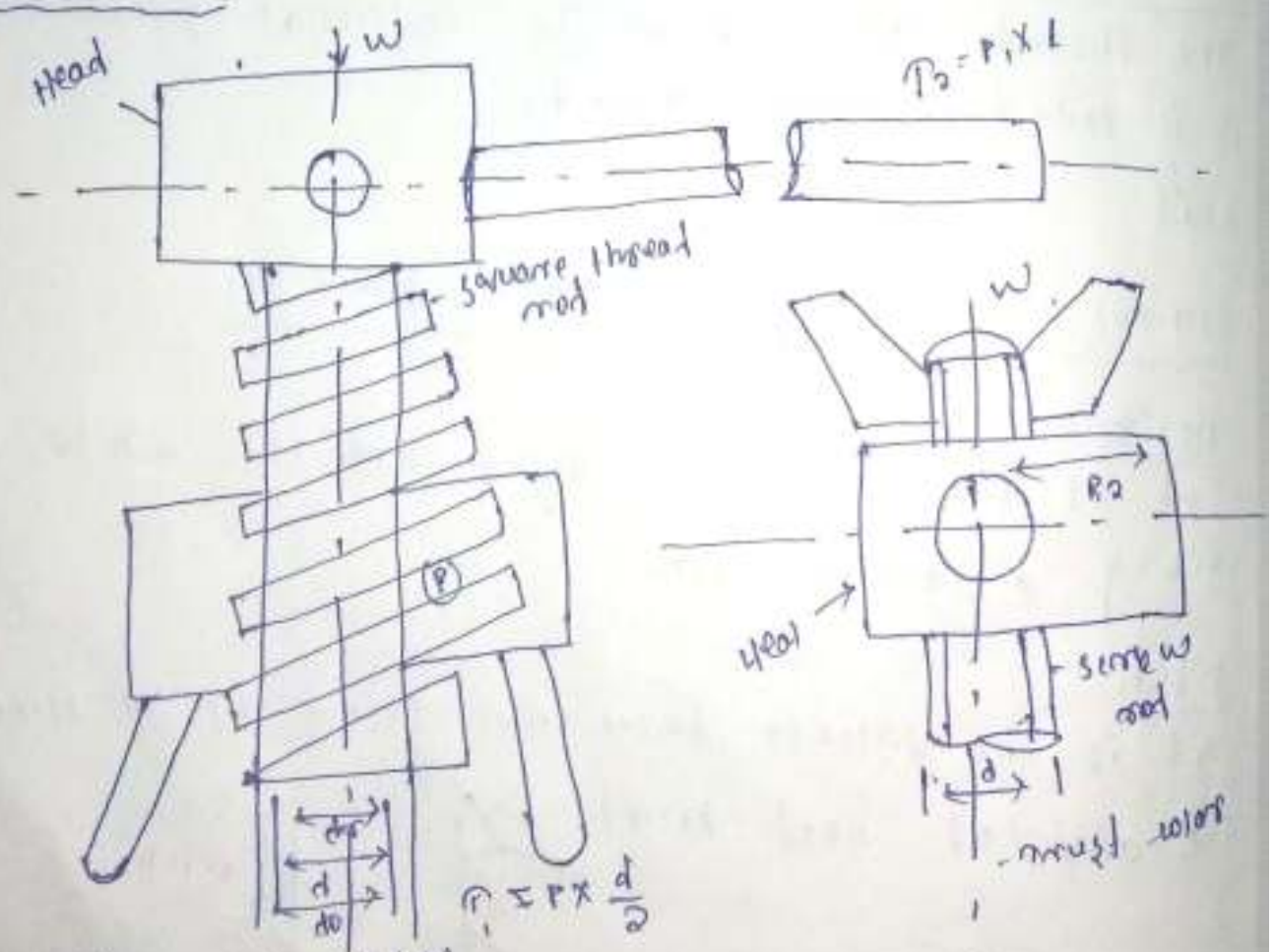
⑤ Single thread screw
If the lead of the screw is equal to its pitch, it is known as single thread screw.

⑥ Helix angle
It is the slope of the thread the horizontal



$$\text{Pitch } \tan \alpha = \frac{1}{\pi d}$$

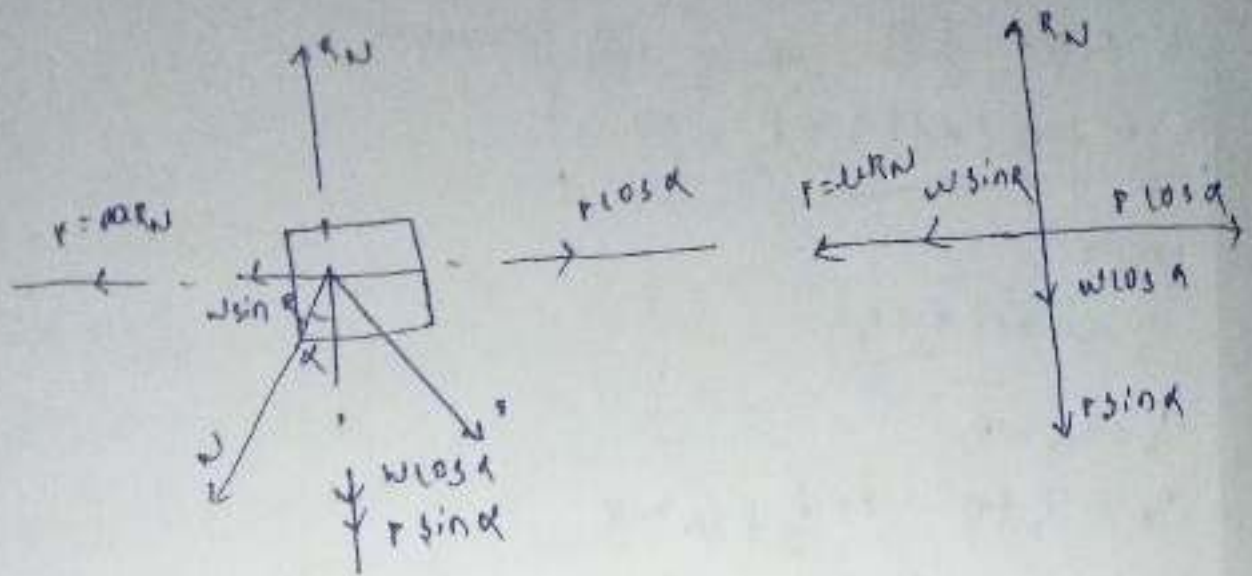
screw rack



upward = $w \tan (\alpha + \theta)$
downward = $w \tan (\alpha - \theta)$

Free body diagram

(3)



$$\sum V = 0$$

$$R_N - W \cos \alpha - P \sin \alpha = 0$$

$$R_N = W \cos \alpha + P \sin \alpha \rightarrow (1)$$

$$\sum H = 0$$

$$P \cos \alpha - F - W \sin \alpha = 0$$

$$P \cos \alpha = F + W \sin \alpha$$

$$\Rightarrow P \cos \alpha = \mu \cdot R_N + W \sin \alpha \rightarrow (2)$$

Put the value of \$R_N\$ in eq (2)

$$P \cos \alpha = \mu \cdot (W \cos \alpha + P \sin \alpha) + W \sin \alpha$$

$$\Rightarrow P \cos \alpha = \mu W \cos \alpha + \mu P \sin \alpha + W \sin \alpha$$

$$\Rightarrow P \cos \alpha - \mu P \sin \alpha = \mu W \cos \alpha + W \sin \alpha$$

$$\Rightarrow P (\cos \alpha - \mu \sin \alpha) = W (\mu \cos \alpha + \sin \alpha)$$

$$\Rightarrow P = \frac{W (\mu \cos \alpha + \sin \alpha)}{(\cos \alpha - \mu \sin \alpha)}$$

$$\Rightarrow P = \frac{W \sin (\alpha + \theta)}{\cos (\alpha + \theta)}$$

$$\Rightarrow P = \frac{W (\cos \alpha \times \frac{\sin \theta}{\cos \theta} + \sin \alpha)}{\cos \alpha - \frac{\sin \theta}{\cos \theta} \times \sin \alpha}$$

$$\Rightarrow \boxed{P = W \tan (\alpha + \theta)}$$

$$\Rightarrow P = \frac{W (\cos \alpha \times \sin \theta + \sin \alpha \times \cos \theta)}{\cos \alpha \times \cos \theta - (\sin \alpha \times \sin \theta)}$$

$$\frac{W (\cos \alpha \times \cos \theta + \sin \alpha \times \sin \theta)}{\cos \alpha \times \cos \theta - (\sin \alpha \times \sin \theta)}$$

$$\tau_1 = P \times \frac{d}{2} \rightarrow (1) \quad \tau_1 = \frac{P d}{2} \rightarrow (2)$$

$$\tau_2 = P_1 \times R \rightarrow (3) \quad \tau_2 = \tau_3 \rightarrow (4)$$

$$\tau_3 = W \tan(\alpha + \phi) \times \frac{d}{2} \rightarrow (5)$$

torque

Let us

$$\tau_3 = \mu_1 W \left(\frac{R_1 + R_2}{2} \right)$$

$$\tau_3 = \mu_1 W R$$

$$\tau_0 = \tau_1 + \tau_3 = P \times \frac{d}{2} + \mu_1 W R$$

$$= W \tan(\alpha + \phi) + \mu_1 W R$$

$$= W \{ \tan(\alpha + \phi) + \mu_1 R \}$$

Mechanical Advantages

$$M.A = \frac{W}{P_1} = \frac{W}{\frac{P d}{2}} = \frac{W 2L}{P d} = \frac{2L \mu_1}{W \tan(\alpha + \phi) \times d} = \boxed{\frac{2L}{\tan(\alpha + \phi) \times d}}$$

$$V.R = \frac{\text{Distance moved by the effort}}{\text{Distance moved by the load}}$$

$$= \frac{2\pi L}{\text{pitch}} = \boxed{\frac{2\pi L}{\tan \alpha \times \text{pitch}}}$$

$$\therefore \frac{2L}{\tan(\alpha + \phi) \times d} = \frac{2L}{\tan \alpha \times \text{pitch}} \times \frac{\tan \alpha \times \text{pitch}}{\tan(\alpha + \phi) \times d}$$

$$= \frac{\tan \alpha}{\tan(\alpha + \phi)}$$

(1) An electric motor driven power screw moves a nut in a horizontal plane against a force of 75 kN at a speed of 300 rpm. The screw has single thread of 6 mm pitch on a measure diameter of 40 mm. The coefficient of friction is 0.1. Estimate the power of motor.

Given

$$W = 75 \text{ kN} = 75 \times 10^3 \text{ N}$$

$$\text{pitch } h = 6 \text{ mm}$$

$$d_o = 40 \text{ mm}$$

$$\mu = 0.1$$

$$v = 300 \text{ mm/min}$$

$$d_m = d_o \cdot \frac{1}{2}$$

$$\tan \alpha = \frac{p}{\pi d} = \frac{6}{\pi \times 37}$$

$$\Rightarrow \tan \alpha = 0.0516$$

$$\text{axial force } P = W \tan(\alpha + \phi)$$

$$W \times \left(\frac{\tan \alpha + \tan \phi}{1 - \tan \alpha \times \tan \phi} \right)$$

$$= 75 \times 10^3 \times \left[\frac{0.0516 + 0.1}{1 - (0.0516 \times 0.1)} \right]$$

$$= 11428.97$$

$$= 11.428 \times 10^3 \text{ N}$$

Power = Torque \times angular velocity

$$P = T \times \omega$$

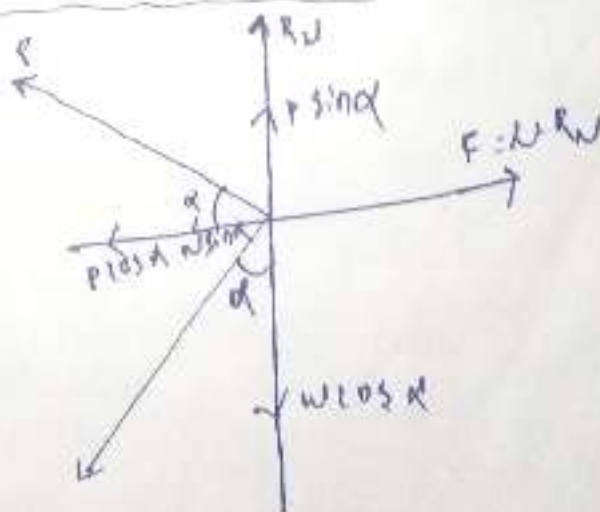
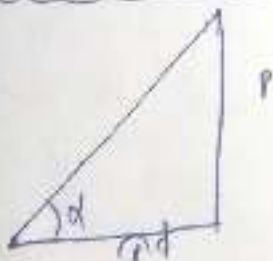
$$= 211.45 \text{ Nm} \times 5.24 \text{ rad/s}$$

$$= 1108 \text{ W} = 1.108 \text{ kW}$$

$$T = P \times \frac{d_m}{2} = 11.428 \times 10^3 \times \frac{37}{2} = 211.45 \text{ Nm}$$

$$\mu = \frac{v}{P} = \frac{\text{speed of nut}}{\text{pitch}} = \frac{300}{6} = 50$$

Torque required to lower the part



$$\sum V = 0$$

$$R_N + W \cos \alpha + P \sin \alpha$$

$$\rightarrow R_N = W \cos \alpha + W \sin \alpha$$

$$\sum H = 0$$

$$P \cos \alpha - W \sin \alpha = 0$$

$$P \cos \alpha = W \sin \alpha \rightarrow (1)$$

Putting the value of R_N in eq (1)

$$P \cos \alpha = W \sin \alpha$$

$$P \cos \alpha = W \sin \alpha - W \sin \alpha$$

$$\rightarrow P \cos \alpha = W \cos \alpha - W \sin \alpha$$

$$\rightarrow P (\cos \alpha + W \sin \alpha) = W (\cos \alpha - \sin \alpha)$$

$$\rightarrow P (\cos \alpha + W \sin \alpha) = W (\cos \alpha - \sin \alpha)$$

$$\rightarrow P = \frac{W (\cos \alpha - \sin \alpha)}{(\cos \alpha + W \sin \alpha)}$$

$$\rightarrow P = \frac{W (\cos \alpha \times \frac{\sin \alpha}{\cos \alpha} - \sin \alpha)}{\cos \alpha + \frac{\sin \alpha}{\cos \alpha} \times \sin \alpha}$$

$$\rightarrow P = \frac{W (\cos \alpha \times \sin \alpha - \sin \alpha)}{\cos \alpha}$$

$$\left(\cos \alpha + \frac{\sin \alpha - \sin \alpha}{\cos \alpha} \right)$$

$$\rightarrow P = \frac{W (\sin \alpha \times \cos \alpha - \sin \alpha \times \cos \alpha)}{\cos \alpha}$$

$$\frac{\cos \alpha \cdot \cos \alpha + \sin \alpha \cdot \sin \alpha}{\cos \alpha}$$

$$P \rightarrow W \frac{\sin (\alpha - \alpha)}{\cos (\alpha - \alpha)}$$

$$P = W \tan (\alpha - \alpha)$$

when $\alpha > \alpha$

Bearing

(7)

- Bearing provides an effective means of supporting rotating shaft while reducing friction.
- Bearings are mechanical assembly that consist of rolling elements & usually inner & outer races which are use for rotating linear shaft applications.

① There are various types of bearing

- Ball bearing
- Roller bearing
- Linear bearing
- Plane bearing

- ② Ball bearing have spherical rolling elements & are use for lower load application while roller bearing use cylindrical rolling elements for heavier load carrying applications.
- ③ Linear bearing are use for linear movement along shaft & may also have rotational capability.

Ball Bearing

- ① Ball bearing are mechanical assembly that consists of rolling spherical elements that are captured between inner & outer races. They provide a means of supporting rotating shaft & minimizing friction between shaft & stationary machine members.
- ② Ball bearing are also known as rolling element bearing or anti-friction bearing.

Advantage

- (i) use to support high speed shaft.
- (ii) large range of standard sizes.
- (iii) can handle radial & axial load with specific configuration.

Roller bearing

- (i) roller bearing are mechanical assembly that consists of cylindrical or tapered rolling element usually captured between inner & outer races.
- (ii) they provide a mean of separating rotating shaft & stationary machine members.
- (iii) they are used primarily in machinery with rotating shaft that requires the support of heavier load than ball bearing provides.
- (iv) they are mostly pretensioned bars.
- (v) High load capacity than ball bearing.
- (vi) can with stand high axial load.

Friction in pivot & collar bearing

- (i) the rotating shaft are frequently subjected to axial thrusts. The bearing surface such as pivot & collar bearing are used to take the axial thrusts of the rotating shaft.

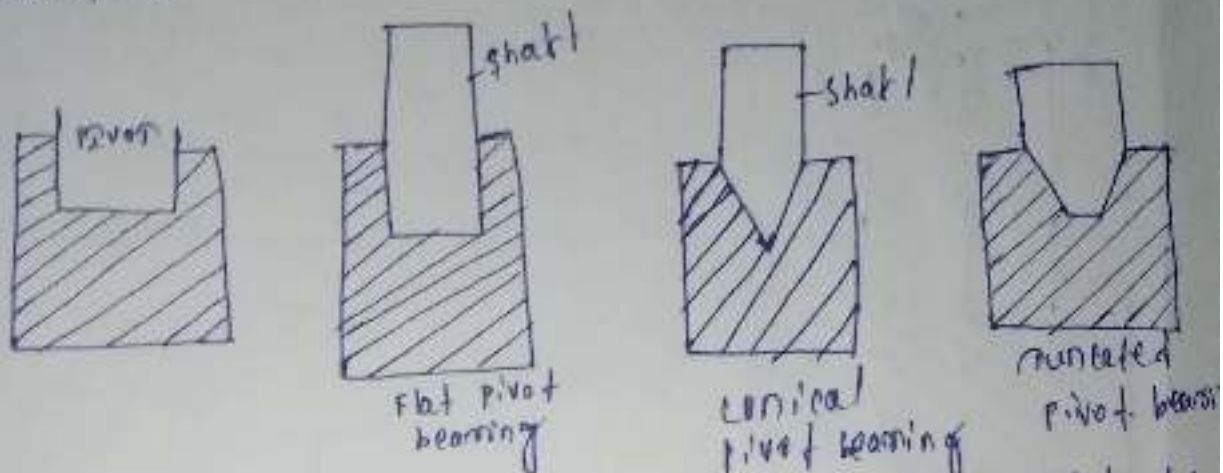
EX: The propeller of ships. The shaft of turbine etc.

- (ii) the bearing surface placed at the end of shaft to take the axial thrust are known as pivot

Types of bearing

Pivot
 flat pivot
 conical
 truncated

Collar
 single flat collar bearing
 multiple flat collar bearing



In a new bearing the contact between the shaft & bearing may be good over the whole surface. In other may be good over the whole surface. In other words we can say that the pressure over the rubbing surface is uniformly distributed.

But when the bearing becomes old all part of the rubbing surface will not move with the same velocity because the velocity of rubbing surface increases with the distance from the axis of bearing. Hence the continuous wear is generated through out the bearing surface.

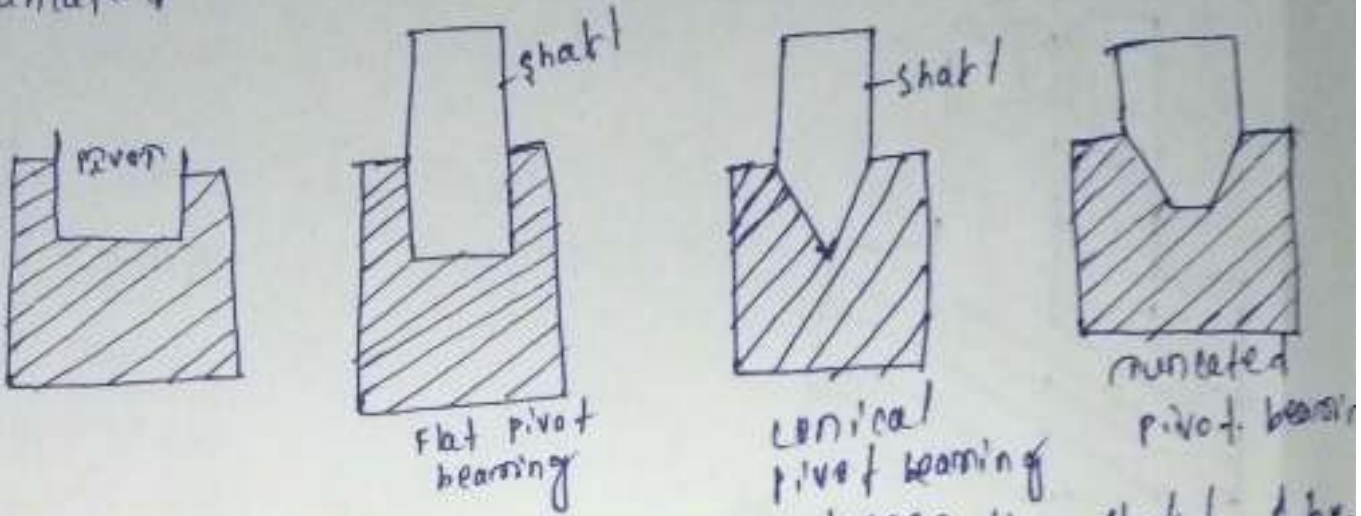
So the torque generated in the shaft & bearing can be found out considering uniform pressure & uniform wear.

Flat pivot bearing

- p = intensity of pressure per unit area of bearing surface
- w = load
- μ = coefficient of friction
- r = radius of small strip

pivot
 Flat pivot
 conical
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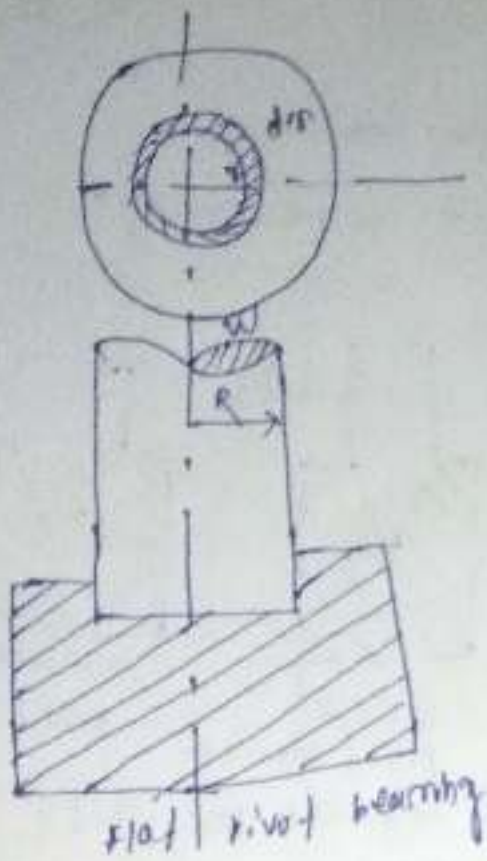
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So the torque generated in the shaft & bearing can be found out considering uniform pressure & uniform wear.

Flat pivot bearing

- p = intensity of pressure per unit area of bearing surface
- w = load
- μ = coefficient of friction
- r = radius of small strip



flat pivot bearing

considering uniform pressure

$$p = \frac{W}{A}$$

$$\Rightarrow p = \frac{W}{\pi R w} \rightarrow (1)$$

$$a = 2\pi R dr$$

$$p = \frac{W}{2\pi R w} \Rightarrow W = p \times 2\pi R w \rightarrow (2)$$

Frictional resistance generated on the ring

$$F_r = \mu \times W$$

$$= \mu \times p \times 2\pi R w$$

$$= 2\pi \mu p R w$$

Frictional torque generated on the ring

$$T_r = F_r \times R$$

$$= 2\pi \mu p R^2 w$$

$$= 2\pi \mu p R^2 w$$

total friction torque generated on the bearing

$$T = \int_0^w 2\pi \mu p R^2 w$$

$$T = \int_0^R 2\pi r \mu r^2 dr$$

$$= 2\pi \mu r \int_0^R r^2 dr$$

$$= 2\pi \mu r \left[\frac{r^3}{3} \right]_0^R$$

$$= 2\pi \mu r \frac{R^3}{3} = 2\pi \mu r \times \frac{W}{\pi R^2} \times \frac{R^3}{3} \Rightarrow \boxed{T = \frac{2}{3} \mu W R}$$

when the shaft rotate at ω radian per second
the power loss in bridle is

$$P = \text{Torque} \times \omega$$

$$P = T \times \omega$$

$$= \pi \times \frac{2\pi \mu}{60} \omega$$

considering uniform wear

$$r \times r = c$$

$$\Rightarrow r = \frac{c}{r} \rightarrow \omega$$

$$f_w = 2\pi r \omega dr$$

$$= \frac{c}{r} \times 2\pi \omega dr$$

$$\rightarrow f_w = 2\pi c \omega dr$$

$$\begin{aligned} \text{total load } W &= \int_0^R 2\pi c \omega dr \\ &= 2\pi c \omega \int_0^R dr \\ &= 2\pi c \omega R \\ \Rightarrow c &= \frac{W}{2\pi R} \rightarrow \text{②} \end{aligned}$$

$$F_T = 2\pi \mu r \omega dr$$

$$= 2\pi \mu r \times \frac{c}{r} \times \omega \times dr$$

$$= \boxed{2\pi \mu c \omega dr}$$

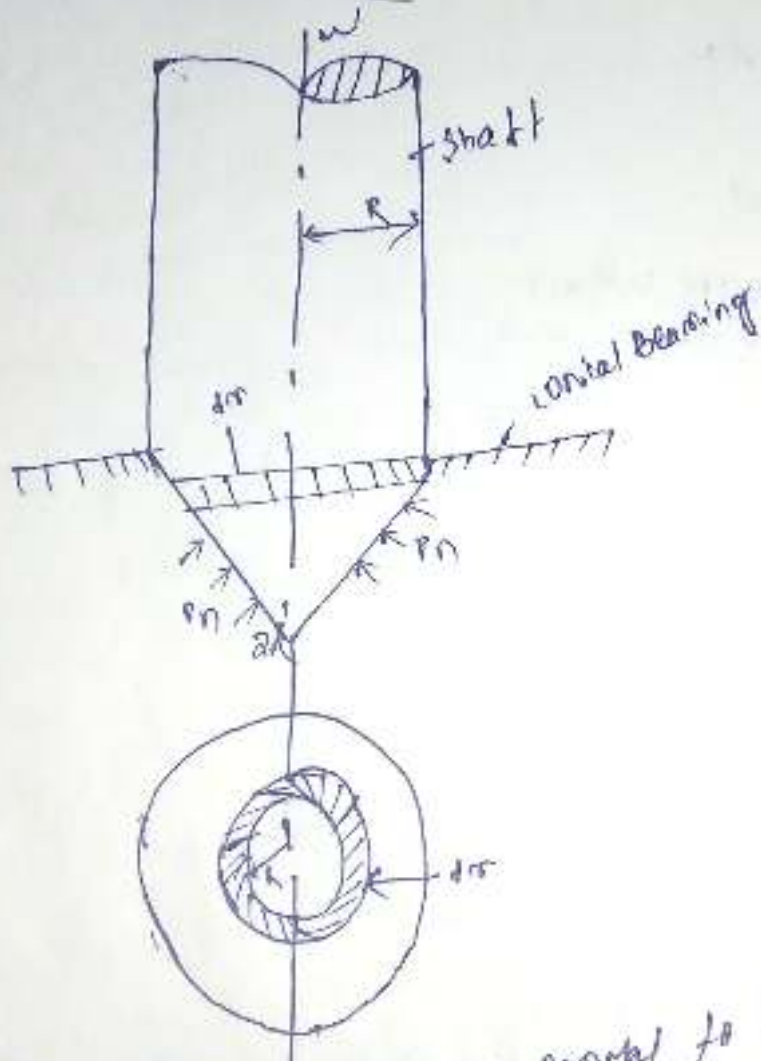
$$F_T = 2\pi \mu c \omega R$$

$$= \boxed{2\pi \mu c \omega R}$$

$$\begin{aligned}
 \text{total torque } T &= \int_0^R 2\pi r \mu \omega r dr \\
 &= 2\pi \mu \omega \int_0^R r^2 dr \\
 &= 2\pi \mu \omega \left[\frac{r^3}{3} \right]_0^R \\
 &= 2\pi \mu \omega \frac{R^3}{3}
 \end{aligned}
 \quad \left| \begin{aligned}
 &= 2\pi \times \mu \times \omega \times \frac{R^3}{3} \\
 &= \frac{1}{3} \mu \omega R^3
 \end{aligned} \right.$$

$$P = T \times \omega = \frac{2\pi \mu \omega R^3}{3} \times \omega$$

Conical pivot bearing



- p_n = Intensity of pressure normal to the cone.
 r = radius of strip
 R = radius of shaft
 W = load applied on the shaft
 dr = thickness of strip
 α = semi angle of the cone
 μ = coefficient of friction between shaft & bearing.

$$a = 2\pi r \times dl$$

$$= 2\pi r dr \cos \alpha \quad (\because dl = dr \cos \alpha)$$

$$\delta W = p_n \times a$$

$$= p_n \times 2\pi r dr \cos \alpha$$

total vertical load acting on the ring $\delta W =$ vertical component of δW_n

$$= \delta W_n \cdot \sin \alpha$$

$$= p_n \times 2\pi r dr \cos \alpha \times \sin \alpha$$

$$= p_n \times 2\pi r dr$$

total vertical load

$$\int_0^{\pi} p_n \times 2\pi r dr$$

$$= p_n \times 2\pi \int_0^{\pi} r dr$$

$$= p_n \times 2\pi \times \frac{R^2}{2}$$

$$W = p_n \pi R^2$$

$$\Rightarrow p_n = \frac{W}{\pi R^2}$$

frictional resistance

$$F_f = \mu \times \delta W$$

$$F_f = \mu \times p_n \times 2\pi r dr$$

$$\tau = F_f \times r = \mu \times p_n \times 2\pi r dr \times r = 2\pi \mu p_n r^2 dr$$

total torque $\tau = \int_0^{\pi} 2\pi \mu p_n r^2 dr \cos \alpha$

$$= 2\pi \mu p_n \cos \alpha \int_0^{\pi} r^2 dr$$

$$= 2\pi \mu p_n \cos \alpha \times \frac{R^3}{3}$$

$$= 2\pi \mu \times \frac{W}{\pi R^2} \times \cos \alpha \times \frac{R^3}{3}$$

$$= \frac{2}{3} \mu W R \cos \alpha$$

$$\tau = \frac{2}{3} \mu W R$$

$$P = \tau \times W = \frac{2\tau W R}{60}$$

Single Flat Collars bearing

$$R = r(r_1^2 - r_2^2)$$

$$r = \frac{w}{R} = \frac{w}{r(r_1^2 - r_2^2)}$$

$$\delta w = r R (r_1^2 - r_2^2) \rightarrow \textcircled{1}$$

$$r = 2\pi \mu r^2 dr$$

$$R = \int_{r_2}^{r_1} 2\pi \mu r^2 dr$$

$$= 2\pi \mu r \int_{r_2}^{r_1} r^2 dr$$

$$= 2\pi \mu r \left(\frac{r^3}{3} \right)_{r_2}^{r_1}$$

$$= 2\pi \mu r \frac{r_1^3 - r_2^3}{3}$$

$$= 2\pi \mu \times \frac{w}{r(r_1^2 - r_2^2)} \times \frac{r_1^3 - r_2^3}{3}$$

$$= \boxed{\frac{2}{3} \mu w \left(\frac{r_1^3 - r_2^3}{r_1^2 - r_2^2} \right)}$$

Uniform wear

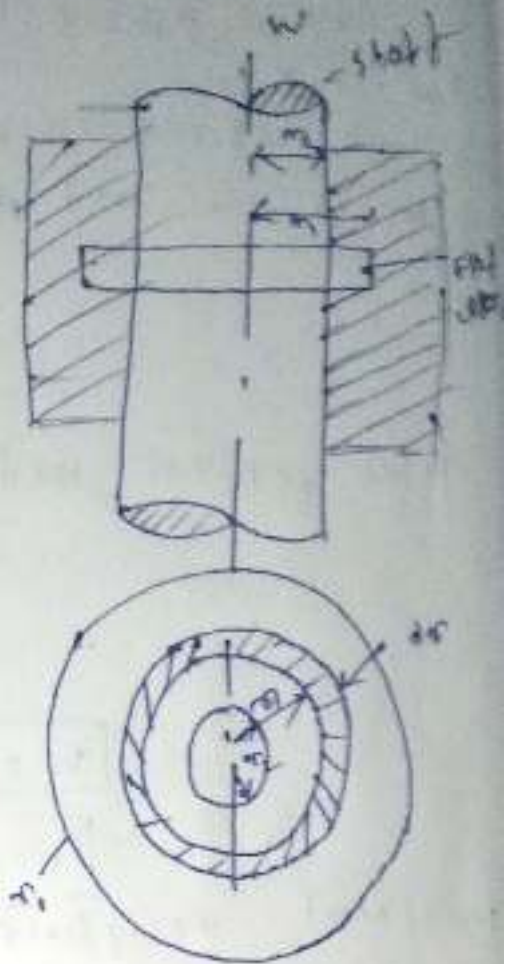
$$r \times r = c \rightarrow r = \frac{c}{r} \rightarrow \textcircled{1}$$

$$\delta w = P_r \times 2\pi r dr = \frac{c}{r} \times 2\pi r dr$$

$$= 2\pi c dr$$

$$= \int_{r_2}^{r_1} 2\pi c dr = 2\pi c \int_{r_2}^{r_1} dr = 2\pi c (r_1 - r_2)$$

$$\delta c = \frac{w}{2\pi (r_1 - r_2)} \rightarrow \textcircled{11}$$



$$r_1 = 2\pi u r dr$$

$$r = \int_{r_2}^{r_1} 2\pi u r dr$$

$$= 2\pi u \int_{r_2}^{r_1} r dr = 2\pi u \left[\frac{r^2}{2} \right]_{r_2}^{r_1}$$

$$= 2\pi u \left(\frac{r_1^2 - r_2^2}{2} \right)$$

$$= 2\pi u \times \frac{w}{2\pi(r_1 - r_2)} \times \frac{(r_1 + r_2)(r_1 - r_2)}{2}$$

$$r = \frac{w}{n\pi} (r_1^2 - r_2^2)$$

MULTIPLE COLLAR BEARING

Q. A shaft has a number of collars integral with it. The external diameter is 400 mm & shaft diameter 250 mm. The intensity of pressure is 0.35 N/mm² & coefficient of friction is 0.05. Find:

- (i) Power absorbed in the shaft runs 103 mm
- (ii) carrying about 150 kN.
- (iii) no. of collar.

Given

$$d_1 = 400 \text{ mm}, r_1 = \frac{1}{2} \times 400 = 200 \text{ mm}$$

$$\text{shaft } d_2 = 250 \text{ mm}, r_2 = \frac{1}{2} \times 250 = 125 \text{ mm}$$

$$p = 0.35 \text{ N/mm}^2$$

$$W = 150 \text{ kN}$$

$$\mu = 0.05$$

$$r = \frac{2}{3} \mu W \frac{r_1^3 - r_2^3}{r_1^2 - r_2^2}$$

$$= \frac{2}{3} \times 0.05 \times 150 \times 10^3 \times \frac{(200)^2 (125)^3}{(200)^2 (125)^2}$$

$$= 1240 \times 10^3 \text{ N}\cdot\text{mm}$$

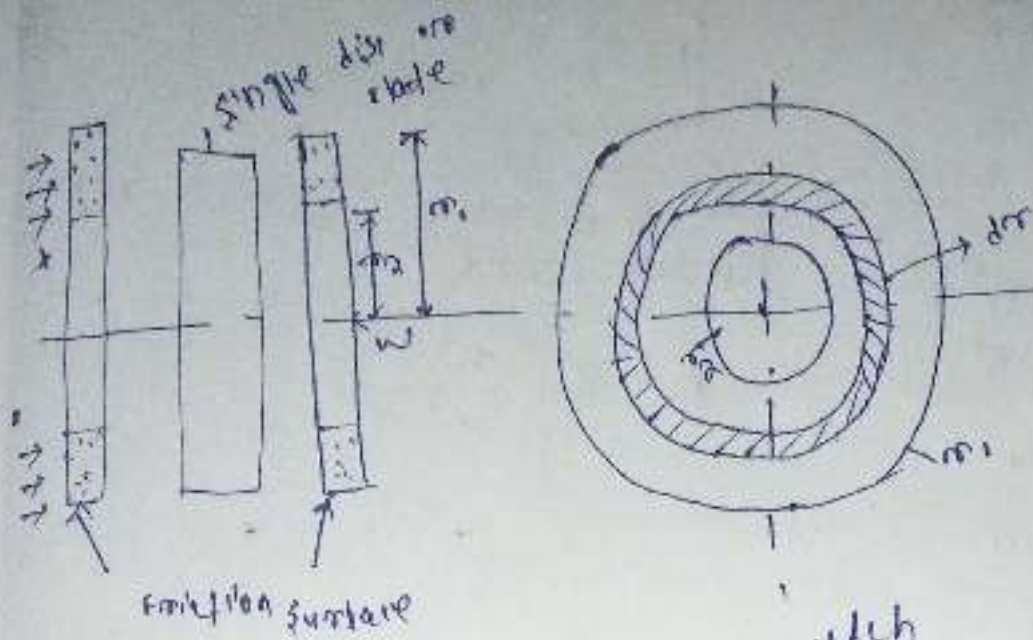
$$= 1240 \text{ N}\cdot\text{m}$$

$$T = \frac{2\pi NT}{60} = \frac{2\pi \times 105 \times 1240}{60} = 13640 \text{ W} = 13.64 \text{ kW}$$

$$r = \frac{W}{\pi \mu (r_1^2 - r_2^2)} = \frac{150 \times 10^3}{\pi \times 0.3 \times \pi \times (200^2 - 125^2)} = 5.6 \text{ mm [ans]}$$

Friction Clutch

- 1) It is used in the transmission of power of shaft machine where must be started, stopped frequently. It is also used to deliver power to the machines that is partially or fully loaded.
- 2) Friction clutch is used to connect the engine to driven shaft. In operation such a clutch can stop or be taken so that the friction surface engage gradually bringing the driven shaft up to proper speed.
- 3) Main types of clutch:
 - 1) Disk or plate clutch (single disk or multiple)
 - 2) cone clutch
 - 3) centrifugal clutch



T = torque transmitted by the clutch
 P = Intensity of pressure with which the contact surfaces are held together
 r_1 = external radius
 r_2 = internal radius
 w = coefficient of friction

- Area of the strip = $2\pi r_1 dr$ → (i)
- load applied on the strip $dW = P \times 2\pi r_1 dr$ → (ii)
- frictional resistance created in the strip.
 $F_f = \mu dW = \mu \times P \times 2\pi r_1 dr$ → (iii)
- Frictional torque applied on the strip
 $T_f = F_f \times r = \mu P \times 2\pi r_1 r dr$ → (iv)

total torque applied on the friction surface

$$T = \int_{r_2}^{r_1} 2\pi \mu P r^2 dr$$

$$= 2\pi \mu P \left[\frac{r^3}{3} \right]_{r_2}^{r_1}$$

$$= 2\pi r \left[\frac{m^3}{3} \right]_{r_2}^{r_1}$$

$$= 2\pi r \times \frac{w}{\pi(r_1^2 - r_2^2)} \times \frac{m^3}{3}$$

$$= \frac{2}{3} \pi w \left(\frac{m_1^3 - m_2^3}{m_1^2 - m_2^2} \right)$$

$$P = \frac{W}{A} = \frac{W}{\pi(m_1^2 - m_2^2)}$$

(8)

if R is mean radius of total
torque = $2\pi r$

$$R = \frac{2}{3} \left[\frac{m_1^3 - m_2^3}{m_1^2 - m_2^2} \right]$$

Uniform wear

$r_1 \times r_2 = \text{const}$

$\Rightarrow P_r = \frac{c}{r} \rightarrow (i)$

Area of shaft \times pressure applied \times radius = $m \times$ pressure applied \times radius
 $= \frac{1}{2} \times 2\pi r \times c \times r = \pi r^2 c$

total load $w = \int_{r_2}^{r_1} 2\pi r c \times r \times dr$

$= 2\pi c \left(\frac{r^3}{3} \right)_{r_2}^{r_1}$

$\Rightarrow w = \frac{2\pi c}{3} (r_1^3 - r_2^3)$

$\Rightarrow c = \frac{3w}{2\pi(r_1^3 - r_2^3)} \rightarrow (ii)$

$F_r = 2\pi r \times P_r$
 $= 2\pi r \times \frac{c}{r}$

$F_r = F_0 \times r = 2\pi r c \times r$
 $= 2\pi c r^2 \rightarrow (iii)$

total torque generated on the friction surface

$T = \int_{r_2}^{r_1} 2\pi r c r^2 \times dr$
 $= 2\pi c \left[\frac{r^4}{4} \right]_{r_2}^{r_1}$

$$= \frac{\pi \mu v w}{2b(r_1 - r_2)} \times \frac{\pi^2 r_1^2 r_2^2}{2}$$

$$= \frac{1}{2} \mu w \frac{(r_1 + r_2)(r_1 r_2)}{(r_1 - r_2)}$$

$$= \frac{1}{2} \mu w (r_1 + r_2)$$

$$P = \frac{r_1 + r_2}{2}$$

Frictional Break

It is a device by means of which artificial frictional resistance is applied to a moving machine member in order to decrease or stop motion of machine.

- (i) In this process the break absorbs either kinetic energy of moving members or potential energy given of hoists being lowered by hoists.
- (ii) The energy absorbed by breaks is dissipated in the form of heat.
- (iii) This heat is dissipated in the surrounding air or water, which is circulated through the passage.
- (iv) The capacity of a break depends upon the following factors:
 - (a) The unit pressure between the breaking surface.
 - (b) Coefficient of friction.
 - (c) Permittal quantity of the break drum.
 - (d) The projected area of friction surface.
- (v) Ability or capacity of break to dissipate heat equivalent to the energy being absorbed.

Types of frictional break

- ① Hydraulic Break : EX : PUMPS or hydrodynamic break / fluid agitator.
- ② Electric Break :- generators & Eddy current breaks.
- ③ Mechanical break :- EX : Bikes, car, automobile etc.

* The hydraulic & electric breaks can't bring the wheels to rest & are mostly use where large amount of energy are to be transferred. while the break is retarding the road. such as in vibratory dynameter, highway tower electric locomotives.

* These breaks are also use for retarding or controlling the speed for down wheel travel.

Mech

① The mechanical break according to the direction of rotation may be divided into the following two groups.

① Radial break

① In these break the force acting on the break drum is radial direction.

② The radial break may be subdivided into external break & internal break.

③ According to function element these breaks may be block or shoe break & band break.

② Axial break

① In these breaks the force acting on the break drum is in axial direction.

② The axial break may be disk break & cone break. The function of break is similar to clutches.

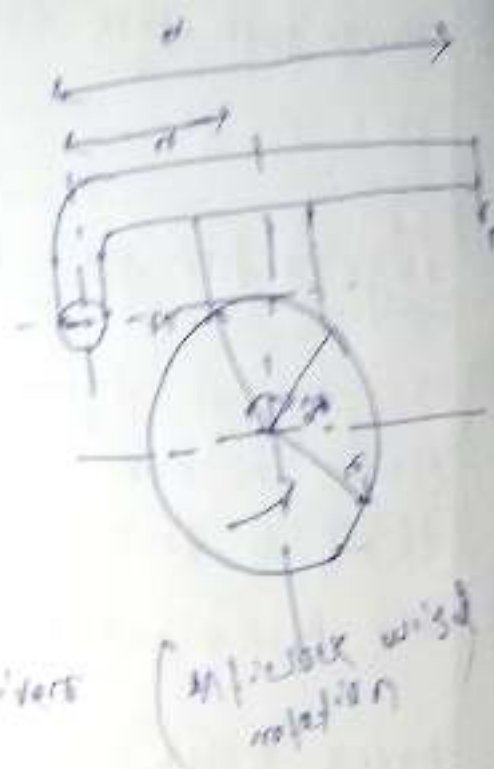
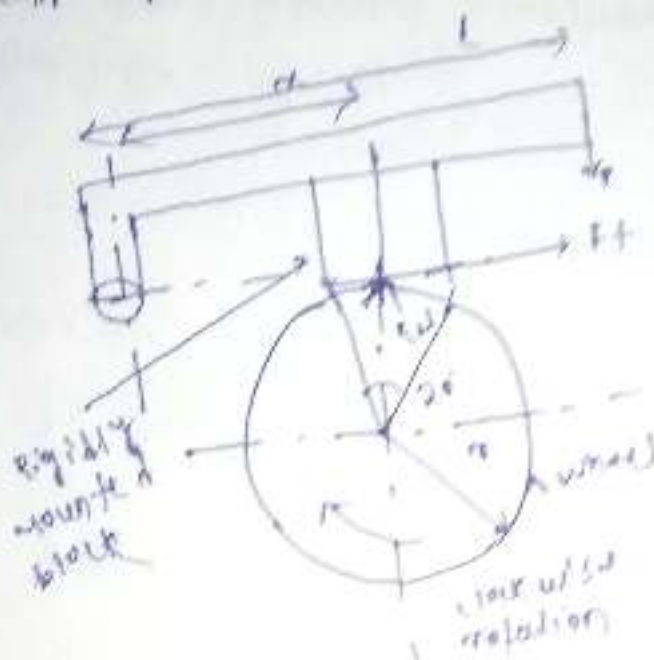
single block or shoe brake

It consists of a block or shoe which is pressed against the rim of the flywheel.

One block is made of a softer material than the rest of the wheel. This type of brake is commonly used on railway coaches & tractors.

One block is made of a softer material than the rest of the wheel. This type of brake is commonly used on railway coaches & tractors.

One block is pressed against the wheel by a force applied to one end of a lever to which the block is rigidly fixed.



P = force applied at the end of levers

$$F_f = \mu \times R_N$$

$$F_f = F_f \times r = \mu \cdot R_N \cdot r$$

$$F_f = \mu \times \frac{P \times l}{a} \times r$$

Dynamometers

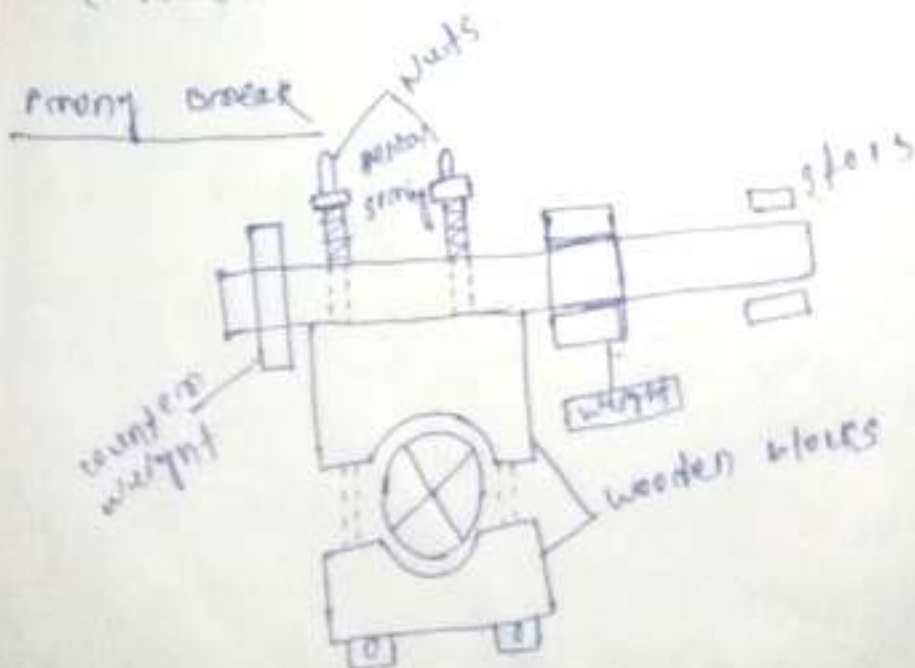
- (i) It is a device which is used to measure the frictional resistance. By knowing frictional resistance we can determine the torque transmitted & the power of the engine.
- (ii) dynamometers can be used to measure torque, torque or power.

Types of dynamometers

- (1) Absorption dynamometers: (i) Rope brake (ii) Rotor brake (iii) Hydraulic dynamometer
- (2) Transmission type dynamometers: (i) Brake transmission dynamometer (ii) Friction dynamometer (iii) Prony dynamometer

Absorption type dynamometers

- (i) This type of dynamometers are used to measure the power absorbed by friction & output of the engine to which they are coupled.
- (ii) The power absorbed is usually dissipated as heat.



① It is one of the simplest dynamometer torsion break powers.

② It is used to stop the engine using a break on the fly wheel & measure the weight which an arm attached to break which support, as it tries to rotate with the fly wheel.

③ The iron break consists in a wooden block of counter weight, vertical spring, stops

④ It works on principle of converting power into heat by dry friction.

⑤ Spring loaded bolts are provided to increase friction by tilting the wooden block.

⑥ One hole of the power absorbed is converted into heat & hence this type of dynamometer must be cooled.

⑦ Break power = $\frac{2\pi n m}{60}$ & torque = $\frac{\text{weight applied } (W)}{\text{distance } (L)}$

Rotary break dynamometer

① It is also used for measuring break power of engine

② It consists of some form of row cone around the rotating drum attached to the output shaft - one side of the row is connected to a spring balance & the other side to a loading side the power is absorbed in friction between row & the drum. Therefore drum in some break dynamometer requires cooling.

- (iii) rope break dynamometers are cheap & can be constructed quickly, but break powers can't be measured accurately because of change in coefficient of rope change temp^{er}.

$$F_p = \frac{W - S}{2} \left(\frac{D + d}{2} \right)$$

parts of rope break dynamometers

- 1) Rope :- made of synthetic fibres
- 2) pulley :- made of wood
- 3) dead weight :- cast iron
- 4) spring balance :- mild steel
- 5) ply wood frame :-

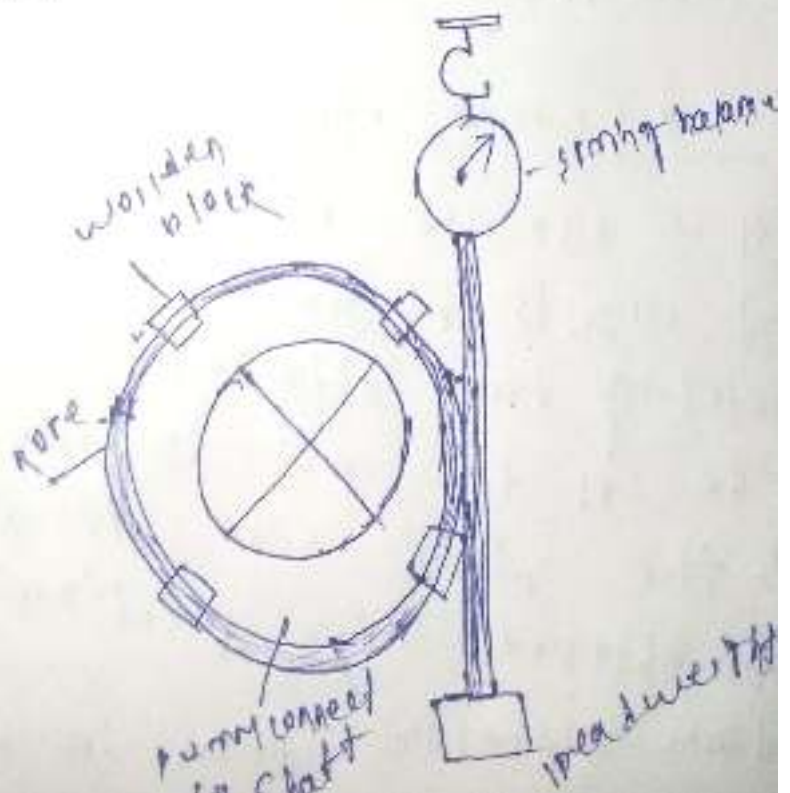
D = diameter of break drum

d = diameter of rope

S = spring balance

W = weight attached

$$P = \frac{2W - S}{2} \left(\frac{D + d}{2} \right)$$



- (2) In a more break dynamometer a rope is mounted over the pulley which is connected to the shaft of engine.
- (i) The diameter of rope depends upon the power of machine.
 - (ii) The scaling of row is done by s-y v share wooden block, which also prevent row from slipping of pulley.
 - (iii) The upper end of the row is attached to the spring balance whereas the lower end supports the weight of suspended or mass.
- As the power is high the heat produced due to friction between the rope & wheel will also high so a cooling arrangement is high, necessarily, from this the channel of fly wheel usually has hang ed on inside in which water from a read is supplied.
- (iv) The more break dynamometer is conveniently used to test the power of engine, it is easy to manufacture & required no lubricant.
- (v) As the rope is wrapped several times over the wheel the tension of the slack side of the rope can be reduce to be a negligible value.

Unit:II BELT DRIVES

Introduction

The belts or ropes are used to transmit power from one shaft to another by means of pulleys which rotate at the same speed or at different speeds.

The amount of power transmitted depends upon the following factors:

1. The velocity of the belt.
2. The tension under which the belt is placed on the pulleys.
3. The conditions under which the belt is used.

Selection of a Belt Drive

Following are the various important factors upon which the selection of a belt drive depends:

1. Speed of the driving and driven shafts,
2. Speed reduction ratio,
3. Power to be transmitted,
4. Centre distance between the shafts,
5. Positive drive requirements,
6. Shafts layout,
7. Space available, and
8. Service conditions.

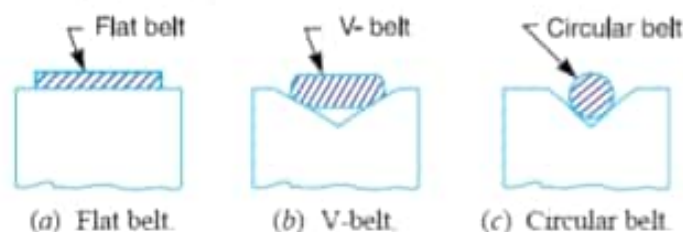
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Types of Belt Drives

The belt drives are usually classified into the following three groups :

1. **Light drives.** These are used to transmit small powers at belt speeds upto about 10 m/s, as in agricultural machines and small machine tools.
2. **Medium drives.** These are used to transmit medium power at belt speeds over 10 m/s but up to 22 m/s, as in machine tools.
3. **Heavy drives.** These are used to transmit large powers at belt speeds above 22 m/s, as in compressors and generators.

Types of Belts



Though there are many types of belts used these days, yet the following are important from the subject point of view:

1. **Flat belt.** The flat belt, as shown in Fig. (a), is mostly used in the factories and workshops, where a moderate amount of power is to be transmitted, from one pulley to another when the two pulleys are not more than 8 metres apart.
2. **V-belt.** The V-belt, as shown in Fig. (b), is mostly used in the factories and workshops, where a moderate amount of power is to be transmitted, from one pulley to another, when the two pulleys are very near to each other.

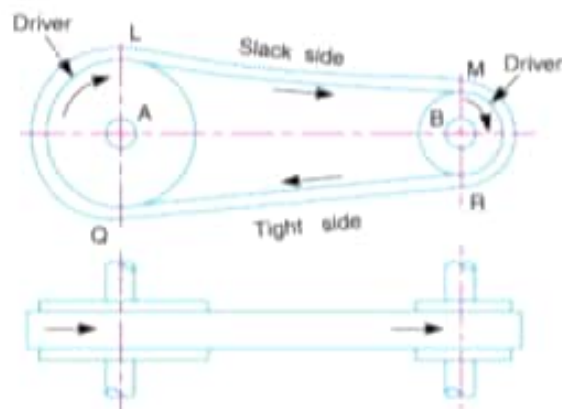
3. Circular belt or rope. The circular belt or rope, as shown in Fig. (c), is mostly used in the factories and workshops, where a great amount of power is to be transmitted, from one pulley to another, when the two pulleys are more than 8 meters apart.

If a huge amount of power is to be transmitted, then a single belt may not be sufficient. In such a case, wide pulleys (for V-belts or circular belts) with a number of grooves are used. Then a belt in each groove is provided to transmit the required amount of power from one pulley to another.

Types of Flat Belt Drives

The power from one pulley to another may be transmitted by any of the following types of belt drives:

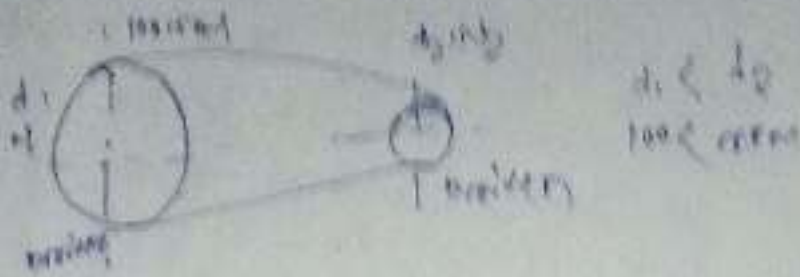
1. Open belt drive. The open belt drive, as shown in Fig. 11.3, is used with shafts arranged parallel and rotating in the same direction. In this case, the driver *A* pulls the belt from one side (*i.e.* lower side *RQ*) and delivers it to the other side (*i.e.* upper side *LM*). Thus the tension in the lower side belt will be more than that in the upper side belt. The lower side belt (because of more tension) is known as **tight side** whereas the upper side belt (because of less tension) is known as **slack side**, as shown in Fig.



2. Crossed or twist belt drive. The crossed or twist belt drive, as shown in Fig. 11.4, is used with shafts arranged parallel and rotating in the opposite directions. In this case, the driver pulls the belt from one side (*i.e.* *RQ*) and delivers it to the other side (*i.e.* *LM*). Thus the tension in the belt *RQ* will be more than that in the belt *LM*. The belt *RQ* (because of more tension) is known as **tight side**, whereas the belt *LM* (because of less tension) is known as **slack side**, as shown in Fig.

A little consideration will show that at a point where the belt crosses, it rubs against each other and there will be excessive wear and tear. In order to avoid this, the shafts should be placed at a maximum distance of $20b$, where b is the width of belt and the speed of the belt should be less than 15 m/s.

velocity ratio of belt drive (from belt drive)

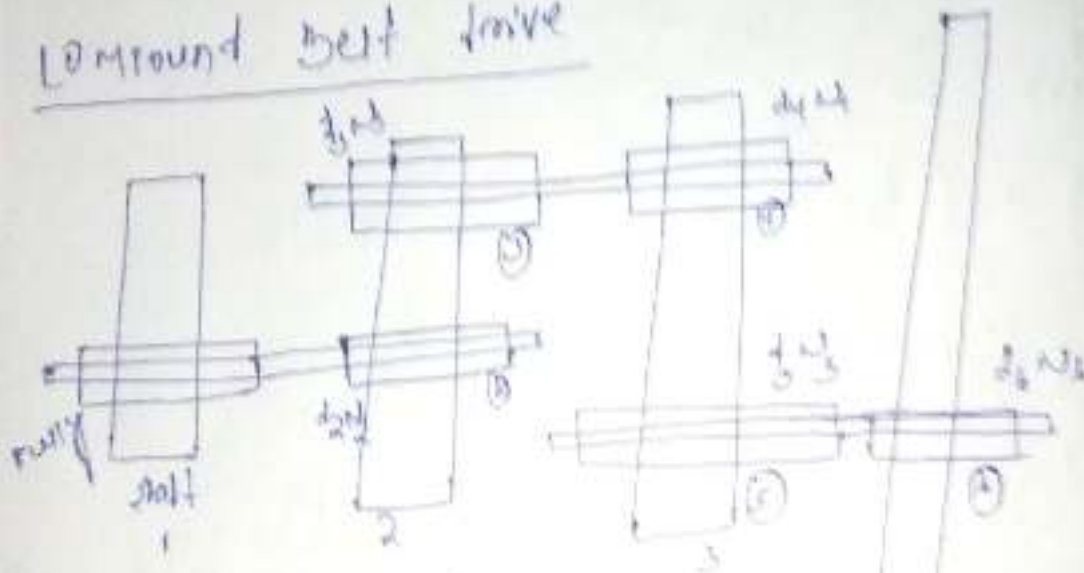


velocity of belt at driver = v_d driver

$$\pi d_1 N_1 = \pi d_2 N_2$$

$$\frac{\pi d_1 N_1}{\pi d_2 N_2} = \frac{\pi d_2 N_2}{\pi d_1 N_1} \Rightarrow \boxed{\frac{N_2}{N_1} = \frac{d_1}{d_2}}$$

Compound belt drive



$$\pi d_1 N_1 = \pi d_2 N_2 \quad \pi d_3 N_3 = \pi d_4 N_4$$

$$\pi d_2 N_2 = \pi d_3 N_3$$

$$\Rightarrow \frac{N_2}{N_1} = \frac{d_1}{d_2} \rightarrow (1) \quad \frac{N_4}{N_3} = \frac{d_3}{d_4} \rightarrow (2)$$

$$\frac{N_2}{N_3} = \frac{d_3}{d_2} \rightarrow (3)$$

$$\frac{N_2}{N_1} \times \frac{N_4}{N_3} \times \frac{N_3}{N_2} = \frac{d_1}{d_2} \times \frac{d_3}{d_4} \times \frac{d_2}{d_3}$$

$$\frac{N_4}{N_1} = \frac{d_1 \times d_2 \times d_3}{d_2 \times d_3 \times d_4}$$

SLIP OF THE BELT

SLIP
 due to insufficient frictional grip there is some forward motion of driver without carrying the belt with it & also there is some backward motion of belt without carrying the driver pulley with it. It is generally expressed as percentage.

$$\begin{array}{ccc} \text{Driver} & \xrightarrow{\hspace{10em}} & \text{Driven} \\ s_1\% & & s_2\% \\ \frac{\pi d_1 N_1}{60} - \frac{\pi d_1 N_1}{60} \times \frac{s_1}{100} & & \frac{\pi d_2 N_2}{60} \end{array}$$

$$\Rightarrow \frac{\pi d_1 N_1}{60} \left(1 - \frac{s_1}{100} - \frac{s_2}{100} \right) = \frac{\pi d_2 N_2}{60}$$

$$\Rightarrow \frac{N_2}{N_1} = \frac{d_1}{d_2} \left\{ 1 - \left(\frac{s_1}{100} + \frac{s_2}{100} \right) \right\}$$

$$\Rightarrow \frac{N_2}{N_1} = \frac{d_1}{d_2} \left(1 - \frac{s}{100} \right)$$

$$\Rightarrow \frac{N_2}{N_1} = \frac{d_1 + t}{d_2 + t} \left(1 - \frac{s}{100} \right)$$

slay side

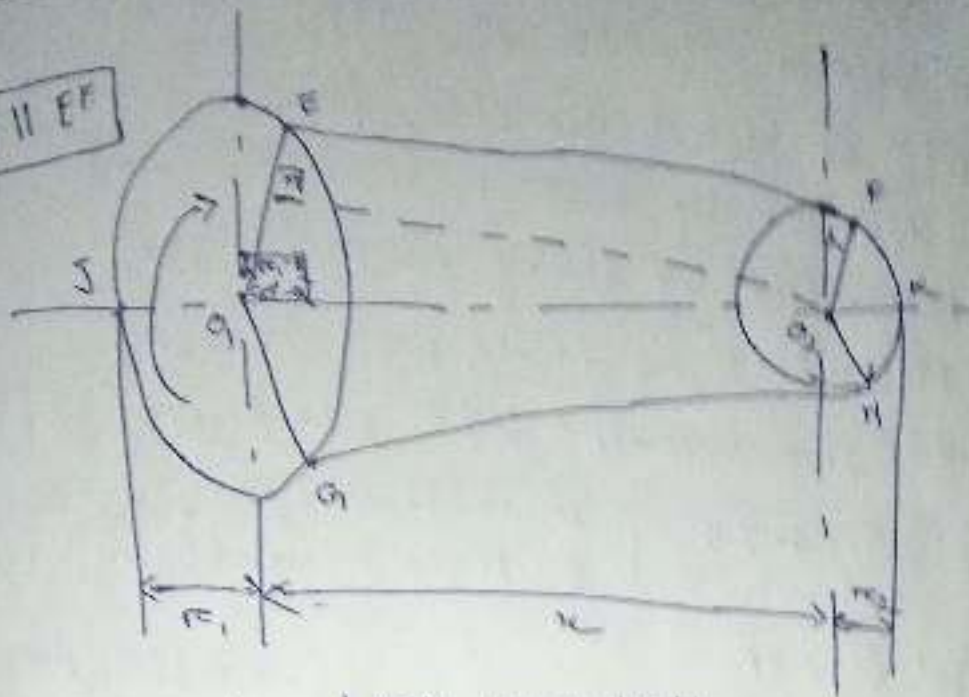
Creep

When the belt passes from the tight side to the slack side. A uniform motion of belt extent it contract again when the belt passes from slack side to tight side, due to these change of length there is a motion belt the belt & pulley this is known as the effect of creep is to reduce slightly the speed of the driven pulley or follower.

velocity ratio $\frac{N_2}{N_1} = \frac{d_1}{d_2} \times \frac{E + \sqrt{r_2}}{E + \sqrt{r_1}}$

length of open belt drive

Q.3) || EF



arc. \widehat{JSE} + \widehat{EF} + arc \widehat{FKH} + \widehat{KH}

$$\rightarrow 2(\text{Arc. } \widehat{JSE}) + 2(\widehat{EF}) + 2(\text{Arc. } \widehat{FKH})$$

$$\rightarrow 2(\text{Arc. } \widehat{JSE} + \widehat{EF} + \text{Arc. } \widehat{FKH})$$

$$\begin{aligned}
 l &= 2 \left\{ r_1 \left(\frac{\pi}{2} + \alpha \right) + x - \frac{(r_1 - r_2)^2}{2r} + r_2 \left(\frac{\pi}{2} - \alpha \right) \right\} \\
 &= 2 \left(r_1 \times \frac{\pi}{2} + r_1 \alpha + x - \frac{(r_1 - r_2)^2}{2r} + r_2 \times \frac{\pi}{2} - r_2 \alpha \right) \\
 &= 2 \left(r_1 \times \frac{\pi}{2} + r_2 \times \frac{\pi}{2} + r_1 \alpha - r_2 \alpha + x - \frac{(r_1 - r_2)^2}{2r} \right) \\
 &= 2 \left(\frac{\pi}{2} (r_1 + r_2) + \alpha (r_1 - r_2) + x - \frac{(r_1 - r_2)^2}{2r} \right) \\
 &= 2 \left(\frac{\pi}{2} (r_1 + r_2) + \frac{(r_1 - r_2)}{r} \sqrt{(r_1 - r_2)^2} + x - \frac{(r_1 - r_2)^2}{2r} \right) \\
 &= \pi (r_1 + r_2) + 2 \frac{(r_1 - r_2)^2}{r} - 2x - \frac{(r_1 - r_2)^2}{r} \quad [\text{multiplying } 2] \\
 &= \boxed{\pi (r_1 + r_2) + 2x + \frac{(r_1 - r_2)^2}{r}} \quad (\text{in radii}) \\
 &= \frac{\pi}{2} (d_1 + d_2) + 2x + \frac{(d_1 - d_2)^2}{4r} \rightarrow (\text{in diameter})
 \end{aligned}$$

* T_1 & T_2 = tension in tight side & slack side

* work per second = $(T_1 - T_2)v$ W/m/s

* v = velocity of belt in m/sec

* power transmitted by belt $P = (T_1 - T_2)v$ watt

* power transmitted by driving pulley $(T_1 - T_2)r_1$

* power transmitted by driven pulley $(T_1 - T_2)r_2$

* the relationship between tight side & slack side =

$$2.3 \log \left(\frac{T_1}{T_2} \right) = \mu \times \theta$$

[μ = coefficient of friction
 θ = angle in contact in radians]

* Centrifugal tension

(i) since the belt continuously runs over the pulley, centrifugal force is raised whose effect is to increase the tension on tight as well as slack side, the tension caused by the centrifugal force is called centrifugal tension.

(ii) it is very low

(iii) it is denoted by T_c

below the belt speed v in m/s.

$$T_c = m \times v^2$$

Gear Train

- A gear from one shaft to another shaft. Theory-of-Machines1.pdf-35.pdf speed of driven

Simple Gear Train

- Series of gears, capable of receiving and transmitting motion from one gear to another is called a simple gear train.

Train value

$$\begin{aligned} &= \frac{N_2}{N_1} = \frac{T_1}{T_2} \\ &= \frac{\text{Number of teeth on driving gears}}{\text{Number of teeth on driver gear}} \end{aligned}$$

Speed ratio

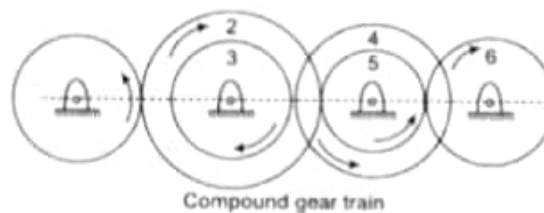
$$= \frac{1}{\text{Train value}}$$

Gears-and-gear-trains

- The intermediate gears have no effect on the speed ratio and therefore they are known as idlers.

Compound Gear Train

- When a series of gears are connected in such a way that two or more gears rotate about an axis with the same angular velocity.



Train value

$$= \frac{\text{Product of number of teeth on driving gears}}{\text{Product of number of teeth on driven gears}}$$

Planetary or Epicyclic Gear Train

- A gear train having a relative motion of axes is called a planetary or an epicyclic gear train. In an epicyclic train, the axis of at least one of the gears also moves relative to the frame.
- If the arm a is fixed the wheels S and P constitute a simple train. However, if wheel S is fixed so that arm a can rotate about the axis of S. The P would rotate around S therefore it is an epicyclic train

CHAPTER 4

Function of Governor

Classification of Governor

- (1) Conceptual explanation of sensitivity & stability of Isochronisms
- (2) Function of fly wheel
- (3) Comparison between fly wheel & governor.
- (4) Function of energy & coefficient of fluctuation of speed.

GOVERNOR

The function of a governor is to maintain or regulate the speed of an engine with specified limit whenever there is variation of load.

Types of Governor / Classification of Governor

The broadly classification of the governor are given below

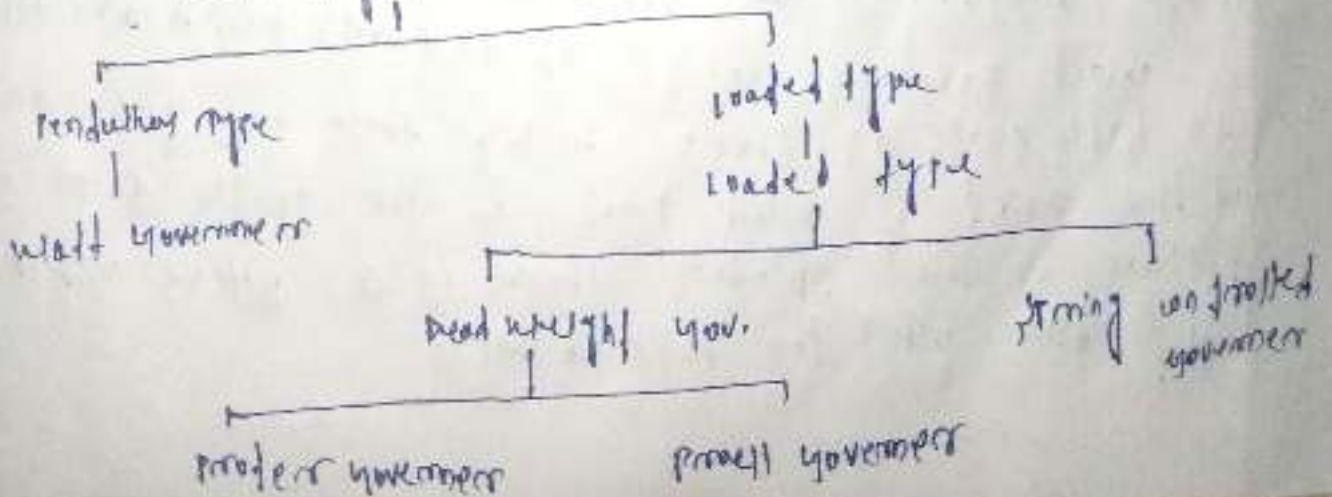
Centrifugal Governor

In this type of governor, the action of governor depends upon the centrifugal forces produced by the masses of two balls.

Controlled Governor

In this type of governor, position of the balls are affected by the forces set up by an angular acceleration or deceleration of the given spindle in addition to centrifugal forces on the balls.

Centrifugal Governor

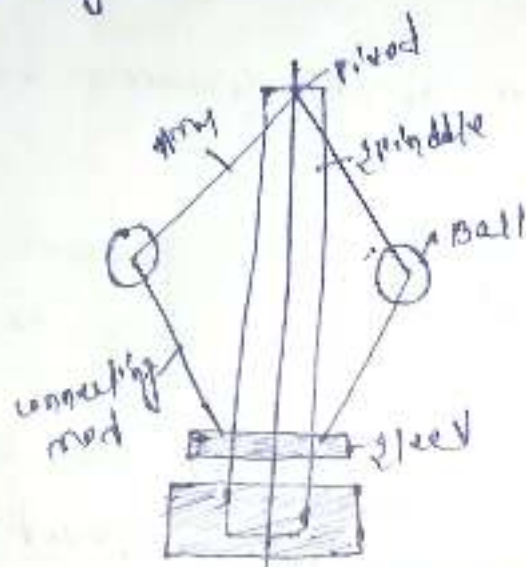


- spring controlled governor
- Hamdrell governor
- Hamdang governor
- Wilson, Hamdrell governor
- Pickering governor

Working of GOVERNOR

Watt Governor

The simplest form of a centrifugal governor is a watt governor. It is basically a conical pendulum with arms of negligible mass. The arms are attached to a sleeve of negligible mass. The arms of governor may be connected to the spindle in following ways.



Watt governor

Watt governor is used to supply the required amount of fuel at different speed. The main reason is to control the engine speed according to the condition.

Watt governor consists of two balls which are attached to both arms as shown in fig. These arms are connected at the point is called pivot on the spindle. At the bottom of the spindle there is a sleeve which moves up & down with the help of balls.

⑤ when the balls rotate with high speed at a fixed center of the pivot the arms get stretched & the belt of connection between the ball & the sleeve gets lifted from the bottom being away from the center of the spindle. on this type of governor when the ball rotates at high speed almost both the balls get in straight line which is also the final position of balls that rotates & belt to supply fuel.

Watt governor is not suitable to supply a large quantity of fuel this is used at only low speeds.

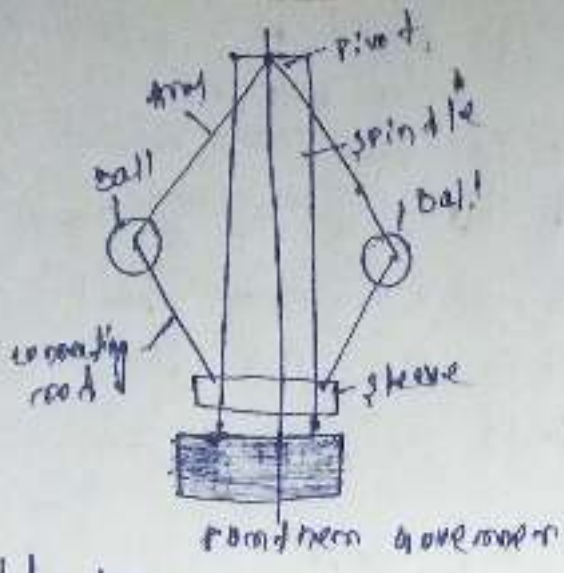
Pontons governor

Pontons governor is dead weight loaded type of gravity controlled centrifugal governor. It is similar to watt governor when a heavy central load is attached to the sleeve of watt governor, it becomes a Pontons governor.

Working

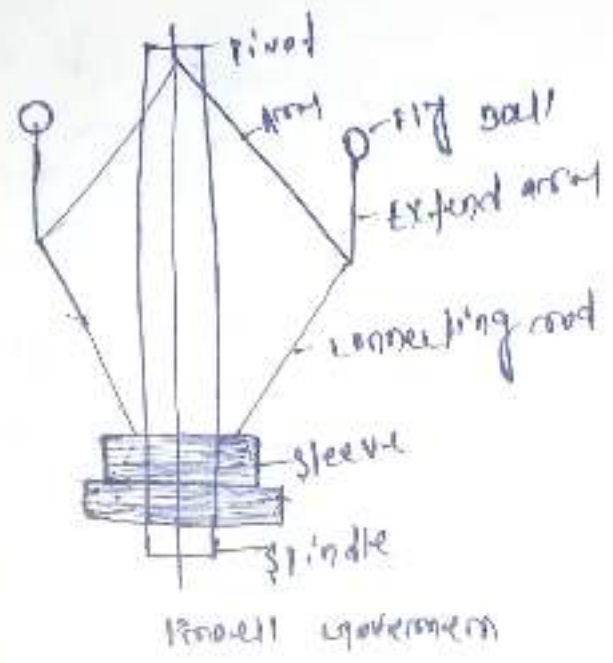
The engine is connected to the central spindle of governor through gear trains. When the load on an engine decreases, there will be a sudden increase in speed of the engine. Governor spindle speed also increases. The centrifugal effect tends to move the balls outward direction. The upper arms of ball pivot at the top. Hence the lower arm pushes the sleeve upward as ball move outward. It decreases the fuel supply. Hence speed is maintained. In case of increasing the load speed of the engine decreases.

①



PROELL GOVERNOR

Proell governor is a type of gravity controlled centrifugal governor.



Working

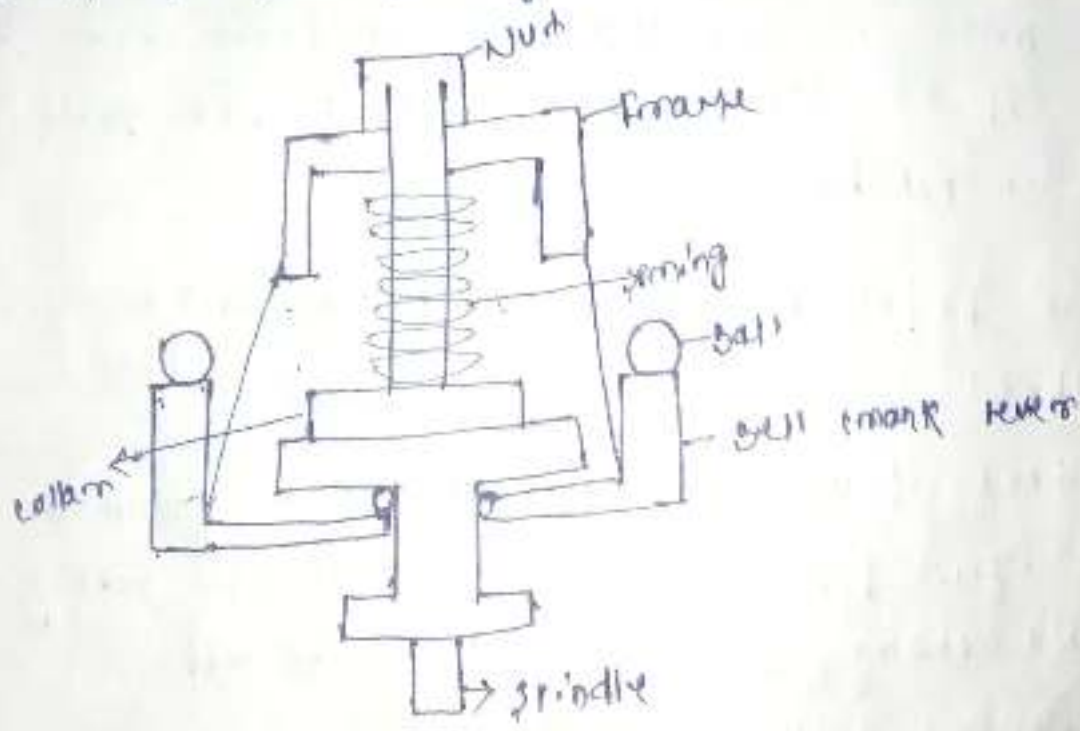
When the load on the engine decreases, the speed of engine increases suddenly & also spindle rotation speed is increased as the spindle is connected to the engine. As the rotation of spindle becomes fast, the arms pivoted to top of spindle also rotates with high speed & the balls move outward due to increased centrifugal force on the balls. When the ball move outward, the sleeve connected to the arm moves up & actuates

5) a mechanism which closes the throttle valve & decreases the fuel supply which decreases the engine speed. Hence the engine speed is maintained.

on the other hand, when the load on the engine increases, speed of the engine decreases.

HARTWELL GOVERNER

Hartwell governor is basically a centrifugal governor with a spring-loaded weight instead of dead weight on the sleeve to increase the speed of the balls required to lift the sleeve on the spindle, which is enable the governor to operate the mechanism to give necessary change in the fuel supply.



[Hartwell governor]

FLYWHEEL

A flywheel is a heavy rotating body which acts as a reservoir of energy. It acts as a bank of energy between the energy source & machinery.

Energy stored in a flywheel is in the form of kinetic energy.

Function of Flywheel

- (1) when the power available at variable rate but is required at uniform rate. Ex the machinery driven by reciprocating internal combustion engine.
- (2) when the power is available at uniform rate but we need it at non uniform rate. Then power is required in punching press.

Difference between flywheel & governor

Flywheel	Governor
(1) A flywheel is used to mitigate cyclic fluctuations in available energy.	(1) but a governor is used to adjust the supply of fuel as per the load.
(2) the energy stored in flywheel is kinetic which is easily available.	(2) but governor mechanism involves friction.
(3) fly wheel is not used when cyclic fluctuation of energy is small or negligible.	(3) unlike a governor is necessary for all the type of engines because it varies the fuel supply as per demand.

(i) Fly wheel has no influence on the mean speed of engine.

(ii) Governor has no influence in cyclic fluctuations in energy.

(iii) Fly wheel controls cyclic fluctuations in energy.

(iv) Governor controls mean speed of the engine.

Fluctuation of ENERGY

The variations of energy above & below the mean resisting torque line are called fluctuations of energy.

Co-efficient of fluctuation of energy ::

It may be defined as the ratio of the maximum fluctuation of energy to the workdone per cycle.

$$E = \frac{\text{Maximum fluctuation of energy}}{\text{Work done per cycle}}$$

CHAPTER - 5

①

Balancing of Machine

- (1) Concept of static & dynamic balancing
- (2) Static balancing of rotating parts
- (3) Principle of balancing of non-rotating parts.
- (4) Difference between static & dynamic balancing.

Static Balancing

- (i) If the shaft carries a number of unbalanced masses such that the center of mass of the system is said to be static balance.
- (ii) A rotating mass is said to be statically balanced if the rotating mass can rest, without turning at any angular position in its bearing.
- (iii) static balancing is a balance of force due to action of gravity.

Dynamic Balancing

- (i) A system of rotating masses is dynamically balanced whenever there does not exist any resultant centrifugal force as well as resultant couple.

Q2
A rotating mass is said to be dynamically balanced when it does not vibrate in its running state. To make a rotating mass dynamically balanced, it must be first statically balanced.

Balancing of rotating parts

The balancing of rotating bodies is important to avoid vibration. In heavy industrial machines such as gas turbines & electric generators, vibration can cause catastrophic failure, as well as noise & discomfort. In the case of narrow wheel, balancing simply involves moving the center of gravity to the center of rotation. For a system to be in complete balance both force & couple polygons should be closed. In order to prevent the effect of centrifugal force, balancing is important to design the machine parts so wisely, that the unbalance is reduced up to the minimum possible level or eliminated completely.

Static balance

Static balance occurs when the center of gravity of an object is on the axis of rotation. The object can therefore remain stationary with the axis horizontal, without the application of any braking force.

- (3) It has no tendency to rotate due to the force of gravity. This is seen in bike wheels where the reflective plate is placed opposite the valve to distribute the centre of mass to the centre of the wheel. Other examples are grindstones, discs on car wheels.

Difference between static & dynamic balancing?

Static balancing

Dynamic balancing

- (i) Static balance refers to the ability of a stationary or object centre of gravity is on the axis of rotation.
- (ii) In static balancing, the rod around which mass is rotating is to be fixed.
- (iii) Static balance will be produced if the sum of the weight about the axis of rotation is zero.
- (i) Where as dynamic balance is the ability of an object to balance whilst in motion or when switching between positions.
- (ii) Where as in dynamic balancing, the rod moves along with the rotating mass.
- (iii) In dynamic balanced when there does not exist any resultant centrifugal force as well as resultant couple.

- Q.1 (a) what do you understand by 'Lower pair' & Higher pair?
 - (i) difference between structure of Machine.
 - (ii) discuss binary, ternary & quaternary link with sketches.

- Q.2. what are the various type of bearings? Derive an expression for the frictional torque of a flat pivot bearing by taking into consideration:
 - (i) uniform pressure theory.
 - (ii) uniform wear theory.

- Q.3. Derive an expression for limiting tension ratio in case of flat belt drive?

or Derive the length of open belt drive?

- Q.4. What do you understand by 'gear train'? Explain with a neat diagram the following:
 - (i) compound gear train.
 - (ii) Epicyclic gear train.

- Q.5. What is the use of a governor? Explain with the help of neat sketch the working of Porter's governor & Hartnell governor.

- Q.6. What do you mean by 'balancing of rotating masses'? Explain the method of balancing several masses rotating in the same plane.

Q.1 what do you mean by:-

- (a) free & forced vibrations
- (b) underdamped & damped vibrations.

Q.2 what do you mean by damping? Explain the following

- (a) viscous damping
- (b) Eddy current damping

Q.3 write short note on the following:-

- (i) Limiting angle of friction.
- (ii) slip in belts.
- (iii) comparison between flywheel & governor.

SET-2

- Q.1 (a) what is a kinematic chain?
- (b) what is the diffrent between lower pair & higher pair? Explain briefly different types of lower pair.
- (c) what is four bar mechanism? state & explain different inversion of four bar mechanism.

Q.2 (a) what is a Bearing?

- (b) state the classification of bearings. with neat sketch of Ball bearing.
- (c) Derive the torque transmitted in that bearing considering the uniform wear.

3) what do you mean by absorption type dynamometer?
(a) describe the length of span best drive.

(1) A shaft has number of collars integral with it. The external diameter is 400 mm & shaft diameter 250 mm. If the intensity of pressure is 0.35 N/mm². & coefficient of pressure traction is 0.13. Estimate

- (i) power absorbed on the shaft runs 150 rpm carrying a load 150 kW.
- (ii) No. of collars.

(4) (a) what is a gear train?

(b) with neat sketch define ritch circle, circular pitch.

(5) (a) state the function of flywheel.

(b) with neat sketch explain the working of porter governor.

(6) (a) what is the difference between static & dynamic balancing?

(b) Explain briefly natural, forced & damped vibration.

(c) describe the method of balancing of several masses rotating different planes.

- 7.
- (a) state the function of cut & followers.
 - (b) Explain the working principle of cycle jump.
 - (c) Function of governor? Explain the term sensitivity & isochronism of a governor.

